

## Hipparcos red stars in the $H_pV_{T2}$ and $V_I$ systems<sup>\*,\*\*</sup>

I. Platais<sup>1,2</sup>, D. Pourbaix<sup>1,\*\*\*</sup>, A. Jorissen<sup>1,\*\*\*</sup>, V. V. Makarov<sup>2,3</sup>, L. N. Berdnikov<sup>4</sup>, N. N. Samus<sup>5,4</sup>,  
T. Lloyd Evans<sup>6</sup>, T. Lebzelter<sup>7</sup>, and J. Sperauskas<sup>8</sup>

<sup>1</sup> Institut d’Astronomie et d’Astrophysique, Université Libre de Bruxelles, CP 226, Boulevard du Triomphe, 1050 Bruxelles, Belgium

<sup>2</sup> Universities Space Research Association, Division of Astronomy and Space Physics, 300 D Street SW, Washington, D.C. 20024, USA

<sup>3</sup> U.S. Naval Observatory, 3450 Massachusetts Ave., NW, Washington D.C. 20392-5420, USA

<sup>4</sup> Sternberg Astronomical Institute and Isaac Newton Institute of Chile, Moscow Branch, 13 Universitetskij Prosp., Moscow 119992, Russia

<sup>5</sup> Institute of Astronomy, Russian Academy of Sciences, 48 Pyatnitskaya Str., Moscow 119017, Russia

<sup>6</sup> School of Physics and Astronomy, University of St Andrews, North Haugh, St Andrews, Fife, Scotland KY16 9SS

<sup>7</sup> Institut für Astronomie, Universität Wien, Türkenschanzstr. 17, 1180 Vienna, Austria

<sup>8</sup> Vilnius University Observatory, Ciurlionio 29, Vilnius 2009, Lithuania

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**Abstract.** For Hipparcos M, S, and C spectral type stars, we provide calibrated instantaneous (epoch) Cousins  $V-I$  color indices using newly derived  $H_pV_{T2}$  photometry. Three new sets of ground-based Cousins  $VI$  data have been obtained for more than 170 carbon and red M giants. These datasets in combination with the published sources of  $VI$  photometry served to obtain the calibration curves linking Hipparcos/Tycho  $H_p - V_{T2}$  with the Cousins  $V-I$  index. In total, 321 carbon stars and 4464 M- and S-type stars have new  $V-I$  indices. The standard error of the mean  $V-I$  is about 0.1 mag or better down to  $H_p \approx 9$  although it deteriorates rapidly at fainter magnitudes. These  $V-I$  indices can be used to verify the published Hipparcos  $V-I$  color indices. Thus, we have identified a handful of new cases where, instead of the real target, a random field star has been observed. A considerable fraction of the DMSA/C and DMSA/V solutions for red stars appear not to be warranted. Most likely such spurious solutions may originate from usage of a heavily biased color in the astrometric processing.

**Key words.** stars: late type – stars: carbon – techniques: photometric – techniques: radial velocities

### 1. Introduction

The Hipparcos Catalogue (ESA 1997) includes two sets of Cousins  $V-I$  color indices – a functional  $V-I$  (entry H75 in the main Hipparcos Catalogue) and a best available  $V-I$  at the time of the Catalogue’s release (entry H40). This color index is an important temperature indicator for late-type stars (Dumm & Schild 1998; Bessell et al. 1998). Since only 2989 Hipparcos stars are listed as having direct measurements of the Cousins  $V-I$  index, nineteen different methods of variable accuracy were used to obtain  $V-I$  photometry (see ESA 1997, Sect. 1.3, Appendix 5). In numerous cases the reductions of Hipparcos

$V-I$  photometry relied heavily upon the satellite’s star mapper photometry – the Tycho  $B_T - V_T$  color indices. However, the Tycho photometric system alone is not well-suited for the studies of fainter red stars. A combination of intrinsically low fluxes from these stars in the  $B_T$  bandpass and a short crossing time ( $\sim 22$  ms) of the star mapper’s four vertical slits resulted in low  $S/N$  ratios. This, in combination with the residual bias that was not fully corrected by the de-censoring analysis (Halbwachs et al. 1997) in deriving the Tycho photometry for faint stars, diminishes the reliability of much of the published Hipparcos  $V-I$  indices for stars with  $V-I \gtrsim 1.5$ . As demonstrated by Koen et al. (2002), the listed Hipparcos  $V-I$  photometry of red stars shows a disappointingly large scatter with respect to the ground-based photoelectric  $V-I$  measurements. In extreme cases the disagreement can reach up to 2–3 mag.

Our interest in the  $V-I$  photometry of red stars is primarily motivated by the potential effect of incorrect  $V-I$  color indices on the chromaticity corrections in Hipparcos astrometry. On average, a one magnitude offset in the  $V-I$  value could introduce a  $\sim 1$  mas bias in the star’s position (abscissa) along the

Send offprint requests to: D. Pourbaix,  
e-mail: pourbaix@astro.ulb.ac.be

\* Based on observations from the Hipparcos astrometric satellite operated by the European Space Agency (ESA 1997).

\*\* Table 7 is only available in electronic form at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsweb.u-strasbg.fr/cgi-bin/qcat?J/A+A/397/997>

\*\*\* Research Associate, F.N.R.S., Belgium.

scan direction. Besides grossly incorrect  $V-I$  indices for some red stars (Koen et al. 2002), there is a systematic color bias related to neglecting in the Hipparcos reductions the intrinsic color variation in large amplitude variables such as Miras.

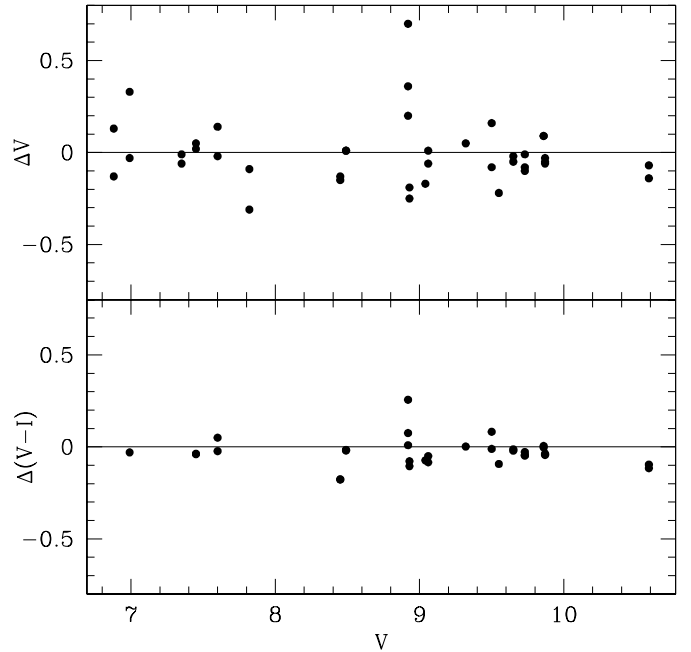
In retrospect, the Hipparcos  $V-I$  photometry would have gained considerably from the parallel-in-time ground-based  $V-I$  observations of stars with extreme colors and/or considerable color variability. For a number of reasons, most importantly, a prorogated decision to choose the  $V-I$  index, this opportunity was lost. Is it possible to improve the Hipparcos  $V-I$  photometry now? Here we attempt to answer this question. It appears that high-grade  $V-I$  photometry for red stars is possible down to  $V \approx 8$  and may even be used to obtain an estimate of effective temperatures. In general, the re-calibrated  $V-I$  photometry is useful in identifying some difficult cases in the Hipparcos Catalogue, such as red and variable stars in binary systems. Throughout the paper we refer to Cousins  $V-I$  color indices, unless it is explicitly stated otherwise.

## 2. Ground-based Cousins $VI$ photometry

The advantages of the broadband Cousins  $VRI$  photometric system such as high internal precision and maintaining this precision over the whole range of spectral types are discussed by Bessell (1979). This system emerged with the advent of GaAs photocathode photomultipliers in the early 1970s. There are two issues which should be considered in the broadband photometry of red stars. First, the majority of cool red stars are variable and no standard stars are available redder than  $V-I \approx 3$ . Second, the presence of numerous molecular bands in the spectra of red stars requires stable and easily reproducible bandpasses in order to avoid possible nonlinear transformations from the instrumental to the standard system. In other words, to exclude the transformation uncertainties, such stars must be observed in the natural Cousins  $VRI$  system, i.e. using the same filters and detector. Examination of the published sources of Cousins  $VRI$  photometry indicates that many extremely red Hipparcos stars actually lack this photometry. Therefore, we have obtained new sets of  $UBVRI$  photometry of the Southern carbon stars and  $BVI$  photometry for the reddest M and C spectral-type stars.

### 2.1. Carbon star photometry at SAAO

The observations of 85 carbon stars including a few hydrogen-deficient (Hd) stars were made in 1984 and 1987 using the single channel Modular Photometer on the 0.5 m reflector at the Sutherland station of the SAAO. The photometer uses a Hamamatsu R943-02 GaAs photomultiplier and a filter set which reproduces the Johnson  $UBV$  and Cousins  $(RI)_C$  photometric systems, with a need for only very small linear and non-linear terms in transformations onto the standard system. The observations were made with frequent reference to the E-region standard stars of Menzies et al. (1989). The results of  $UBV(RI)_C$  photometry are provided in Table 1. The CGCS numbers are those in Stephenson (1989). The last column indicates the total number of observations, usually obtained over 2–3 nights. The standard error of individual observations is about 0.01 mag.



**Fig. 1.** Differences between the  $V$ -magnitude (top panel) and  $V-I$  color index (bottom panel) from Table 1 and that of Walker (1979). A relatively large spread visible in the top panel is mainly due to the variability.

It was necessary, however, to extrapolate the color system as some of the stars here are redder than any standard star in one color or another and in any case these are carbon stars (or helium stars in the case of Hd stars) whose colors differ systematically from the oxygen-rich M spectral type standard stars. In addition, most of our programme stars are variable to some degree. All cases with apparent variability or uncertain photometry are marked by (v) or (:), accordingly. Since in the  $UBVRI$  photoelectric photometry the aperture size varied from 20'' to 40'', a nearby optical component, marked in Table 1, may affect the accuracy of our photometry. The generally good agreement (Fig. 1) with the data of Walker (1979), whose observations were made with separate blue and red sensitive photomultipliers and a different filter set, give added confidence to the results.

