

Dust and molecular shells in asymptotic giant branch stars^{★,★★,★★★}

Mid-infrared interferometric observations of R Aquilae, R Aquarii, R Hydrae, W Hydrae, and V Hydrae

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ABSTRACT

Context. Asymptotic giant branch (AGB) stars are one of the largest distributors of dust into the interstellar medium. However, the wind formation mechanism and dust condensation sequence leading to the observed high mass-loss rates have not yet been constrained well observationally, in particular for oxygen-rich AGB stars.

Aims. The immediate objective in this work is to identify molecules and dust species which are present in the layers above the photosphere, and which have emission and absorption features in the mid-infrared (IR), causing the diameter to vary across the *N*-band, and are potentially relevant for the wind formation.

Methods. Mid-IR (8–13 μm) interferometric data of four oxygen-rich AGB stars (R Aql, R Aqr, R Hya, and W Hya) and one carbon-rich AGB star (V Hya) were obtained with MIDI/VLTI between April 2007 and September 2009. The spectrally dispersed visibility data are analyzed by fitting a circular fully limb-darkened disk (FDD).

Results. The FDD diameter as function of wavelength is similar for all oxygen-rich stars. The apparent size is almost constant between 8 and 10 μm and gradually increases at wavelengths longer than 10 μm . The apparent FDD diameter in the carbon-rich star V Hya essentially decreases from 8 to 12 μm . The FDD diameters are about 2.2 times larger than the photospheric diameters estimated from *K*-band observations found in the literature. The silicate dust shells of R Aql, R Hya and W Hya are located fairly far away from the star, while the silicate dust shell of R Aqr and the amorphous carbon (AMC) and SiC dust shell of V Hya are found to be closer to the star at around 8 photospheric radii. Phase-to-phase variations of the diameters of the oxygen-rich stars could be measured and are on the order of 15% but with large uncertainties.

Conclusions. From a comparison of the diameter trend with the trends in RR Sco and S Ori it can be concluded that in oxygen-rich stars the overall larger diameter originates from a warm molecular layer of H₂O, and the gradual increase longward of 10 μm can be most likely attributed to the contribution of a close Al₂O₃ dust shell. The chromatic trend of the Gaussian FWHM in V Hya can be explained with the presence of AMC and SiC dust. The observations suggest that the formation of amorphous Al₂O₃ in oxygen-rich stars occurs mainly around or after visual minimum. However, no firm conclusions can be drawn concerning the mass-loss mechanism. Future modeling with hydrostatic and self-consistent dynamical stellar atmospheric models will be required for a more certain understanding.

Key words. stars: AGB and post-AGB – circumstellar matter – infrared: stars – stars: mass-loss

1. Introduction

Asymptotic giant branch (AGB) stars are among the most important distributors of dust into the interstellar medium due to their high mass-loss rates in combination with an effective dust

condensation. Especially, the dust plays a crucial role for the formation and acceleration of the dense wind. By providing the seed particles for interstellar grains, AGB stars contribute to the chemical evolution of the interstellar medium (ISM) and facilitate further star and planet formation. Progress in the theoretical understanding has been made (Höfner et al. 2003; Woitke 2006a; Höfner 2008; Norris et al. 2012), but the wind formation mechanism and dust condensation sequence in oxygen-rich AGB stars need further observational constraints. Also for low mass-loss carbon-rich objects the wind formation has not been fully understood (Mattsson & Höfner 2011; Sacuto et al. 2011).

The slow wind of AGB stars is driven by stellar pulsation in combination with radiation pressure on dust. In order to support this current understanding, the location and compo-

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** Color versions of the figures and Appendices A–C are available in electronic form at <http://www.aanda.org>

*** FITS files of the calibrated visibilities are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/545/A56>

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sition of newly formed dust as function of the pulsation cycle, mass-loss rate and underlying chemistry are investigated. The size of the inner region free of dust is one of the parameters best constrained from mid-IR interferometric observations. This quantity is fundamental for understanding the condition of dust formation.

The low surface gravity and the stellar pulsation lead to an increased scale height of the atmosphere and make it possible to provide the conditions for dust grain formation. The consequence of a very extended atmosphere is a not clearly definable and measurable photospheric radius R_{phot} ¹ (e.g. [Mennesson et al. 2002](#); [Tej et al. 2003](#); [Ohnaka 2004](#); [Woodruff et al. 2004](#); [Fedele et al. 2005](#)) and observations at different wavelengths probe different atmospheric layers ([Baschek et al. 1991](#); [Scholz 2001](#)). The measured apparent diameters are correlated to the absorption and emission features of the most abundant and radiatively important molecular species (e.g. [Hofmann et al. 1998](#); [Jacob et al. 2000](#), and references therein) as well as first dust grain species with high sublimation temperatures (e.g. [Lorenz-Martins & Pompeia 2000](#); [Verhoelst et al. 2009](#)).

The immediate objective in this work is to identify molecules and dust which are present in close layers above the photosphere (at around $2 R_{\text{phot}}$), and which have absorption features in the mid-IR, causing the diameter to vary across the N -band. Candidates in O-rich environments are H_2O , SiO , CO , and TiO molecules, and dust grains composed of Mg_2SiO_4 , MgSiO_3 , SiO_2 , Al_2O_3 , and TiO_2 (e.g. [Woitke 2006a](#)). In C-rich stars, molecular layers of C_2H_2 and HCN , and dust composed of SiC and amorphous carbon (AMC) can be expected.

The size of the photosphere, close molecular and dust layers are constrained by a broad sampling of the visibility in the first lobe, i.e. by carrying out observations over a large projected baseline range. Visibility points at the shortest baselines are used to measure the contribution of surrounding dust in the more extended circumstellar environment. Observations were conducted at several orientations to establish whether the sources are elongated or not.

From infrared spectroscopy, it is already known that there is no simple relation between the spatial distribution of different molecules and pulsation phase (e.g. [Woodruff et al. 2009](#), and references therein). By monitoring the stars regularly over a few pulsation cycles the dynamic behavior is studied, in particular the variation in the distribution of the close warm layers of dust and molecules.

One star in this study (W Hya) was already extensively described in [Zhao-Geisler et al. \(2011\)](#), thereafter Paper I) and is included here only for completeness. In addition, some content refers to Paper I. Section 2 gives an overview of the target stars, and Sect. 3 describes the observation and data reduction. This is followed by Sect. 4 showing the light curves, spectra and results of the visibility modeling. The data are interpreted and discussed in Sect. 5 including an investigation of the dynamic properties and morphology. A summary is given in Sect. 6.

2. Target properties

The observations concentrated on a relative small number of stars to obtain a fair number of visibility points to sample the uv-plane as well as the pulsation phase. In total five stars, namely R Aql, R Aqr, R Hya, W Hya, and V Hya, were observed in the framework of a Guaranteed Time Observation (GTO) program (cf. Sect. 3.1). The targets were chosen to cover different

chemistries, evolution stages and mass-loss rates. R Aql, R Aqr, R Hya, and W Hya are oxygen-rich AGB stars, with R Aqr being a symbiotic system, while V Hya is an evolved carbon-rich AGB star with a fast collimated wind.

In the following, important theoretical and observational work from previous publications are summarized for each star giving an overview of their characteristic properties. Table 1 lists some of the relevant phenomenological features for each star. The given K band diameter, but also other optical and IR interferometric angular diameter measurements, are discussed in Sect. 4.4. The distances given in Table 1 are assumed throughout this paper.

2.1. R Aquilae

The visual period of the Mira R Aql has declined quite dramatically with an average rate of approximately 0.4 days per cycle since 1900 ([Greaves 1998](#); [Greaves & Howarth 2000](#)). While in 1915 the period was about 320 days, it declined to about 264 days in 2010. This has been accompanied by a decrease in amplitude of about 1 mag ([Bedding et al. 2000](#)). The shrinking of the period is attributed to a recent thermal pulse ([Wood & Zarro 1981](#)). R Aql is listed in the Washington Visual Double Star Catalog (WDS [Mason et al. 2001](#)) as triple system. However, the two companion stars have dissimilar proper motions and are probably only optical companions ([Greaves & Howarth 2000](#)).

The distance to R Aql is relatively well known. The Hipparcos catalog ([Perryman & ESA 1997b](#)) gives a value of 211^{+71}_{-42} pc, while [Kamohara et al. \(2010\)](#) estimated the distance to 214^{+45}_{-32} pc via maser observations. The mass and luminosity, obtained from modeling and observations, are $1 M_{\odot}$ and $3470 L_{\odot}$, respectively ([Hofmann et al. 2000](#)). Pulsation phase dependent effective temperature determinations range from (2550 ± 150) K ([Haniff et al. 1995](#)), over 3072 ± 161 K ([Hofmann et al. 2000](#)) to 3198 ± 147 K ([van Belle et al. 1996](#)). From the relations between pulsation period, mass and linear radius, [Hofmann et al. \(2000\)](#) came to the result that R Aql is a fundamental mode pulsator in agreement with recent considerations.

SiO , H_2O and OH maser emissions have been monitored for this O-rich star. SiO maser emission was reported by [Benson et al. \(1990\)](#), [Pardo et al. \(2004\)](#) and [Cotton et al. \(2010\)](#). The latter author derived for the 43.1 and 42.8 GHz emission average ring diameters of (26.1 ± 1.5) mas and (22.3 ± 1.9) mas, respectively, in agreement with the supposed extended atmosphere. At a larger diameter of around 330 mas, [Lane et al. \(1987\)](#) and [Brand et al. \(1994\)](#) detected H_2O maser emission. Studies of OH masers were performed by [Bowers et al. \(1989\)](#), [Etoka & Le Squeren \(2000\)](#) and [He et al. \(2005\)](#), showing that this maser emission originates in a region with a diameter between 2000 and 3000 mas.