### 2.2. Photometry of red stars at Siding Spring Observatory

In March–April 2002 additional  $BVI_C$  photometry for 47 very red Hipparcos carbon and M stars was secured at the Siding Spring Observatory, Australia. The data were obtained using the 24 inch reflector and a single channel photometer. A cooled unit containing a Hamamatsu GaAs photomultiplier tube and a set of filters allow us to match closely the Cousins photometric system, in the same way as was done at SAAO. Each night a set of the E-region standards (Menzies et al. 1989) was measured to obtain the atmospheric extinction coefficients and the transformation coefficients to the standard system. Mean transformation coefficients for this run were as follows:  $\xi_V = 0.005$ ,

**Table 1.** SAAO photometry of selected carbon stars.

CGCS	HIP	GCVS	V	B-V	U-B	R-I	V-I	n	CGCS	HIP	GCVS	V	B-V	U-B	R-I	V-I	n
177		AM Scl	12.33	2.16	3.42:	1.02	1.85	3	3810			10.39	1.41	0.90	0.83	1.63	5
196	5809		10.02	1.33	1.34	0.59	1.09	5	3813			11.02v	2.39	2.61	1.30	2.45	4
258			10.19	1.31	1.16	0.61	1.12	6	3842	85750		9.37	1.88	2.02	0.88	1.66	5
327	10472	V Ari	8.71	2.19	2.45	1.16	2.15	6	3855 <sup>a</sup>			11.20	1.30	0.91	0.64	1.19	2
378	12028		8.16	1.24	0.77	0.60	1.09	4	3864 <sup>a</sup>	V450 Sco		10.30v	2.38	3.56:	1.50	2.82	4
576	17933		8.30	1.65	1.72	0.75	1.41	6	3938	88584	W CrA	9.95	1.89	1.83	0.99	1.81	4
639	19269		10.66	1.23	0.68	0.72	1.43	4	3939		V1783 Sgr	10.53	1.54	1.01	0.94	1.74	3
725	21051		8.91	1.14	1.12	0.55	1.04	6	3957	88887		9.80	1.52	1.18	0.96	1.87	4
1380	31725		9.37	1.37	1.28	0.58	1.07	3	3958			10.45	1.34	0.95	0.66	1.23	6
1460	33042	KY CMa	10.75	2.73	4.00:	1.33	2.42	4	3966 <sup>a</sup>			11.06v	1.95	1.76	1.05	1.95	4
1489	33550	RV Mon	6.88	2.65	7.16:			3	3992	89783	FO Ser	8.42	1.85	1.85	1.15	2.21	3
1507	33794	V614 Mon	7.32v	1.76	2.14:	1.13		4	4021	90694		9.90	1.39	0.92	0.81	1.60	3
1659	35549	MY CMa	10.63	2.44	3.08:	1.36	2.55	3	4042			11.13	2.08	2.01	1.05	1.90	3
1790			9.58	1.85	2.15	1.11	2.07	3	4070			9.33	1.29	1.00	0.58	1.06	3
1871 <sup>a</sup>			10.16	1.23	0.82	0.56	1.02	3	4086	91929	RV Sct	10.02	2.35	2.52	1.54	2.92	3
1968	38787	V406 Pup	7.62v	3.20:	4.60:	1.40		4	4094	92115		9.49	0.83	0.47	0.42	0.67	3
2153	40805	V433 Pup	9.54v	1.67	1.66	1.07	2.05	3	4145	93181	V4152 Sgr	9.33	1.16	0.84	0.57	0.94	1
2331	43093	UZ Pyx	7.32	2.01	2.99	1.09		4	4168			9.95	1.29	1.22	0.59	1.10	4
2449	45295	GM Cnc	8.65	1.57	1.50	1.00	1.93	3	4179 <sup>a</sup>	94049		10.29	1.26	0.83	0.60	1.14	3
2759	50994		9.53	1.30	1.07	0.59	1.09	4	4194	94294	V1445 Aql	11.31	2.08	2.35:	1.31	2.51	3
2787			9.48	1.29	0.96	0.60	1.11	5	4196			10.82	1.42	1.24	0.68	1.31	3
2829	52271		7.08	1.33	1.16	0.59	1.11	4	4229	94940	V1942 Sgr	7.06	2.56	4.45:			1
2852	52656	TZ Car	8.71v	2.10	2.60	1.30	2.50	4	4247	95289		6.96	1.07	0.58	0.57	0.97	1
2925	53810		8.33	1.16	1.08	0.55	1.05	4	4498			11.14	1.32	1.19	0.61	1.12	3
2975	54806		10.16	1.44	1.14	0.85	1.64	4	4524 <sup>a</sup>	98117		9.18	1.21	0.61	0.54	1.01	3
2986		DI Car	10.5 v	1.4 v	1.30v	0.64v	1.2v	6	4567	98223		9.35	2.03	2.06	0.92	1.73	4
3001	55448	V905 Cen	10.51v	1.80	1.87	1.15	2.20	4	4595	98542	V1468 Aql	10.36	2.04	2.55	1.16	2.13	3
3066	56551		8.76	1.06	0.51	0.51	0.92	4	4598	98538	V1469 Aql	8.37	2.08	2.52	0.96	1.77	3
3141	58513	DD Cru	8.87	2.20	2.94:	1.04	2.03	4	4614	98958		8.05	1.07	0.97	0.51	0.98	3
3199		TV Cen	8.02v	2.74	2.89	1.42	2.57	5	4873	101277	BI Cap	9.67v	1.42	1.09	0.95	1.85	3
3227	60534	S Cen	7.66v	1.89	2.70:	1.11	2.10	5	4972	102726		10.30	1.29	0.92	0.63	1.14	3
3286	62401	RU Vir	9.97v	4.63	5.10:	1.99	3.42	4	4978	102706		8.16v	1.28	0.94	0.58	1.14	3
3335	63955		8.50	1.17	1.03	0.54	1.01	4	5147	104522		9.82	1.56	1.49	0.97	1.86	6
3405	66070	V971 Cen	8.50	1.87	2.12	1.02	1.94	5	5227	105212		9.67	1.26	0.87	0.57	1.06	5
3492	70339	RS Lup	9.62v	2.69	4.70:	1.35	2.46	5	5408	107349	BU Ind	10.15v	1.45	1.28	0.95	1.85	4
3545			10.95	1.40	0.80	0.77	1.44	5	5420	107490	RR Ind	9.34v	2.84v	5.29v	1.31v	2.36v	7
3558			10.42	1.51	1.26	1.01	1.98	5	5561	108953	HP Peg	8.89	1.45	1.13	0.61	1.15	2
3606	75694	HM Lib	7.48v	1.20	0.86	0.61	1.07	4	5627			10.71	1.72	1.63	0.82	1.50	3
3657			9.84	1.59	1.32	0.69	1.28	5	5761	113150		10.82	1.17	0.55	0.59	1.11	6
3672	79484		10.36	1.69	1.46	0.77	1.42	5	5823	114509		9.26	1.22	0.81	0.60	1.11	5
3707	81254	LV TrA	8.30	0.95	0.67	0.45	0.72	5	5937	117467		8.48	1.37	1.30	0.62	1.15	5
3756	83387	T Ara	9.03v	2.78	4.90:	1.40	2.55	5	5980	168		9.55	1.12	0.48	0.51	0.96	4
3765			9.11	1.39	1.26	0.65	1.25	4									

<sup>a</sup> Close companion: 1871 (9'' separation, bright); 3855 (15''); 3864 (11''); 3966 (15'', bright), 4179 (14''), 4524 (13'' & 18'').

$\xi_{B-V} = 1.010$ , and  $\xi_{V-I_C} = 1.015$  (see Berdnikov & Turner 2001, Eq. (2)). Hence the instrumental system is very close to the standard  $BVI_C$  system, which greatly alleviates the problem of color-related extrapolation in the reductions of very red programme stars. Every 60–90 min two standard stars (red and blue) were used to define instantaneous zeropoints in the transformation relations. Some very bright programme stars were observed with the addition of an Oriel 50550 neutral density filter. The  $BVI_C$  photometry is presented in Table 2.

### 2.3. VRI photometry of red variables with APT

Since 1996 the University of Vienna has been obtaining  $UBV(RI)_C$  photometry in Arizona using two 0.75 m automatic photoelectric telescopes<sup>1</sup> (APT) located on the grounds of Fairborn Observatory. The photometer of the APT dubbed Amadeus (Strassmeier et al. 1997), has an EMI-9828 S-20/B

<sup>1</sup> Operated by the University of Vienna and the Astrophysikalisches Institut, Potsdam.

**Table 2.** *BVI* photometry at Siding Spring.

HIP	GCVS	JD-2 450 000	<i>V</i>	<i>B-V</i>	<i>V-I</i>
23203	R Lep	2353.915	11.63	4.60	3.75
23636	T Lep	2376.883	12.18	1.75	5.92
24055	U Dor	2376.977	8.61	1.62	4.17
		2378.889	8.62	1.60	4.17
25004	V1368 Ori	2376.871	10.07	3.53	3.48
25673	S Ori	2376.874	8.71	1.65	4.66
28041	U Ori	2376.870	10.22	1.87	5.40
		2378.880	9.94	2.00	5.45
29896	GK Ori	2353.919	9.96	4.22	3.52
34413	W CMa	2361.980	6.74	2.69	2.43
35793	VY CMa	2353.922	8.19	2.28	3.28
39967	AS Pup	2376.928	9.01	1.50	4.61
		2378.919	9.01	1.48	4.60
40534	R Cnc	2376.925	11.22	2.26	5.77
		2378.931	11.31	2.30	5.81
41061	AC Pup	2376.908	8.99	3.23	2.78
		2378.933	9.04	3.31	2.80
43905	T Cnc	2353.926	8.23	4.31	3.29
48036	R Leo	2353.929	7.28	1.71	5.02
53085	V Hya	2354.036	7.34	4.66	3.61
53809	R Crt	2354.038	8.43	2.01	4.81
57607	V919 Cen	2354.039	6.93	1.59	4.15
63642	RT Vir	2354.175	8.25	1.81	4.67
64569	SW Vir	2354.178	7.09	1.72	4.53
67419	W Hya	2354.179	8.42	2.44	5.64
69754	R Cen	2354.178	7.48	1.94	4.22
70969	Y Cen	2354.181	8.12	1.60	4.50
75393	RS Lib	2354.182	10.79	1.96	5.41
80365	RT Nor	2354.183	10.08	1.01	0.94
80488	U Her	2379.168	8.68	1.60	4.84
80550	V Oph	2357.168	9.21	4.13	3.19
82392	V TrA	2364.266	8.16	2.23	2.24
84876	V1079 Sco	2354.185	9.40	3.31	3.34
85617	TW Oph	2357.168	7.86	4.24	3.32
85750		2357.174	9.36	1.93	1.65
86873	SZ Sgr	2357.170	8.78	2.36	2.73
87063	SX Sco	2357.172	7.65	2.86	2.65
88341	V4378 Sgr	2379.172	10.37	2.97	3.24
88838	VX Sgr	2379.174	9.20	2.82	4.34
89739	RS Tel	2357.254	10.01	0.85	0.77
90694		2357.252	9.93	1.37	1.61
93605	SU Sgr	2357.258	8.33	1.73	4.39
93666	V Aql	2357.260	6.78	3.98	3.07
98031	S Pav	2379.201	7.82	1.64	4.63
99082	V1943 Sgr	2379.195	7.67	1.77	4.58
99512	X Pav	2357.256	8.97	1.91	4.92
100935	T Mic	2357.265	7.68	1.78	4.76