[Matsuura et al. \(2002\)](#) modeled the extended molecular spheres of R Aql with two layers of water vapor of different temperatures. The radius of the hot layer changes from 1 to 2 photospheric radii between visual minima and maxima. The model could explain the emission and absorption features seen in the near infrared ($2.5\text{--}4.0 \mu\text{m}$). While [Cotton et al. \(2010\)](#) could not identify strong asymmetries in the SiO maser distribution, [Lane et al. \(1987\)](#) and [Bowers et al. \(1989\)](#) saw highly elongated and complex structures in the H_2O (NW-SE oriented) and OH masers (NE-SW oriented), respectively. In addition, the interferometric measurements by [Ragland et al. \(2006\)](#) gave a

¹ The definition of $R_{\text{phot}} = \theta_{\text{phot}}/2$ used in this work is given in Sect. 4.4.

Table 1. Target properties and phenomenology.

Target name:	R Aql	R Aqr	R Hya	W Hya	V Hya
	HIP 93820	HIP 117054	HIP 65835	HIP 67419	HIP 53085
Associated calibrator ^a :	η Sgr, ϵ Peg	30 Psc	2 Cen	2 Cen	α Hya
Type:	Mira	Mira	Mira	Mira/SRa	SRa/L
Chemistry:	O-rich	O-rich	O-rich	O-rich	C-rich
Mass ^b (M_{\odot}):	1.0	1.5	2.0	1.0	1.0
Distance ^c (pc):	214^{+45}_{-32}	250 ± 50	130 ± 25	98^{+30}_{-18}	360 ± 70
12 μm flux ^d (Jy):	402 ± 36	1580 ± 60	1590 ± 80	4200 ± 210	1110 ± 60
Spectral classification ^e :	M7 III e var	M7 III pev	M7 III e g	M7 III e g	N; C7, 5e
Effective temperature ^b (K):	3000 ± 300	2800 ± 300	2700 ± 300	2500 ± 300	2650 ± 300
Luminosity ^b (L_{\odot}):	3470 ± 500	5000 ± 500	$11\,600 \pm 1000$	5400 ± 500	7850 ± 500
K-band diameter ^f (mas):	11.5 ± 1.4	16.6 ± 3.0	24.5 ± 1.2	42.8 ± 3.2	14.5 ± 0.3
Mass-loss rate ^g ($10^{-7} M_{\odot} \text{yr}^{-1}$):	6–35	0.1–9	0.1–2	0.8–5	10–600
Multiplicity ^b :	triple system	SB	wide binary	wide binary	wide binary
Evolutionary stage ^b :	TP-AGB	TP-AGB	TP-AGB	early-AGB	post-AGB
Jets/fast wind ^b :	no	yes	no	no	yes
Asymmetry ^b :	maybe	yes	no	yes	yes
Maser ^b :	SiO, H ₂ O, OH	SiO, H ₂ O, OH	SiO, H ₂ O, OH	SiO, H ₂ O, OH	CO?
Period ^b :	decreasing	stable	decreasing	stable	two periods
Others ^b :	recent He flash	symbiotic system (Mira+WD)	detached shell, recent He flash	–	common envelope, rapid rotator

Notes. ^(a) For calibrator properties see Sect. 3.1 and Table 3. ^(b) See text for references, errors are approximations derived from the values found in the literature. ^(c) For R Aqr, R Hya and V Hya derived from the period-luminosity relation (cf. Whitelock et al. 2008), and for R Aql and W Hya obtained from maser measurements (Kamohara et al. 2010; Vlemmings et al. 2003, respectively). ^(d) IRAS flux (Neugebauer et al. 1984). ^(e) SIMBAD. ^(f) Values are averages from the literature (cf. Sect. 4.4). ^(g) Range of current mass-loss rates as given in Sect. 2. For W Hya see e.g. De Beck et al. (2010), Muller et al. (2008) and Justanont et al. (2005).

significantly non-zero closure phase, indicating an asymmetry as well.

Total mass-loss rates were estimated to $8 \times 10^{-7} M_{\odot} \text{yr}^{-1}$ and $5.6 \times 10^{-7} M_{\odot} \text{yr}^{-1}$ by Gehrz & Woolf (1971) and Hagen (1982), respectively, whereas Knapp & Morris (1985) found a much higher value of $3.5 \times 10^{-6} M_{\odot} \text{yr}^{-1}$. The dust mass-loss rate was derived by Hagen (1982) with a value of $6 \times 10^{-8} M_{\odot} \text{yr}^{-1}$. Wind velocities are measured in a range from 7 to 10 km s^{-1} (Bowers et al. 1989, and references therein).