multi-alkali cathode photomultiplier, which is sensitive up to ~900 nm. This photomultiplier in combination with filters close to those suggested by Bessell (1976) reproduces a  $V(RI)_C$  system close to the one used by Walker (1979). In 1997 a monitoring programme of nearly 60 late spectral type semiregular and irregular variables was initiated. Typical light curves resulting from this programme can be found in Lebzelter (1999) and Kerschbaum et al. (2001). A complete sample of light curves will be published elsewhere (Lebzelter et al., in preparation). In Table 3 we present median *V*, *V-I<sub>C</sub>*, and an intercept *a*<sub>0</sub>

**Table 3.** APT photometry of selected red variables.

HIP	GCVS	<i>V</i>	<i>V-I<sub>C</sub></i>	<i>a</i> <sub>0</sub>	<i>a</i> <sub>1</sub>	<i>n</i>
4008	VY Cas	9.49	4.14	0.66	0.366	217
5914	Z Psc	6.85	2.54	-0.18	0.396	49
6191	AA Cas	8.24	3.47	0.00	0.422	206
10472	V Ari	8.52	2.07	-1.15	0.379	30
17821	BR Eri	7.15	3.16	-0.15	0.465	270
21046	RV Cam	8.16	3.81	0.38	0.420	326
22667	<i>o</i> <sup>1</sup> Ori	4.84	2.50	-0.10	0.536	83
32083	VW Gem	8.32	2.41	-0.86	0.391	36
33369	BG Mon	9.66	2.46	-1.40	0.400	35
41061	AC Pup	9.05	2.83	-1.42	0.474	360
41201	FK Hya	7.29	3.48	0.22	0.446	388
43063	EY Hya	9.60	4.49	1.01	0.366	85
44601	TT UMa	9.02	3.68	-0.17	0.427	425
44862	CW Cnc	8.70	4.03	0.90	0.360	67
56976	AK Leo	8.54	2.87	-1.37	0.497	68
57504	AZ UMa	8.50	3.97	0.57	0.400	440
59108	RW Vir	7.33	3.63	0.66	0.405	377
61022	BK Vir	7.81	4.24	2.13	0.268	98
61839	Y UMa	8.39	4.40	1.92	0.295	411
66562	V UMi	7.91	2.92	-0.95	0.488	78
69449	EV Vir	6.91	2.62	-1.05	0.533	223
70236	CI Boo	6.48	2.93	-0.63	0.549	182
70401	RX Boo	7.43	4.33	2.97	0.184	105
71644	RV Boo	8.24	4.06	1.30	0.333	190
73213	FY Lib	7.24	3.65	0.30	0.460	225
74982	FZ Lib	7.10	3.04	-1.00	0.570	367
78574	X Her	6.28	3.92	1.60	0.371	346
80259	RY CrB	9.63	4.02	0.24	0.393	255
80704	g Her	4.86	3.47	1.23	0.461	291
81188	TX Dra	7.26	2.96	-0.58	0.488	153
81747	AX Sco	8.73	4.00	-0.60	0.527	120
82249	AH Dra	7.54	3.52	0.00	0.465	301
84027	CX Her	9.86	4.04	1.85	0.225	33
84329	UW Her	7.97	3.42	-0.29	0.464	298
84346	V438 Oph	9.12	4.26	2.41	0.199	164
93989	V398 Lyr	7.39	3.30	-0.32	0.490	265
95173	T Sge	9.29	4.66	2.45	0.236	276
96919	V1351 Cyg	6.56	3.06	0.00	0.466	226
102440	U Del	6.77	3.61	0.88	0.402	299
103933	DY Vul	7.09	3.58	0.55	0.425	207
107516	EP Aqr	6.63	4.01	2.16	0.279	183
109070	SV Peg	8.67	4.47	0.18	0.490	69
110099	UW Peg	8.89	3.39	-0.82	0.473	207
112155	BD Peg	8.66	3.82	0.56	0.376	159
113173	GO Peg	7.37	2.66	-0.76	0.464	168

and slope *a*<sub>1</sub> from the fit *V-I* vs. *V* for 45 selected Hipparcos variables used in the following calibration (Sect. 3). The total number of observations *n* is indicated in the last column.

#### 2.4. Published sources of *VI* photometry

Only two large surveys of relatively bright red stars are available in the *VI<sub>C</sub>* system – a survey of the Southern carbon stars (Walker 1979) and the recent photometry of nearly 550 Hipparcos M stars (Koen et al. 2002). Additional literature on the *VI<sub>C</sub>* photometry of Hipparcos red stars is not rich, therefore we included some other sources containing Johnson *VI<sub>J</sub>*

photometry. We used normal color indices for M0 to M8 spectral type stars (Celis 1986, Table 4) to obtain the following relationship between the Johnson  $V-I_J$  and Cousins  $V-I_C$ :

$$V-I_C = -0.359 + 0.894(V-I)_J - 0.0087(V-I)_J^2, \quad (1)$$

defined for the giants of M spectral type. This is valid for zirconium (S-type) stars, and probably usable for carbon stars as well, throughout the  $V-I_J$  range from 1.9 to 8.7 mag. Note that this relationship yields a bluer color index, by  $\sim 0.1$ , than a similar relationship from Hipparcos Catalogue (ESA 1997, vol. 1). A list of all sources used in this paper to calibrate  $V-I$  photometry is given in Table 4. It contains the reference, the number of stars  $n$ , spectral type, photometric system, and remarks. This list is not complete since we deliberately left out a few sources for the further independent comparisons.

**Table 4.** Selected sources of  $VI$  photometry.

Source	$n$	Type	System	Remarks
Bagnulo et al. (1998)	1	C	Cousins	
Barnes (1973)	11	M	Johnson	narrow-band $I$
Celis (1982)	24	M	Kron(?)	$\sim$ Johnson $I$
Celis (1986)	20	M	Cousins	
Eggen (1972)	30	C	Eggen	$\sim$ Cousins $I$
de Laverny et al. (1997)	2	C	Cousins	
Kizla (1982)	36	C,M	Johnson	
Koen et al. (2002)	80	M	Cousins	only $V < 8.4$
Lee (1970)	43	M	Johnson	
Mendoza & Johnson (1965)	33	C	Johnson	
Olson & Richer (1975)	11	C	Johnson	
Percy et al. (2001)	16	C,M	Johnson	
Walker (1979)	119	C	Cousins	
Table 1	61	C	Cousins	this study
Table 2	42	C,M	Cousins	this study
Table 3	45	C,M	Cousins	this study

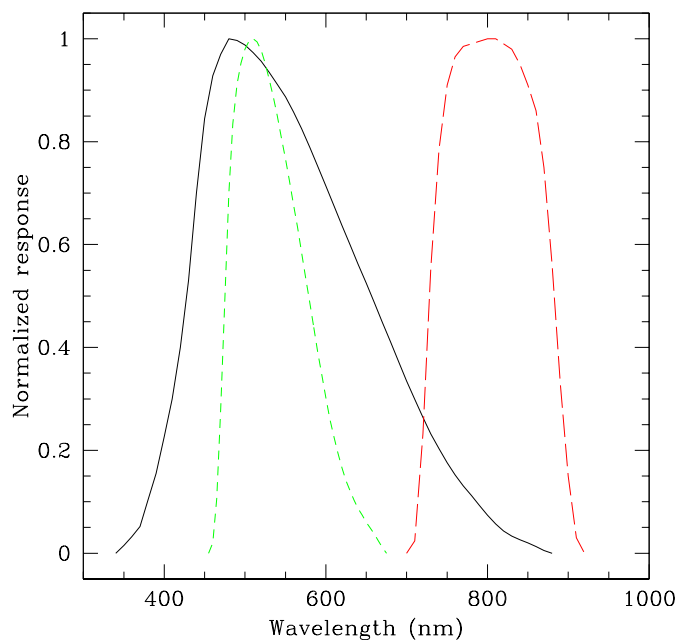
### 2.5. Radial velocities

Although radial velocities have no direct bearing on the photometry, they could be used to identify spectroscopic binaries and hence shed light on possible discrepancies in the photometry caused by duplicity. We selected 19 Hipparcos carbon stars, mostly R type. The radial velocity measurements were made with a Coravel-type spectrometer using the Steward Observatory 1.6 m Kuiper Telescope at Mt. Bigelow, Arizona in February, 2002. Additional measurements were also obtained with the Moletai Observatory 1.65 m telescope in Lithuania and the 1.5 m telescope of the Turkish National Observatory near Antalya. A detailed description of the spectrometer is given in Upgren et al. (2002). On average, the estimated precision of a single measurement is  $0.7 \text{ km s}^{-1}$ . A total of 61 measurements of radial velocity are given in Table 5, where columns 1–6 are Hipparcos number, carbon star number from Stephenson (1989), GCVS variable star name (Kholopov et al. 1985–1995), Julian date, heliocentric radial velocity and its estimated standard error, both in  $\text{km s}^{-1}$ . More details on the observing and reduction procedure can be found in

Upgren et al. (2002). By examining the ratio of external and internal error in accordance with Jasniewicz & Mayor (1988), it is evident that two stars in Table 5, HIP 53522 and 53832, are new SB1 spectroscopic binaries, although the time span is too short for the orbit determination. Both stars are suspected CH-like carbon stars (Hartwick & Cowley 1985), which adds more weight to the paradigm that most CH stars are binaries.

### 3. Deriving $V-I$ from Hipparcos $H_p$

The central idea of this study is to derive new sets of  $V-I$  color indices for red stars bypassing all various methods used in the original derivation of  $V-I$  (ESA 1997). We abandon the calibration methods based upon the ground-based  $B-V$  or Tycho  $B_T-V_T$  for two reasons. First, the  $B-V$  color index, at least for carbon stars, is a poor representative of effective temperature due to the severe blanketing effect by molecular bands (Alksne et al. 1991) in the  $BV$  bandpasses. Second, many Hipparcos red stars have such a large  $B-V$  color index that their measurements are uncertain or, in the case of Tycho magnitudes, missing due to extremely low fluxes in the  $B_T$  bandpass. In this sense the potential of Tycho  $B_TV_T$  photometry for red stars is limited. However, there is a color index,  $H_p - V_T$ , which to our knowledge, has been used neither in the Hipparcos reductions nor the following studies. The normalized  $H_p$  and  $V_T$  response curves provided by Bessell (2000) indicate only a 21 nm difference in the mean wavelength (see Fig. 2). This wavelength is calculated assuming a flat spectral energy distribution (SED) which is definitely not the case for late-type stars. If we account for the observed spectral energy distribution, e.g., from Gunn & Stryker (1983), then for an M7III spectral-type star (HIP 64569) the difference in the effective wavelengths of the two filters reaches 150 nm. The SEDs for the two carbon stars



**Fig. 2.** Normalized response curves for the Hipparcos  $H_p$  (solid line), Tycho  $V_T$  (short-dashed line), and Cousins  $I$  (long-dashed line) bandpasses. The corresponding curves are taken from Bessell (1990, 2000).

**Table 5.** Radial velocities of *R* and other selected carbon stars.

HIP	CGCS	GCVS	JD-2 450 000	$RV_{\text{hel}}$	$\sigma_{RV}$	HIP	CGCS	GCVS	JD-2 450 000	$RV_{\text{hel}}$	$\sigma_{RV}$
26927	1035	...	2327.617	42.5	0.6	53832	2919	...	2327.946	5.2	0.7
			2332.630	42.2	0.6				2332.843	3.4	0.6
29896	1222	GK Ori	2330.729	54.6	1.5				2363.492	-2.8	0.7
...	1226	V1393 Ori <sup>a</sup>	2332.641	34.2	0.6				2368.389	-3.1	0.7
29961	1230	V1394 Ori	2327.658	70.8	0.7				2382.344	-5.5	0.7
31829	1337	NY Gem	2327.732	-123.0	0.8				2386.347	-6.4	0.7
32187	1373	V738 Mon	2327.706	60.3	0.7				2399.392	-8.9	0.7
			2332.650	61.2	0.7				2403.329	-8.4	0.7
33369	1474	BG Mon	2327.752	71.4	0.7				2419.261	-11.5	0.7
			2333.745	71.6	0.7				2423.270	-12.1	0.7
			2350.255	71.4	0.7	58786	3156	...	2349.500	-21.3	0.7
34413	1565	W CMa	2330.686	18.9	0.6				2368.400	-21.4	0.7
			2333.737	19.6	0.6				2386.299	-21.2	0.7
35681	1622	RU Cam	2350.266	-24.4	0.6	62944	...	...	2327.992	8.5	0.6
			2356.253	-26.3	0.7				2332.853	6.5	0.6
			2375.335	-24.9	0.7				2363.504	6.7	0.6
38242	1891	...	2327.760	13.7	0.7				2368.416	6.2	0.6
			2332.664	15.7	0.7				2382.382	7.3	0.6
39118	1981	...	2327.772	95.5	0.7	63955	3335	...	2327.957	-9.2	0.7
			2332.670	96.2	0.7				2332.919	-10.1	0.6
44812	2428	...	2327.917	20.2	0.7	69089	...	...	2330.980	-20.3	0.6
			2350.314	20.1	0.8				2332.906	-20.3	0.7
			2375.300	20.7	0.7				2359.572	-21.4	0.6
50412	2715	...	2349.486	-84.8	0.7				2382.449	-20.2	0.6
			2386.284	-84.9	0.7				2399.479	-20.9	0.6
53354	2892	...	2330.801	4.7	0.7						
			2332.827	5.8	0.8						
53522	2900	...	2327.938	28.0	0.6						
			2369.333	31.5	0.7						
			2375.326	33.3	0.7						
			2382.336	34.9	0.7						
			2386.337	34.3	0.7						
			2399.377	36.3	0.7						
			2403.322	37.5	0.7						
			2419.255	37.5	0.7						
			2423.255	38.5	0.7						

<sup>a</sup> Not HIP 29899. See Table 8.

HIP 99 and 95777 yield an 84 and 94 nm difference in the effective wavelength, respectively. It is the extended red response of the S20 photocathode of Hipparcos main detector – Image Dissector Tube, which makes the  $H_p - V_T$  index fairly sensitive in the K–M spectral range (see ESA 1997, vol. 1, Fig. 1.3.4). We employ this property to calibrate  $V - I$  for late-type stars using  $H_p - V_T$ .

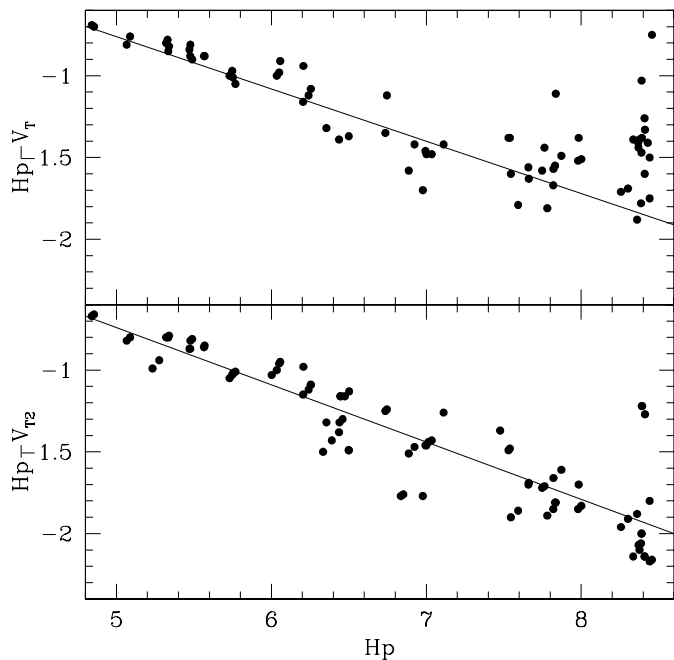
### 3.1. Tycho photometry

First trials using the published Tycho  $V_T$  photometry indicated two problems. First, a large fraction of red stars lack Tycho photometry. Second, the  $V_T$  photometry shows a progressively increasing bias at faint magnitudes ( $V_T > 9$ ). This effect is illustrated by Fig. 3 where  $H_p - V_T$  values are abnormally small at  $H_p > 8$ , equivalent to the “brightening” of  $V_T$  at these  $H_p$  magnitudes. It is suspected that the de-censoring technique (Halbwachs et al. 1997) has failed to completely correct the

faint-magnitude bias. Therefore, it was decided to make use of the Identified Counts Data Base, ICDB (Fabricius & Makarov 2000b) – a by-product of the Tycho-2 data re-processing (Høg et al. 2000).

All transits of about 2.5 million stars included in the Tycho-2 Catalogue are represented in the ICDB by sequences of 13 time-ordered photon counts, separately for the inclined and vertical slits, and the  $B_T$  and  $V_T$  bandpasses. Combined with some instrument calibration files, this data base is sufficient to reproduce a complete astrometric solution for any Tycho-2 star, including its possible binarity status, photometric variability, etc. In this paper, we exploit the possibility to extract epoch photometry for selected stars by estimating the signal at the pre-computed, mission-averaged astrometric position.

The working version of Tycho-2 epoch photometry was derived some time ago for a search of a particular kind of variable stars, although it has not been implemented in the



**Fig. 3.** Bias in the  $Hp - V_T$  at  $Hp > 8$  originating from original Tycho  $V_T$  magnitudes for a bright Mira T Cep = HIP 104451 (top panel). If the  $V_{T2}$  epoch photometry is used, the bias disappears (bottom panel). A straight line is fitted to the data in the bottom panel and then just overlotted in the top panel.

construction of the Tycho-2 Catalogue. It should be noted that, even though based on the same observational data, the Tycho-2 epoch photometry used here differs significantly from the published Tycho epoch photometry (ESA 1997). Nevertheless, the global calibrations of our current epoch photometry are consistent with the Tycho mission-average calibrations. On the star-by-star level, the Tycho-2 processing (both astrometric and photometric) is based on a single so-called Maximum Cross-Correlation estimator, while the original Tycho epoch photometry is the result of a series of successive linear and non-linear filterings (Halbwachs et al. 1997; ESA 1997, vol. 4). The main difference in the reduction procedure is that for a given star in Tycho-2, the determination of astrometric parameters was done over all collected transits at once; whereas in Tycho, a complete cycle of astrometric and photometric reductions was performed for each transit.

The latter method proved to be unreliable at a low signal-to-noise ratio, as the noise may mimic a signal from the star and produce a spurious astrometric detection and a subsequent false photometric estimate at the derived location. Such false detections tend to be abnormally bright, which then produce a bias in the faint magnitudes and hence necessitate the de-censuring analysis (Halbwachs et al. 1997) as the lesser of two evils.

The Tycho-2 epoch photometry is largely free of this de-censuring bias, since all photometric estimations are made at the correct location of a star image (within the astrometric precision), and all observations are retained. Still, Tycho-2 epoch photometry can only find restricted applications due to a

possibly high background and contamination from other stars which could be present in the 40'-long slits of the star mapper.

We will denote the re-processed Tycho photometry as  $V_{T2}$  to distinguish it from the original Tycho  $V_T$  epoch photometry.