2.2. R Aquarii

R Aqr is the closest known symbiotic binary at a distance of about 250 pc (derived from the period-luminosity relation by Whitelock et al. 2008). This D-type (dusty) symbiotic system consists of a 1.0–2.0 M_{\odot} Mira variable and a 0.6–1.0 M_{\odot} white dwarf (WD) (Hollis et al. 1997; Boboltz et al. 1997; Tatebe et al. 2006; Gromadzki & Mikołajewska 2009) that accretes matter through a disk (e.g. Hollis et al. 2000). The R Aqr binary system was for the first time resolved in the continuum radio emission at 7 mm by Hollis et al. (1997). Hollis et al. (1997) and Gromadzki & Mikołajewska (2009) derived orbital solutions with a period of about 44 years, while McIntosh & Rustan (2007) estimated the orbit period to be 34.6 years. The fitted semi-major axis is in all cases on the order of 15 AU (60 mas), meaning that even during periastron passage, the Mira variable remains relatively far from filling the Roche lobe (Gromadzki & Mikołajewska 2009).

The binary system hosts a compact HII region within a filamentary oval nebula of 30 arcsec size (e.g. Kafatos et al. 1986). It is surrounded by a large and expanding hour-glass shaped nebula with an extension of at least 120 arcsec (Wallerstein &

Greenstein 1980; Hollis et al. 1985; Henney & Dyson 1992; Corradi et al. 1999). The accretion disk, formed around the compact component, gives rise to prominent jets, detected across all spectral domains (cf. e.g. Kellogg et al. 2007; Nichols & Slavin 2009; Hollis et al. 1991; Paresce & Hack 1994; Hollis et al. 1985). The symmetric jets, oriented along a NE-SW axis, extend up to 2500 AU (10 arcsec) and have expansion velocities of 90 to 200 km s^{-1} .

The current mass-loss rate of this star is rather low, but uncertainties are very high due to difficulties in obtaining reliable gas-to-dust ratios. Rate estimates range from $1.3 \times 10^{-8} M_{\odot} \text{yr}^{-1}$ (Henney & Dyson 1992) and $6 \times 10^{-8} M_{\odot} \text{yr}^{-1}$ (Matthews & Reid 2007) to $3 \times 10^{-7} M_{\odot} \text{yr}^{-1}$ (Mennesson et al. 2002) and $8.9 \times 10^{-7} M_{\odot} \text{yr}^{-1}$ (Danchi et al. 1994). In most calculations an effective temperature of 2800 K (Burgarella et al. 1992; Matthews & Reid 2007) and a luminosity of 5000 L_{\odot} (Ragland et al. 2008) were assumed.

The O-rich Mira variable R Aqr is one of only three among 48 symbiotic Miras that exhibits H₂O masers (Iverson et al. 1994, 1998; Whitelock et al. 2003). A complementary study of SiO masers showed strong emission at 42.8 and 43.1 GHz. SiO maser ring diameters were obtained by Boboltz et al. (1997), Hollis et al. (2001) and Cotton et al. (2004, 2006), with relatively consistent values between 30 and 33 mas and errors on the order of 1.5 mas. This corresponds to a radius of 1.9 photospheric radii. OH maser and CO thermal lines are very weak and only tentative detections have been published by Iverson et al. (1998) and Groenewegen et al. (1999), respectively. In the most popular model, UV radiation and a fast wind from the companion remove the outer envelope of dusty molecular gas, where an OH maser or a thermal CO line could originate (Iverson et al. 1998).

Ragland et al. (2008) modeled the star with a three-component model, consisting of a symmetric central star sur-

rounded by a water vapor shell with a radius of about 2.25 photospheric radii, and an off-axis compact feature at about 2 photospheric radii at a position angle of 131° . They concluded that the observations are best explained with a clumpy, extended H_2O circumstellar envelope. In this model the SiO masers appear at the outer edge of the molecular envelope, as reported for other Mira stars.

Possibly caused by interactions with the close companion, asymmetries could be identified in the close environment around R Aqr. Ragland et al. (2006, 2008) found non-zero closure phases, and Hollis et al. (2001) and Cotton et al. (2004, 2006) detected an asymmetric distribution of the SiO maser emission with position angles between 150° and 180° . Terminal wind velocity measurements are rare. Kotnik-Karuza et al. (2007) obtained a value of $6\text{--}7\text{ km s}^{-1}$, while Dougherty et al. (1995) assumed $10\text{--}30\text{ km s}^{-1}$.

2.3. R Hydrae

The O-rich variable star R Hya is well known for its declining period (Wood & Zarro 1981; Zijlstra et al. 2002) and the presence of a detached shell. In the past few centuries, the period of R Hya has declined by over a hundred days and has remained constant since 1950 (Zijlstra et al. 2002). The steady decrease in the period can be possibly attributed to a recent thermal pulse (Wood & Zarro 1981; Zijlstra et al. 2002). In the post thermal-pulse evolution the decline in luminosity causes a reduction in stellar radius, which in turn, causes the period to become shorter.

The detached shell observed around R Hya (Young et al. 1993; Hashimoto et al. 1998) indicates a change in the mass-loss rate some 220 years ago. The shell is located about 1.9 arcsec from the star ($\approx 250\text{ AU}$). While the mass-loss rate before 1770 is estimated to be between $1.5 \times 10^{-7}\text{ M}_\odot\text{ yr}^{-1}$ and $3 \times 10^{-7}\text{ M}_\odot\text{ yr}^{-1}$ (Hashimoto et al. 1998; Zijlstra et al. 2002), the present day mass-loss rate is a factor of ≈ 20 lower and between $1 \times 10^{-8}\text{ M}_\odot\text{ yr}^{-1}$ and $4 \times 10^{-8}\text{ M}_\odot\text{ yr}^{-1}$ (Decin et al. 2008; Teyssier et al. 2006, respectively). De Beck et al. (2010) gives an average mass-loss rate of $1.6 \times 10^{-7}\text{ M}_\odot\text{ yr}^{-1}$.

This derived mass-loss history nicely agrees with the period decline analyzed by Zijlstra et al. (2002). Even the stellar evolution tracks calculated by Vassiliadis & Wood (1993) confirmed that mass-loss fluctuations during the thermal pulse cycle can lead to detached circumstellar shells. An apparent large detached shell may also arise from the interaction of the AGB wind with the ISM. Ueta et al. (2006) and Wareing et al. (2006) detected a far-IR nebula at a distance of about 100 arcsec to the west. This is explained by a slowing-down of the stellar wind by surrounding matter. Therefore, no extra mass-loss modulation at around 100 arcsec, i.e. around 10 000 years ago, needs to be invoked (Decin et al. 2008).

Distance estimations for R Hya range from $(110 \pm 21)\text{ pc}$ (Jura & Kleinmann 1992) to 165 pc (Zijlstra et al. 2002), while the period-luminosity relation gives an intermediate value of 130 pc (Whitelock et al. 2008). The mass and luminosity, inferred from modeling and observations, are 2 M_\odot and $11\,600\text{ L}_\odot$, respectively (Zijlstra et al. 2002). Effective temperature determinations range from 2600 K (Teyssier et al. 2006), over $2680 \pm 70\text{ K}$ (Haniff et al. 1995) to 2830 K (Zijlstra et al. 2002). R Hya is believed to be a wide binary system with a very long orbital period. The angular separation is 21 arcsec (WDS).

The wind in the inner CSE starts with a velocity of 1.5 km s^{-1} and accelerates to 6.5 km s^{-1} farther out, as modeled by Teyssier et al. (2006), before reaching a terminal velocity of 7.5 km s^{-1}

(Justtanont et al. 1998) to 10.0 km s^{-1} (Hashimoto et al. 1998; Knapp et al. 1998). Justtanont et al. (1998) found that a $13\text{ }\mu\text{m}$ dust feature and the appearance of strong emission lines of CO_2 originate in a warm layer close to the star. R Hya exhibits maser emission of SiO (Humphreys et al. 1997), H_2O (Takaba et al. 2001) and OH (Lewis et al. 1995). The resolution of these observations were too low to derive any spatial information. Thus, asymmetries were not studied with masers. A morphology study in the visual ($0.7\text{--}1.0\text{ }\mu\text{m}$, Ireland et al. 2004a) and K -band (Monnier et al. 2004) gave no indications of a departure from symmetry.

2.4. W Hydrae

The main characteristics of the O-rich star W Hya were extensively described in Paper I, but are summarized in Table 1.

2.5. V Hydrae

V Hya is a classical (N type) carbon star (Zuckerman et al. 1977) and is believed to be in a short-lived but critical stage in the evolution of a mass-losing AGB star into a bipolar PN (Tsuji et al. 1988; Kahane et al. 1996). This dust-enshrouded star has a C/O ratio of 1.05 and an effective temperature of about 2650 K (Lambert et al. 1986). The luminosity is estimated to be 7850 L_\odot (Knapp et al. 1997). Distance calculations range from 340 pc (Barnbaum et al. 1995) and 380 pc (Knapp et al. 1997) to 440 pc (Olivier et al. 2001) and 550 pc (Bergeat et al. 1998), while the period-luminosity relation (Whitelock et al. 2008) gives a value at the lower end with 360 pc .

V Hya has two variability periods, $(529.4 \pm 30)\text{ d}$ with a peak-to-peak variation of 1.5 mag and $(6160 \pm 400)\text{ d}$ ($\approx 17\text{ years}$) with a peak-to-peak variation² of 3.5 mag , and is classified as semi-regular (SRa) by Mayall (1965) and Mira variable by Knapp et al. (1999). While the 529.4 d period is typical of a luminous AGB star, Knapp et al. (1999) suggests that the regular long period dimming of V Hya is due to a thick dust cloud orbiting the star.