### 3.2. Relationship $Hp - V_{T2}$ vs. $Hp$

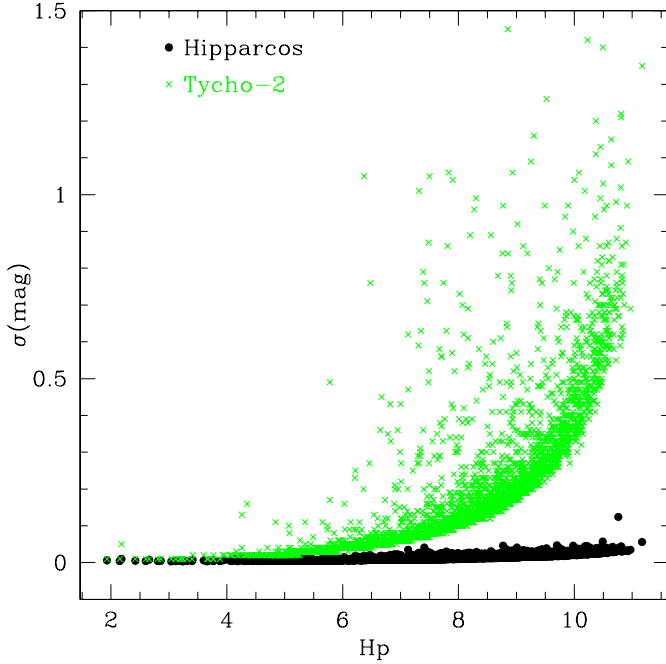
Due to the differences in spectral features, we kept the processing of carbon and oxygen- and zirconium-rich (M, S) stars separately. There are 321 carbon stars and 4464 stars of M and S spectral type, which have a pair of  $Hp$  and  $V_{T2}$  values. These stars were selected according to the listed spectral type in the Hipparcos Catalogue (field H76) but not fainter than  $Hp = 11$ . In the case of a missing spectral type, we included the stars having Hipparcos  $V - I > 1.5$ . Finally, the stars of K spectral-type were also considered if their  $V - I > 2$ . Note that for the Hipparcos photometry we used the so-called  $Hp_{dc}$  magnitude estimate derived from the unmodulated part of a signal intensity (ESA 1997), since the mean photometric parameters have been obtained from  $Hp_{dc}$ . In addition, the ground-based photoelectric photometry is always integrated over some aperture (usually with  $\varnothing = 15\text{--}30''$ ) centered onto the target and hence, the flux from any object within this aperture is going to be included. However, in Tycho-2 photometry, if the star was found to be a binary (minimum separation  $\sim 0''.4$ ), only the brightest component has been retained and subsequently used for this study. Because of that, the color index  $Hp - V_{T2}$  of resolved binaries could be biased to some degree and thus, should be considered with caution.

For each star, the color index  $Hp - V_{T2}$  was visually examined as a function of  $Hp$  ignoring the listed status flags. A pair of  $Hp, V_{T2}$  photometry was deleted if it deviated from the mean trend by more than  $3\sigma$ . As seen in Fig. 4 the precision of  $Hp - V_{T2}$  is driven by the precision of the  $V_{T2}$  photometry. A rapidly deteriorating error budget at  $Hp > 9$  actually poses a problem of reliability of calculated slopes in the  $Hp - V_{T2}$  vs.  $Hp$  plot. We opted for an interactive and iterative linear fit to find a slope, i.e., gradient  $\nabla_{HpV_T} = \Delta(Hp - V_{T2})/\Delta Hp$  and an intercept. It was decided to keep all datapoints unless any were clearly deviant or there was a peculiar trend usually due to very faint or corrupted  $V_{T2}$  epoch photometry. It should be noted that we were not able to find a perceptible difference in the color of variable stars observed at the same magnitude on the ascending or descending part of a lightcurve. In the case of a constant star or large uncertainties in the  $V_{T2}$  photometry, only the mean  $Hp - V_{T2}$  has been calculated. We note that  $Hp$  can be predicted for any  $V_{T2}$  via

$$Hp = \frac{b_0 + V_{T2}}{1 - b_1}, \quad (2)$$

where  $b_0$  is the intercept and  $b_1$  is the slope from a linear fit. This simple relationship is crucial in bridging the ground-based  $VI$  photometry and Hipparcos  $Hp$  photometry (see Sect. 3.3).

The calculated color gradients  $\nabla_{HpV_T}$  vs. the observed amplitude in  $Hp$  within the 5-to-95 percentile range,  $Hp_{95} - Hp_5$ , are shown in Fig. 5, separately for 136 carbon and 906 M and S stars. For both groups of stars, the color gradient ranges between  $-0.1$  and  $-0.45$ . For carbon stars, the mean gradient is

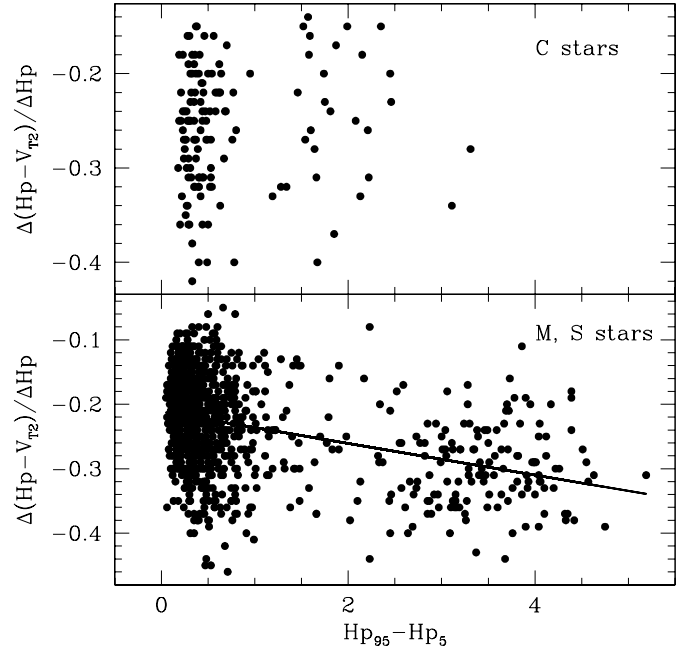


**Fig. 4.** The distribution of mean standard errors for red stars from  $Hp$  photometry (solid dots) and Tycho-2  $V_{T2}$  data (crosses) as a function of median  $Hp$  magnitude. The large scatter in the distribution of  $V_{T2}$  errors is due to the variability – observations of Miras generate the largest scatter. The lower envelope of the same error distribution reflects the contribution by photon noise.

$\langle \nabla_{HpV_T} \rangle = -0.24$ , whereas it is  $-0.26$  for the M and S stars. This indicates that on average the gradient  $\nabla_{HpV_T}$  is only marginally sensitive to the C/O ratio in the atmospheres of red stars. On the other hand, for M and S stars, the gradient is definitely correlated with the amplitude of a brightness variation in  $Hp$  – the color gradient increases at the rate  $-0.025$  per mag of amplitude. Similarly, the gradient is correlated with the median  $V-I$  for M and S stars: this merely reflects another correlation between the amplitude of brightness variation and median  $V-I$ .

### 3.3. $V-I$ calibration curves

We have not been able to find any ground-based  $V-I_C$  data for the red stars concurrent with the Hipparcos lifetime. To relate the ground-based  $V-I$  observations to Hipparcos/Tycho photometry we postulate that a star’s luminosity-color relation (encapsulated by parameters  $b_0$  and  $b_1$  in Eq. (2)) is constant over several decades and adopt the  $V_{T2}$  magnitude as a proxy to tie ground-based observations into the Hipparcos  $HpV_{T2}$  system. In practice, it involves two important steps. First, the ground based  $V$  magnitude should be transformed into the system of Tycho  $V_T$ . This is not trivial for red stars, therefore we provide step-by-step instructions explaining how to do that for carbon and M, S stars. Second, the derived  $V_{T2}$  magnitude now allows us to find the corresponding  $Hp$  value using Eq. (2) and thus, the color  $Hp - V_{T2}$ . Only then, it is possible to relate a ground-based measurement of  $V-I$  to the corresponding  $Hp - V_{T2}$  value and be reasonably certain that both measurements are on the same phase of a light curve in the case of variable stars.



**Fig. 5.** Calculated gradients  $\Delta(Hp - V_{T2})/\Delta Hp$  as a function of observed  $Hp$  amplitude within the 5-to-95 percentile range,  $Hp_{95} - Hp_5$ , for 136 carbon stars (top panel) and 906 M and S stars (bottom panel). For M and S stars, the gradient is correlated with the amplitude of the brightness variation as indicated by a linear fit.

As demonstrated by Kerschbaum et al. (2001), there is no phase shift between the variability in the  $V$  and  $I_C$  bandpasses for asymptotic giant branch stars, a dozen of which can also be found in Table 3. A small and consistent rms scatter of the residuals in the linear fits given in Table 3 for additional M stars and a few carbon stars, is another reassuring sign of the lack of a phase shift – a crucial assumption in the calibration procedure.

#### 3.3.1. Carbon stars

Many carbon stars are too faint in the  $B_T$  bandpass, hence their  $B_T - V_T$  color index is either unreliable or is not available at all. Therefore, we first derived a relationship between the ground-based  $(V-I)_C$  and  $(B-V)_J$  using the Walker (1979) data:

$$(B-V)_J = 1.59 - 0.942(V-I)_C + 0.5561(V-I)_C^2. \quad (3)$$

Then, the  $B_T - V_T$  can be easily estimated using Eq. (1.3.31) in ESA (1997), vol. 1:

$$(B_T - V_T) = 1.37(B-V)_J - 0.26. \quad (4)$$

Finally, knowing the ground-based  $V$ -magnitude and employing Eq. (1.3.34) in ESA (1997), vol. 1, we derive

$$V_{T2} = V_J - 0.007 + 0.024(B_T - V_T) + 0.023(B_T - V_T)^2, \quad (5)$$

which in combination with Eq. (2) yields the corresponding  $Hp - V_{T2}$ .

#### 3.3.2. M and S stars

Owing to some, albeit weak, dependence of TiO absorption upon the surface gravity, the stars of spectral type M can be

divided into giants and dwarfs (main sequence stars). All stars in our sample with Hipparcos parallaxes smaller than 10 mas are considered to be giants. For M giants,  $V_{T2}$  follows directly from Eq. (1.3.36) (see ESA 1997, vol. 1):

$$V_{T2} = V_J + 0.20 + 0.03(V-I - 2.15) + 0.011(V-I - 2.15)^2. \quad (6)$$

To calculate a similar relationship for M dwarfs, we used the data from Koen et al. (2002):

$$V_{T2} = V_J + 0.20 + 0.042(V-I - 2.15). \quad (7)$$

As expected, Eqs. (6) and (7) are very similar so that, considering the uncertainties involved, our  $V-I$  photometry is not sensitive to the surface gravity. Equation (6) or (7) in combination with Eq. (2) then yields  $Hp - V_{T2}$ .

### 3.3.3. Calibration curves

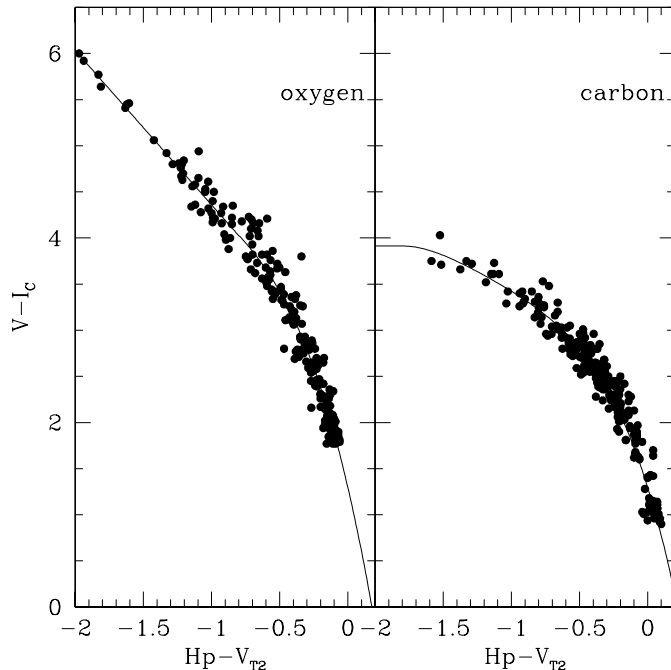
From the sources listed in Table 4, we have chosen 274 measurements of  $V-I$  for carbon stars and 252 for M and S stars. Quite often there is more than one  $V-I$  measurement for a given star. In the case of multi-epoch ground-based  $V-I$  data, we first obtained a linear fit to  $V-I$  as a function of  $V$  (e.g., Table 3). The coefficients of that fit were used to estimate the  $V-I$  index of variable stars at maximum brightness. The corresponding  $Hp - V_{T2}$  color index at maximum brightness has the advantage of being relatively insensitive to the uncertainties affecting the  $Hp - V_{T2}$  vs.  $Hp$  relation at its faint end (see Figs. 3 and 4). This is especially important at the blue end of the relationship between  $V-I$  and  $Hp - V_{T2}$  (corresponding to the maximum brightness in the case of variable stars) requires more care due to its steepness.

The calibration curves for oxygen (actually M and S) stars and carbon stars are presented in Fig. 6.

Since many calibrating stars are fainter than  $Hp = 8$ , the scatter is mainly along the  $Hp - V_{T2}$  axis (see also Fig. 4). The relationship between  $V-I_C$  and  $Hp - V_{T2}$  cannot be represented by a single polynomial, hence we provide segments of calibration curves along with a color interval of their validity (Table 6). Within this interval, a Hipparcos  $(V-I)_H$  is

$$(V-I)_H = \sum_{k=0}^4 c_k (Hp - V_{T2})^k. \quad (8)$$

To calculate an epoch  $(V-I)_H$ , one should use the epoch  $Hp$  photometry and obtain  $Hp - V_{T2} = b_0 + b_1 \times Hp$  (see Eq. (2)). Then, a polynomial transformation given by Eq. (8) and Table 6 leads directly to the desired  $(V-I)_H$  color index. However, there are numerous cases when it was not possible to determine a slope  $b_1$  in the  $Hp - V_{T2}$  vs.  $Hp$  plot, although the amplitude of  $Hp$  variations indicated a likely change in  $Hp - V_{T2}$  as well. Therefore, for all such stars with a light amplitude having the range between maximum and minimum luminosities,  $\Delta Hp > 0.15$  (see entries H50-H49, ESA 1997, vol. 1), we adopted the mean slope, i.e., the mean gradient given in Sect. 3.2. A difficulty then is to find a point in the  $Hp - V_{T2}$  vs.  $Hp$  plot, to which the mean slope can be applied in order to



**Fig. 6.** Color-color transformation for M and S stars (left panel) and carbon stars (right panel). The red end of this transformation ( $Hp - V_{T2} < -1.5$ ) for carbon stars is uncertain due to the lack of intrinsically very red Hipparcos calibrating carbon stars.

estimate an intercept  $b_0$ . The median of the 3–5 brightest values of  $Hp$  and the corresponding median  $Hp - V_{T2}$  color were adopted for such a “reference” point.

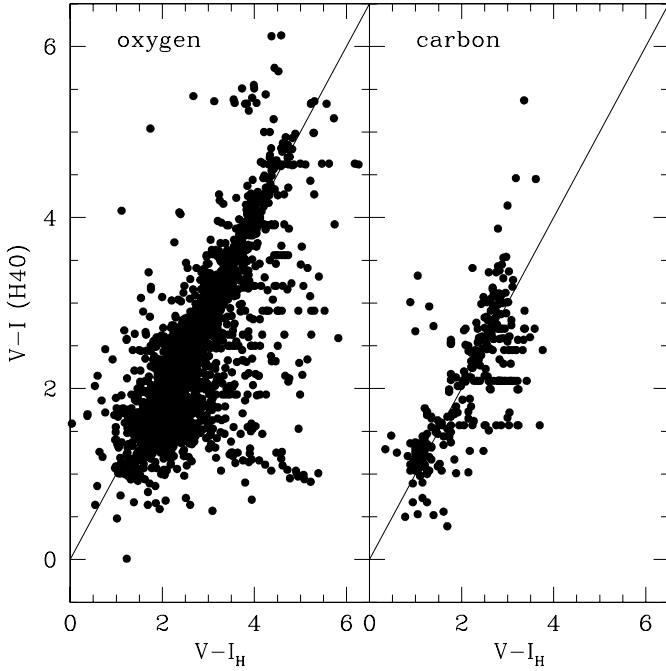
An important issue is to verify the system of our  $(V-I)_H$  photometry for red stars. The differences between the new median  $(V-I)_H$  and the best available Hipparcos  $V-I$  photometry (entry H40) are plotted in Fig. 7. On average the two systems are consistent. The very red carbon stars are an exception because their  $(V-I)_H$  color indices reach saturation, whereas the Hipparcos  $V-I$  index is not restrained. Then, there are numerous cases where the newly derived  $(V-I)_H$  values differ considerably from those in the Hipparcos Catalogue – in extreme cases up to 3–4 mag. A closer look at these cases indicates various reasons for such discrepancies. It could be duplicity, an incorrect target, severe extrapolation in color, etc. Noteworthy is the fact that the  $I_C$  bandpass given in ESA (1997) is  $\sim 30$  nm wider on the red side than the one published by Bessell (1979). Uncertainty in the location of the red-side cut-off of the  $I_C$ -bandpass owing to different detectors is known to be a major source of a small color-dependent bias ( $< 0.1$  mag) in the ground-based photometry of red stars.

### 3.3.4. Verification of the new $V-I$ color

From the variety of available sources, we have chosen the two largest sets of ground-based Cousins  $V-I$  data to test our  $(V-I)_H$  color indices; that is Koen et al. (2002) for M stars and Walker (1979) for carbon stars. We also selected the data of Lahulla (1987), which is an independent source of  $V-I$ , albeit in the system of Johnson  $VI$  which was not used in the calibration.

**Table 6.** Polynomial transformation from  $Hp - V_{T2}$  to  $V - I_C$ .

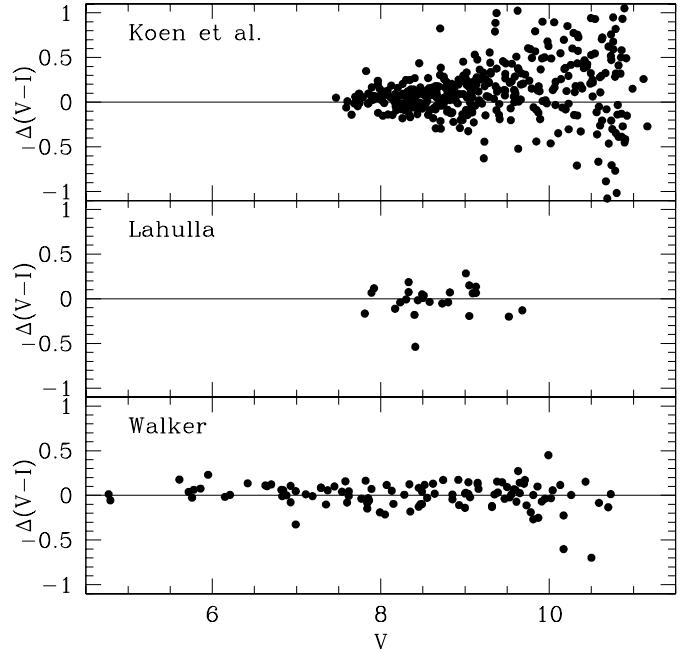
Spectral Type	Color Range	$c_0$	$c_1$	$c_2$	$c_3$	$c_4$
M, S	$-0.20 > Hp - V_{T2} \geq -0.80$	1.296	-6.362	-5.128	-1.8096	0.0
M, S	$-0.80 > Hp - V_{T2} \geq -2.50$	2.686	-1.673	0.0	0.0	0.0
C	$-0.20 > Hp - V_{T2} \geq -1.77$	1.297	-4.757	-4.587	-2.4904	-0.5343
C	$-1.77 > Hp - V_{T2} \geq -2.00$	3.913	0.0	0.0	0.0	0.0

**Fig. 7.** Hipparcos median  $V - I$  (ESA 1997, entry H40) vs. newly derived median  $(V - I)_H$  in this study. The reasons for some very large discrepancies are discussed in Sect. 4.1.

The differences,  $(V - I)_H - (V - I)_C$ , are plotted as a function of ground-based  $V$  (Fig. 8). For the Walker (1979) and Lahulla (1987) datasets, the mean offset  $\langle (V - I)_H - (V - I)_C \rangle$  is not more than +0.01 mag; the scatter of individual differences is 0.12 mag. The Koen et al. (2002) data are instrumental to test the reliability of  $(V - I)_H$  for early-type M stars, both dwarfs and giants. We note that at  $V - I \approx 2$  the calibration curve is very steep (left panel, Fig. 6). At this  $V - I$ , a variation in  $Hp - V_{T2}$  by only 0.01 mag corresponds to a 0.05 mag change in  $V - I$ . For relatively bright Hipparcos stars ( $V < 9$ ), the mean offset  $\langle (V - I)_H - (V - I)_C \rangle$  is +0.04 but it increases to +0.20 for fainter stars ( $9 < V < 11$ ). The scatter also rises from 0.13 to 0.40 in these two intervals. A noticeable bias in the mean  $(V - I)_H$  towards faint magnitudes might be an indication of some residual systematic error either in the Hipparcos  $Hp$  epoch photometry or in Tycho-2  $V_{T2}$  magnitudes. As expected, rapidly increasing errors in  $V_{T2}$  as a function of magnitude (Fig. 4) clearly set a limitation on the accuracy of  $(V - I)_H$ .