The rotation velocity of an AGB star, evolving in isolation, is not likely to be greater than 2 km s^{-1} , even if its main-sequence progenitor rotated at breakup velocity. In contrast, the rotation velocity, $v \sin i$, derived for V Hya from a high resolution optical spectral broadening analysis by Barnbaum et al. (1995) is on the order of $11\text{ to }14\text{ km s}^{-1}$. Barnbaum et al. (1995) and Kahane et al. (1996) concluded that this rapid rotation is due to the spin-up by a companion in a common envelope configuration, but alternative explanations have also been proposed (Luttermoser & Brown 1992; Olivier & Wood 2003). The secondary star could be an early G or F star, implying a mass of $1.0\text{--}1.5\text{ M}_\odot$, or possibly a WD (Barnbaum et al. 1995). V Hya is in contrast inferred to have a mass of about 1 M_\odot (Kahane et al. 1996). In addition, a wide companion, with a separation of 46 arcsec , exists (WDS).

A consequence of the fast rotation is an enhanced equatorial mass loss producing a disk and a jet-like structure (e.g. Soker 1992; Morris 1987). High angular resolution CO maps, millimeter, infrared and optical spectra suggest that the circumstellar structure of V Hya consists of three kinematic components: a low-velocity disk with a radial velocity of $\Delta v \approx \pm(8\text{ to }16)\text{ km s}^{-1}$, an intermediate-velocity wind with $\Delta v \approx \pm 60\text{ km s}^{-1}$, and a high-velocity jet with $\Delta v \approx \pm(60$

² The long secondary pulsation amplitudes in *JHKL* are 2.4, 2.1, 1.7, and 0.7 mag, respectively (Olivier et al. 2001).

Table 2. Number of visibility measurements used in this study.

Semester	Program ID	Disperser	R Aql	R Aqr	R Hya	W Hya	V Hya
79 (1st Apr., 2007–30th Sep., 2007)	079.D-0140	GRISM	11	10	18	22	8
80 (1st Oct., 2007–31st Mar., 2008)	080.D-0005	PRISM	6	10	16	17	26
81 (1st Apr., 2008–30th Sep., 2008)	081.D-0198	PRISM	15	7	16	18	8
82 ^a (1st Oct., 2008–31st Mar., 2009)	082.D-0641	PRISM	0	4	12	14	20
83 ^a (1st Apr., 2009–30th Sep., 2009)	083.D-0294	PRISM	8	8	10	12	1

Notes. See Appendix C for a detailed observation log and Paper I in the case of W Hya. ^(a) The observation program was still ongoing at the time of analyzing the data.

Table 3. Calibrator properties.

Calibrator name:	η Sgr	ϵ Peg	30 Psc	2 Cen	α Hya
Associated target ^a :	HD 167618 R Aql (46.4°)	HD 206778 R Aql (42.8°)	HD 224935 R Aqr (10.3°)	HD 120323 W Hya (6.1°) R Hya (12.0°)	HD 81797 V Hya (23.8°)
Spectral classification ^b :	M2 III	K2 Ib var	M3 III	M5 III	K3 III
Parallax ^b (mas):	21.87 ± 0.92	4.85 ± 0.84	7.86 ± 0.94	18.39 ± 0.74	18.40 ± 0.78
12 μ m flux ^c (Jy):	214 ± 9	104 ± 5	87 ± 4	255 ± 26	158 ± 10
Angular diameter ^c (mas):	11.66 ± 0.04	7.59 ± 0.05	7.24 ± 0.03	13.25 ± 0.06	9.14 ± 0.05
Quality flag ^d :	1	1	1	2	1

Notes. ^(a) For target properties see Table 1. The angular separation between calibrator and target is given in brackets. ^(b) Hipparcos (Perryman & ESA 1997b); ^(c) IRAS flux and model diameter from Verhoelst (2005), http://www.ster.kuleuven.ac.be/~tijl/MIDI_calibration/mcc.txt; ^(d) ESO CalVin database, <http://www.eso.org/observing/etc/>

to 200) km s⁻¹ (Zuckerman & Dyck 1986; Sahai & Wannier 1988; Lloyd Evans 1991; Knapp et al. 1997; Olivier et al. 2001; Hirano et al. 2004; Sahai et al. 2009).

The low-velocity circumstellar environment component is flattened or has a disk-like shape, and is elongated along the north-south direction (Tsuji et al. 1988; Kahane et al. 1988, 1996; Sahai et al. 2003). This may enable or enhance the formation of an accretion disk and supports a model in which the jet is driven by an accretion disk around an unseen, compact companion. Images obtained at 9.8 and 11.7 μ m by Lagadec et al. (2005) show an additional slightly elongated structure in the southwest direction, tracing the dust emission from material blown away, while the overall structure is roughly spherically symmetric.

The star has a large infrared excess and strong millimeter molecular line emission, showing that it is losing mass at a fairly high rate. Total mass-loss rates were estimated to $6.1 \times 10^{-5} M_{\odot} \text{ yr}^{-1}$ (De Beck et al. 2010), $2.5 \times 10^{-5} M_{\odot} \text{ yr}^{-1}$ (Knapp et al. 1997), $1.5 \times 10^{-6} M_{\odot} \text{ yr}^{-1}$ (Kahane et al. 1996; Knapp et al. 2000), and $1.0 \times 10^{-6} M_{\odot} \text{ yr}^{-1}$ (Barnbaum et al. 1995) with dust mass-loss rates of 2.0 to $5.7 \times 10^{-8} M_{\odot} \text{ yr}^{-1}$ (Knapp et al. 1997; Hirano et al. 2004, respectively). Knapp et al. (1997) modeled the dust envelope of V Hya by assuming grains consisting of amorphous carbon with dimensions of 0.2 μ m. Zuckerman & Dyck (1986) discovered the presence of a narrow CO emission feature superposed on a standard broad stellar CO profile, which probably represents the first example of a CO maser ever seen in any interstellar or circumstellar source.

3. Observations and data reduction

3.1. Interferometric observations with MIDI/VLTI

The data presented here were obtained with the mid-IR (8–13 μ m) interferometer MIDI (Leinert et al. 2003, 2004) at the Very Large Telescope Interferometer (VLTI) in service mode using the Auxiliary Telescopes (ATs). All five stars were monitored from P79 to P83 (April 2007 to September 2009) under the pro-

gram IDs 079.D-0140, 080.D-0005, 081.D-0198, 082.D-0641 and 083.D-0294 in GTO time. An overview of the course of observations is given in Table 2. It should be noted that observations were still ongoing at the time of analyzing the data, and that observations not executed in a specific semester are shifted to the next semester. A complete observation log is given in Table C.2 in the Appendix. Projected baselines range from 11 to 71 m and the position angles (PA, θ ; east of north) are differently distributed for each star. The uv-coverages are shown later in the left hand panels of Fig. 6.

Before or after each target observation a calibrator star is observed with the same setup in order to calibrate the visibilities and fluxes. The properties of the calibrator stars are listed in Table 3. Necessary input parameters for the calibration are the angular diameter (model diameter from Verhoelst 2005)³ and the IRAS⁴ 12 μ m flux. The second row lists the associated targets for which the calibrator is used. The angular separation between calibrator and target is given in brackets and shows that they are located relatively far away from each other as a consequence of the low number of available calibrators. However, this is fortunately not a big concern in the mid-infrared. In particular, the visibility calibration is not affected by different airmasses since both, the correlated and uncorrelated flux, changes proportionally with it. Nevertheless, observations need to be carried out under good seeing conditions (typical $\leq 1.4''$) and a clear sky. Both are necessary to have a long coherence time to obtain fringes and to reduce the infrared background.

In order to identify molecules and dust species, the mid-infrared fringes are spectrally dispersed. The high spectral resolution GRISM mode of MIDI, with $R = \lambda/\Delta\lambda = 230$, would be therefore of advantage, but introduces additional problems in the reduction process (e.g. the photometric channels are unfa-

³ http://www.ster.kuleuven.ac.be/~tijl/MIDI_calibration/mcc.txt; see also ESO CalVin database: <http://www.eso.org/observing/etc/>

⁴ <http://irsa.ipac.caltech.edu/Missions/iras.html>

Table 4. Fitted visual light and mid-IR light curves.

Target	Visual (AAVSO+ASAS)				$\Delta\phi$	Mid-IR (MIDI)	
	P days	T_0 JD	V_0 mag	V_{ampl} mag		N_0 Jy	N_{ampl} Jy
R Aql	271 ± 4	2 452 910	8.30	1.80 ± 0.15	-0.21 ± 0.50	377 ± 50	80 ± 50 (21%)
R Aqr	390 ± 5	2 452 480	8.75	2.75 ± 0.20	$+0.15 \pm 0.05$	1080 ± 100	330 ± 50 (31%)
R Hya	374 ± 5	2 453 231	6.95	1.95 ± 0.15	$+0.08 \pm 0.05$	1930 ± 200	240 ± 50 (12%)
W Hya	388 ± 5	2 452 922	7.56	1.41 ± 0.10	$+0.15 \pm 0.05$	4910 ± 200	510 ± 100 (10%)
V Hya ^d	529 ± 10	2 450 045	8.50	1.50 ± 0.10	$+0.29 \pm 0.05$	1330 ± 200	580 ± 200 (44%)

Notes. $V(t) = V_{\text{ampl}} \sin [2\pi(t - T_0)/P] + V_0$ and $N(t) = N_{\text{ampl}} \sin [2\pi(t - T_0)/P - \Delta\phi] + N_0$, respectively. The phase shift $\Delta\phi$ gives the positive offset in respect to the visual phase. ^(a) V Hya has a second period with $P_2 = (6160 \pm 400)$ days, $T_{0,2} = 2446937$ days, $V_{0,2} = 8.50$ mag and $V_{\text{ampl},2} = (3.50 \pm 0.50)$ mag (Knapp et al. 1999).

vorably illuminated). Hence, mainly the PRISM with a spectral resolution of 30 was used. Since the targets are bright enough, observations were executed in SCI-PHOT mode, where the photometric and the interferometric spectra are recorded simultaneously. This has the advantage that the photometric spectrum and the fringe signal are observed under the same atmospheric conditions.