#### 4. New $V - I$ and some applications

We have calculated instantaneous (epoch)  $(V - I)_H$  color indices for 4414 M stars, 50 S stars from the list by

**Fig. 8.** Differences between our instantaneous  $(V - I)_H$  color index and those of Koen et al. (2002); Lahulla (1987); Walker (1979). The upper two panels represent M stars, whereas the bottom panel contains carbon stars. The accuracy of our calibrated  $V - I$  colors is clearly insufficient in the case of faint M dwarfs, which represent a large fraction of the Koen et al. (2002) sample.

van Eck et al. (1998), and 321 carbon stars, which include R, N, and Hd sub-types. A condensed version of this effort is presented in Table 7<sup>2</sup>, which contains HIP number, GCVS name for variable stars, median  $Hp$  magnitude (entry H44, ESA 1997, vol. 1), 5-to-95 percentile  $Hp$  range or the  $Hp$  “amplitude”, coefficients  $b_0, b_1$  (if  $b_1$  has not been determined, it is set equal to zero), median  $V - I$  from this study, spectral type (M, S, or C).

We note that about 2% of Hipparcos M, S, and C stars do not have adequate Tycho-2 photometry and, hence, are not given in Table 7. Those include some very bright stars and a number of faint stars. More than a dozen stars of intermediate brightness with  $8.0 > Hp > 5.0$  failed in the Tycho-2 photometry reductions due to poor astrometry, high background and/or a parasitic signal, which corrupted the signal from the target object.

<sup>2</sup> Table 7 is only available in electronic form at the CDS, via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsweb.u-strasbg.fr/cgi-bin/qcat?J/A+A/397/997>

#### 4.1. Remarks on individual carbon stars

We used the derived  $(V-I)_H$  color index and in some cases individual slopes from the  $Hp - V_{T2}$  vs.  $Hp$  plot to scrutinize the identity of some Hipparcos carbon stars. If an anonymous field star is measured instead of a real carbon star, it could yield a positive slope in the fit of  $Hp - V_{T2}$  vs.  $Hp$ . This is because the  $Hp$  measures have been overcorrected, using a  $V-I$  color index appropriate for an expected carbon star but not for the actual target. On the other hand, the Tycho-2  $V_{T2}$  photometry appears to be insensitive to the color a star really has. The net result is a very small or even positive slope. After identifying such cases, we checked the 2MASS Atlas Images for the true location of a carbon star in question. The offset in position is given in Table 8. If a carbon star has incorrect coordinates in Alksnis et al. (2001), it is coded by “GCGCS:” in Remarks. If an incorrect identification is already acknowledged in the Hipparcos Catalogue, it is indicated by the “HIP note” in Remarks. In the case of contradictory spectral classifications, we list only the alternative classification, since in nearly all such cases Hipparcos spectral type is “R...”. None of them can be found in Alksnis et al. (2001); therefore, the true identity of these stars has yet to be confirmed by spectroscopic means. An exception is HIP 94049 = CGCS 4179 which is a genuine carbon star (Houk, private communication; see also Table 1).

#### 4.2. Duplicity and $V-I$ color index

Perhaps, the star HIP 12086 = 15 Tri is a prototype of a very rare but characteristic Hipparcos problem due to the neglected poor input coordinates. The declination of HIP 12086 listed in the Hipparcos Input Catalogue (ESA 1992) is off by  $10''$ , hence in the detector’s instantaneous field of view (see ESA 1997, vol. 3, Fig. 5.2) the signal has apparently been affected by the sensitivity attenuation profile. This kind of bias is absent in the star mapper’s instrumentation. As a result, there is a very large positive slope in the  $Hp - V_{T2}$  vs.  $Hp$  plot. Not only is the  $Hp$  photometry clearly corrupted but the astrometry is also degraded as indicated by unusually large errors in the astrometric parameters. A similar effect of poor Hipparcos performance is known to be present, if the targets were wide binaries with separations in the range  $\sim 15''-20''$  (Fabricius & Makarov 2000a). Here we list such binaries among red stars when the epoch  $Hp$  photometry is clearly biased: HIP 7762, 13714 & 13716, 17750, 18465, 45343, 57473, 86961, 87820, 108943, 116191, 114994. We note that from this list the revised astrometry is already available for HIP 17750, 86961, 87820, 116191 (Fabricius & Makarov 2000a).

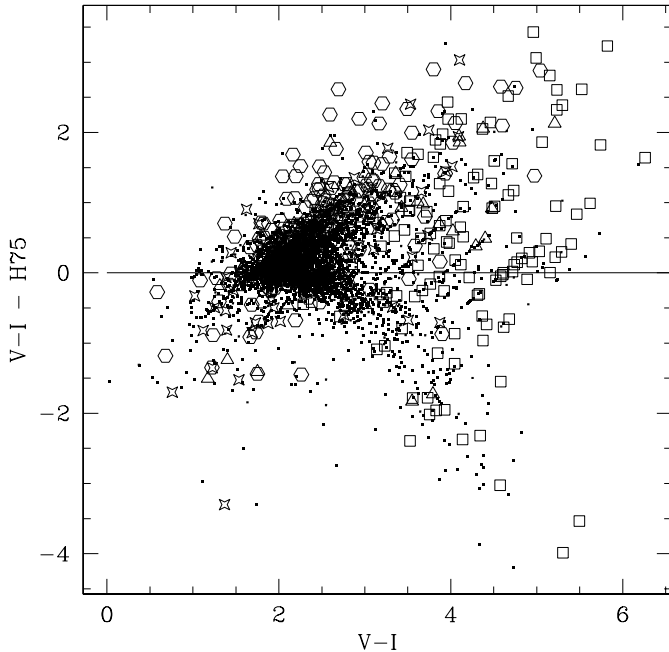
Strictly speaking the  $V-I$  index derived in this study for Hipparcos binary and multiple stars could be affected by the component(s) and, hence should be considered with caution. On the other hand, a peculiar  $V-I$  value may very well signal a genuine problem, be it of astrophysical or instrumental character. With this in mind, we examined the location of complex astrometric solutions in the plot given in Fig. 7. It turns out that certain areas, as seen in Fig. 9, are heavily populated by such cases. Why is it so? It is helpful to look at the relative fraction of DMSA C,G,V, and X solutions as a function of

**Table 8.** Upper part: erroneous Hipparcos pointings of carbon stars or a contradictory spectral classification with Hipparcos indicating “R...” spectral type. The offsets in coordinates,  $\Delta RA$  and  $\Delta Dec$ , are given in (s) and ( $''$ ), respectively, in the sense “true position-Hipparcos”. Lower part contains significant corrections “true position-GCGCS” required in Alksnis et al. (2001) to the positions of non-Hipparcos R stars from Table 1.

HIP	CGCS	$\Delta RA$	$\Delta Dec$	Remarks
4266				M0 (SAO)
14055				M0 (SAO)
21392				M0 (SAO)
22767	808	-21.0	+9	HIP note
24548	893	0.0	-242	
29564				M0 (SAO)
29899	1226	+3.4	+26	GCGCS:
35015	1615	+7.1	-146	GCGCS:
35119	1616	+0.3	+59	HIP note, GCGCS:
37022	1787	-2.6	+32	HIP note, GCGCS:
39337	2007	+16.7	+31	
40765				G1V (Houk & Swift 1999)
44235				not C-star? (Stephenson 1989)
75691	3614	+8.38	+94	GCGCS:
83404	3762	-0.4	-197	GCGCS:
85148	3820	-1.6	+58	GCGCS:
88170				M0 (SAO)
94049				C-star, not F5V
95024	4241	+5.3	+10	HIP note, GCGCS:
106599	5371	-7.7	+4	HIP note, GCGCS:
113840				M0 (SAO)
118252	5970	-2.3	-13	HIP note, GCGCS:
	258	-3.0	0	
	3765	-0.6	-42	
	3810	+10.3	+10	
	3813	+0.4	+9	
	3864	+0.3	-10	
	3939	+0.5	-2	
	3966	0.0	+25	
	4042	+0.8	-2	
	4168	+0.8	-14	
	4498	+3.7	-35	

differences between our median  $(V-I)_H$  and Hipparcos  $(V-I)_{H75}$ . Figure 10 shows that the relative fraction of supposedly complex systems, i.e., binary or multiple stars, is abnormally high for red stars. For  $\Delta(V-I) > 1$  and  $Hp < 10$  (see unshaded and hatched areas in Fig. 10), the relative fraction of such systems is 40% and higher as compared to only  $\sim 10\%$  among the stars having correct  $(V-I)_{H75}$  index (dark-shaded histogram).

Table 9 lists all red stars with  $(V-I)_H - (V-I)_{H75} > 2$ . As indicated from comparisons with an independent ground based  $V-I$  color index (see Col. 3 in Table 9), such differences are real. In essence, the stars listed in Table 9 have been processed with the  $(V-I)_{H75}$  color index off by more than 2 mag! Among such stars, the fraction of DMSA C,G,V, and X solutions – nearly 75% – is conspicuous in itself. For example, in the case of HIP 19488 and HIP 91703, it is evident that speckle interferometry could not confirm duplicity and, hence the Hipparcos DMSA/C solution must be spurious. This is nearly a watertight result since the limiting angular resolution of speckle

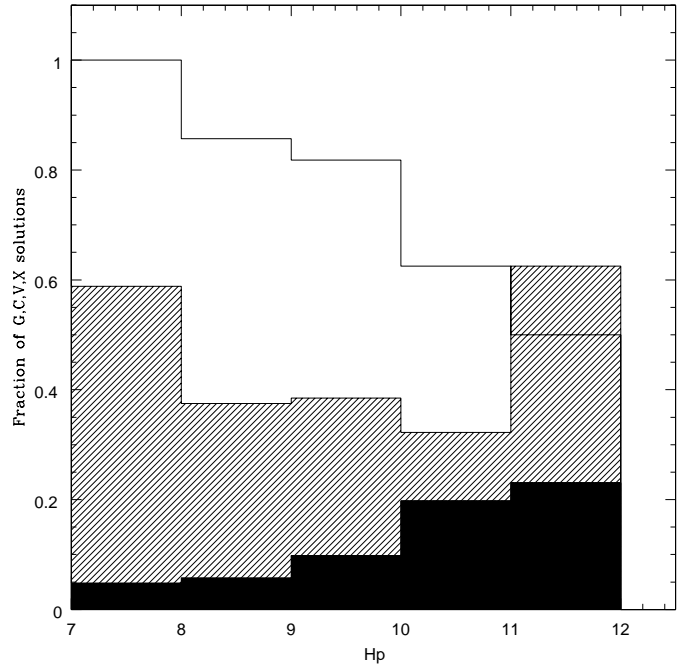


**Fig. 9.** Comparison of the  $V-I$  color indices used in the preparation of the Hipparcos Catalogue (H75) with those rederived from a color transformation based on  $H_p - V_{T2}$ . Only red stars with spectral types M and S are considered. Single-star solutions are depicted by black dots, whereas the open symbols denote more complex solutions (hexagons – component solutions C; triangles – acceleration solutions G; squares – Variability-Induced Mover (VIM) solutions V; stars – stochastic solutions X). It is worth noting that nearly all datapoints in the upper right corner of the diagram correspond to complex solutions, thus hinting at problems encountered in the Hipparcos data processing for these stars.

interferometry (Mason et al. 1999; Prieur et al. 2002) is 2–3 times higher than the separation given in the Hipparcos Catalogue. The other stars with a DMSA/C solution listed in Table 9 have not been observed so far under similar conditions nor are they listed in the Fourth Catalog of Interferometric Measurements of Binary Stars<sup>3</sup>, so that their possible spurious nature has yet to be established. Nevertheless, the high fraction of failed confirmations of binarity for Hipparcos stars with a DMSA/C solution (e.g., Mason et al. 1999, 2001; Prieur et al. 2002) is indicative that many such solutions might be spurious. We suspect that the phenomenon of such non-existent binaries among the red stars could very well be rooted in the improper chromaticity correction applied to these stars due to the poor knowledge of their true  $V-I$  color.

#### 4.3. Empirical effective temperatures of red stars

Due to very complex spectra the red stars are cumbersome objects for getting their effective temperature – one of the fundamental stellar parameters. From different vantage points this has been investigated, e.g., by Bessell et al. (1998), Bergalet et al. (2001), Houdashelt et al. (2000). Although the Cousins  $V-I$  color index may not be the optimal color to calibrate



**Fig. 10.** A histogram showing the fraction of red stars with a DMSA C, G, V or X solution in the Hipparcos Catalogue (field H59), as a function of  $H_p$  magnitude, for three different sets of  $\Delta(V-I) = (V-I)_H - (V-I)_{H75}$ , where  $(V-I)_H$  is the newly derived median color index and  $(V-I)_{H75}$  is Hipparcos median  $V-I$  (entry H75). The unshaded histogram shows the fraction of these DMSA solutions among the stars with  $\Delta(V-I) > 2$ ; hatched for  $2 \geq \Delta(V-I) > 1$ ; and dark-shaded for  $1 \geq \Delta(V-I) > -1$ . The fraction of G, C, V, and X solutions clearly correlates with  $\Delta(V-I)$ ; except for the faintest stars which always have a large fraction of G, C, V, X solutions.

effective temperature due to the strong influence by molecular absorption bands and possible reddening, nevertheless we attempted to derive an empirical calibration of effective temperatures for carbon and M giants. We used median  $(V-I)_H$  for Hipparcos stars having interferometric angular diameter measurements in  $K$  ( $\lambda = 2.2 \mu\text{m}$ ) bandpass (Dyck et al. 1996; van Belle et al. 1997, 1999) and corresponding effective temperature estimates. It is expected that the interstellar reddening is low for the chosen Hipparcos stars because of their relative proximity to the Sun. In total, from these sources of effective temperature determinations, we selected 27 small amplitude ( $\Delta H_p < 0.5$ ) M giants in the range  $3.6 > V-I > 1.5$  and 16 carbon stars ( $3.8 > V-I > 2.4$ ) with no restriction on variability. Similarly to Dumm & Schild (1998) we adopted a linear relationship

$$\log T_{\text{eff}} = d_0 + d_1(V-I). \quad (9)$$

For M giants, a least squares fit using Eq. (9) yields  $d_0 = 3.749 \pm 0.014$ ,  $d_1 = -0.087 \pm 0.007$ , and the standard error  $\sigma_T = 110$  K. For carbon stars the coefficients from the fit are:  $d_0 = 3.86 \pm 0.06$ ,  $d_1 = -0.153 \pm 0.021$ , and the standard error  $\sigma_T = 210$  K. Apparently, the effective temperature scale is not satisfactory for carbon stars in terms of its precision. The color mismatch between our median  $(V-I)_H$  and the color of a variable star at the time of interferometric observation can only partly explain the noted large scatter. Another

<sup>3</sup> <http://ad.usno.navy.mil/wds/int4.html>

**Table 9.** All M, S spectral type stars with  $\Delta(V-I)_H = (V-I)_H - (V-I)_{H75} > 2$  (Col. 2), where  $(V-I)_H$  is a color index from this study. When available,  $\Delta(V-I)_0 = (V-I)_H - (V-I)_{\text{obs}}$ , where  $(V-I)_{\text{obs}}$  is the ground-based photoelectric measurement. The stars are ordered by increasing amplitude of variability  $\Delta Hp$  (Col. 4). The column labelled DMSA provides a type of Hipparcos solution assuming more than one component. Angular separation between components,  $\rho$ , is given for DMSA/C solutions only.

HIP	$\Delta(V-I)_H$	$\Delta(V-I)_0$	$\Delta Hp$	$Hp$	DMSA	$\rho('')$	Remarks
19488	2.41		0.13	9.535	C	0.18	unresolved (Mason et al. 1999)
78501	2.19		0.14	10.285	C	0.17	
24661	2.31		0.15	10.170			
87221	2.61		0.19	8.763	C	0.17	
87433	2.27	-0.44	0.28	8.537			
76296	2.26		0.33	8.878	C	0.16	
42068	2.33	-0.49	0.41	8.511	C	0.18	
91703	2.65		0.46	8.799	C,V	0.21	unresolved (Prieur et al. 2002)
7762	2.03		0.48	8.615	X		companion star at 20''
84346	2.05		0.61	8.454	V		unresolved (Prieur et al. 2002)
100404	2.14	-0.76	0.61	8.464	V		unresolved (Mason et al. 2001)
37433	2.17		0.64	8.984			
56533	2.64		0.65	8.581	C	0.24	
84004	2.40		0.78	7.499	X		
80259	2.19		0.91	9.017	V		unresolved (Prieur et al. 2002)
16328	2.10		0.98	9.612	C	0.30	
90850	2.32		1.38	11.001			
78872	2.06	-0.47	1.70	9.841	G		
703	2.43	-0.59	2.09	11.112	V		
9767	2.19		2.10	9.773	V		
11093	2.52	0.16	2.10	9.756	V		
89886	3.27		2.26	10.883			
96031	2.29		2.64	10.512			
75393	3.06	0.32	2.73	8.554	V		
16647	3.23		2.87	10.376	V		
81026	2.66		2.89	11.538			
1901	2.61	1.27	2.97	10.705	V		unresolved (Prieur et al. 2002)
86836	3.43		3.15	11.196	V		
47066	2.61	0.87	3.49	10.073	V		
57642	2.32	0.78	3.60	9.968	V		
60106	2.04		3.81	9.854			
110451	2.01		3.90	11.460			
94706	2.81	0.67	3.97	10.826	V		T Sgr: composite spectrum
25412	2.39	0.29	4.00	9.974	V		
33824	2.02	0.97	4.05	9.922			

reason might include an unaccounted for circumstellar extinction, carbon abundance and metallicity effects on the color, and rather large errors in the effective temperature determination. The latter is discussed in detail by Dyck et al. (1996). An alternative scale of effective temperatures for carbon stars is given by Bergeat et al. (2001), although it may have the same kind of inherent problems. We note that the slope  $d_1$  for M giants is 2.5 times larger than in Dumm & Schild (1998). The main reason for that is a stretched color scale of Hipparcos  $V-I$  (see Fig. 7). It is felt that the empirical effective temperature scale based on  $V-I$  color has a limited use, in particular for carbon stars. Near infrared observations in  $JHKL$  bandpasses should be used to obtain better estimates of effective temperature for the coolest stars. With the advent of large optical interferometers the number of precise angular diameters for cool and red stars undoubtedly will increase substantially. However, an equal effort should be invested in deriving reliable

bolometric fluxes, which are equally important in establishing a precise scale of effective temperatures.

## 5. Summary and conclusions

The main result of this work is demonstrating the feasibility of the  $Hp - V_{T2}$  color index in studies of red stars. This color index is tightly correlated with the Cousins  $V-I$  color and, thus, allows us to derive an independent estimate of  $(V-I)_H$  for carbon, M and S stars. Such estimates are indispensable in the analysis of red variable stars, which have been little studied in the Cousins  $VI$  system.

We have shown that a considerable fraction of Hipparcos best estimates of  $V-I$  color index (entry H40, ESA 1997) for red stars might be in error by more than a full magnitude. Conspicuously, among the most discrepant cases we find an unusually large number of DMSA C, G, V, and X solutions

implicating a binary or multiple star status for these stars. On the other hand, extensive speckle interferometric observations have largely failed to confirm the binarity, despite the 2–3 times better angular resolution. This strongly suggests that some DMSA C, G, V, X solutions are not real and maybe due to the poor knowledge of the  $V-I$  color index, which served as a measure of star's color in both photometric and astrometric reductions by the Hipparcos consortia.

However, our attempts have not succeeded in improving the astrometry for single red stars. It was expected that an incomplete correction for the chromaticity effects should leave a color-related “jitter” in the abscissa data at the level of 1–3 mas due to incorrect  $V-I$ , used in accounting for these effects. Surprisingly, we were not able to find clear traces of residual chromaticity effects, for instance, in carbon star Hipparcos astrometry. Either they have been somehow accounted for in the original Hipparcos reductions or they are insignificant.

On the other hand, the re-analysis of so-called Variability-Induced Movers (VIM) has benefited substantially from the new set of  $(V-I)_H$  color indices. As indicated in Sect. 4.2, some of the DMSA/V solutions are suspected to be not warranted. Much finer analysis of all DMSA/V solutions for red stars (Pourbaix et al. 2002) provides strong evidence that nearly half of DMSA/V solutions are not justified, mainly thanks to reliable  $V-I$  colors now available at all phases of lightcurve for long-period variables such as Miras. This knowledge of  $V-I$  colors could be useful to further investigate other difficult systems having an extreme and changing color in combination with hints of duplicity, which can be resolved with interferometric means.

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