3.2. MIDI SCI-PHOT data reduction

The standard MIA+EWS⁵ (version 1.6) data reduction package with additional routines for processing SCI-PHOT data (Jaffe, priv. comm.) was used. Measurements at wavelengths beyond $12.0 \mu\text{m}$ were excluded due to too low fluxes of the calibrator stars in that wavelength regime and therefore difficulties to determine the signal in the presence of a high infrared background⁶. The remaining wavelength range from 8 to $12 \mu\text{m}$ is then binned into 25 wavelength bins. A detailed description of the reduction process and how the errors are derived are given in Paper I and Zhao-Geisler (2010). In the end, 32 of 40, 26 of 39, 64 of 72, 75 of 83 and 48 of 63 observations could be adequately reduced for R Aql, R Aqr, R Hya, W Hya and V Hya, respectively. Rejected are observations where the reduction process failed or unphysical visibilities arose due to bad environmental conditions.

4. Light curves, spectra and visibility modeling results

4.1. Light curves

In order to assign a pulsation phase to the observations, visual data from the American Association of Variable Star Observers (AAVSO)⁷ and the All Sky Automated Survey (ASAS Pojmanski et al. 2005)⁸ are used. After binning the AAVSO data into 10 day bins a simple sinusoid is fitted to the AAVSO and ASAS data over a period of about 10 years (2000–2010). The

⁵ <http://www.strw.leidenuniv.nl/~nevec/MIDI>

⁶ Remaining flux, coming from short term variations of the high sky background and instrumental imperfections, not subtracted by the unchopping has to be determined and removed. The reduction routines have to distinguish between sky, tunnel and source flux, and have to know the slit position. This changes with AT position, projected baseline and pointing. If the flux of the calibrator is too low, its flux can not be reliably recovered and the calibration process fails.

⁷ <http://www.aavso.org/>

⁸ <http://www.astrouw.edu.pl/asas/>

resulting periods P , Julian Dates of maximum brightness T_0 (defined as phase 0.0), mean visual magnitudes V_0 and visual semi-amplitudes V_{ampl} are given in Table 4. The errors given are estimates derived from the fitting process. The uncertainties for T_0 and V_0 are of the same order as the uncertainties for the period and the visual semi-amplitude, respectively. Note that V Hya has two periods and the longer period is taken from Knapp et al. (1999).

For each star the photometric data as well as the fit are plotted in Fig. 1 versus time and versus visual phase, covering the period of the MIDI observations. In addition, the mid-IR fluxes in Jy (averaged between 11.5 and $12.5 \mu\text{m}$) obtained with MIDI are shown in the right hand panels as function of visual phase. As described in Paper I, the MIDI fluxes are strongly error-prone due to difficulties in the reduction removing instrumental imperfections and the large sky background which varies on short time scales. Additional scatter in the N -band flux originates from cycle-to-cycle variations caused by the movement of the dust shell in the case of a dust driven wind (e.g. Nowotny et al. 2010).

However, a clear phase dependence is detectable in each of the phase-folded plots. The results of a sinusoidal fit are summarized in Table 4. The table gives the relative phase shifts $\Delta\phi$ of the mid-IR maximum with respect to the visual maximum, the mean N -band fluxes N_0 and the semi-amplitudes N_{ampl} with the corresponding percentage flux variations given in brackets. R Aql shows only a very small variation in the mid-IR by eye, suggesting that the amplitude is overestimated by the fit, and it is even consistent with no variation at all. The poor fit could be the reason why a mid IR maximum before the visual maximum is obtained in comparison to the other objects.

The Mira R Aqr and the semiregular variable V Hya show the highest mid-IR flux variations. Both systems are close binary systems and might therefore contain a large amount of circumstellar material. The fit to the mid-IR flux data of R Aqr is fair and the flux variation of about 30% seems to be real. Even though the mass-loss rate is low, the orbiting dust in this symbiotic system could be the reason for an increased mid-IR flux variation.

In contrast, the mid-IR flux of V Hya varies not only with a high amplitude but also with a large scatter, resulting in a fit which is not very robust. Since V Hya displays two superimposed visual periods, an assignment of a visual phase is not an adequate description. Even if the short period is Mira-like, the cause and influence of the long secondary period is not well known. Many different causes probably contribute to its large and varying mid-IR flux. In C-rich stars the production of carbonaceous dust is more effective, and hence more dust can radiate. The fact that V Hya is probably a common envelope

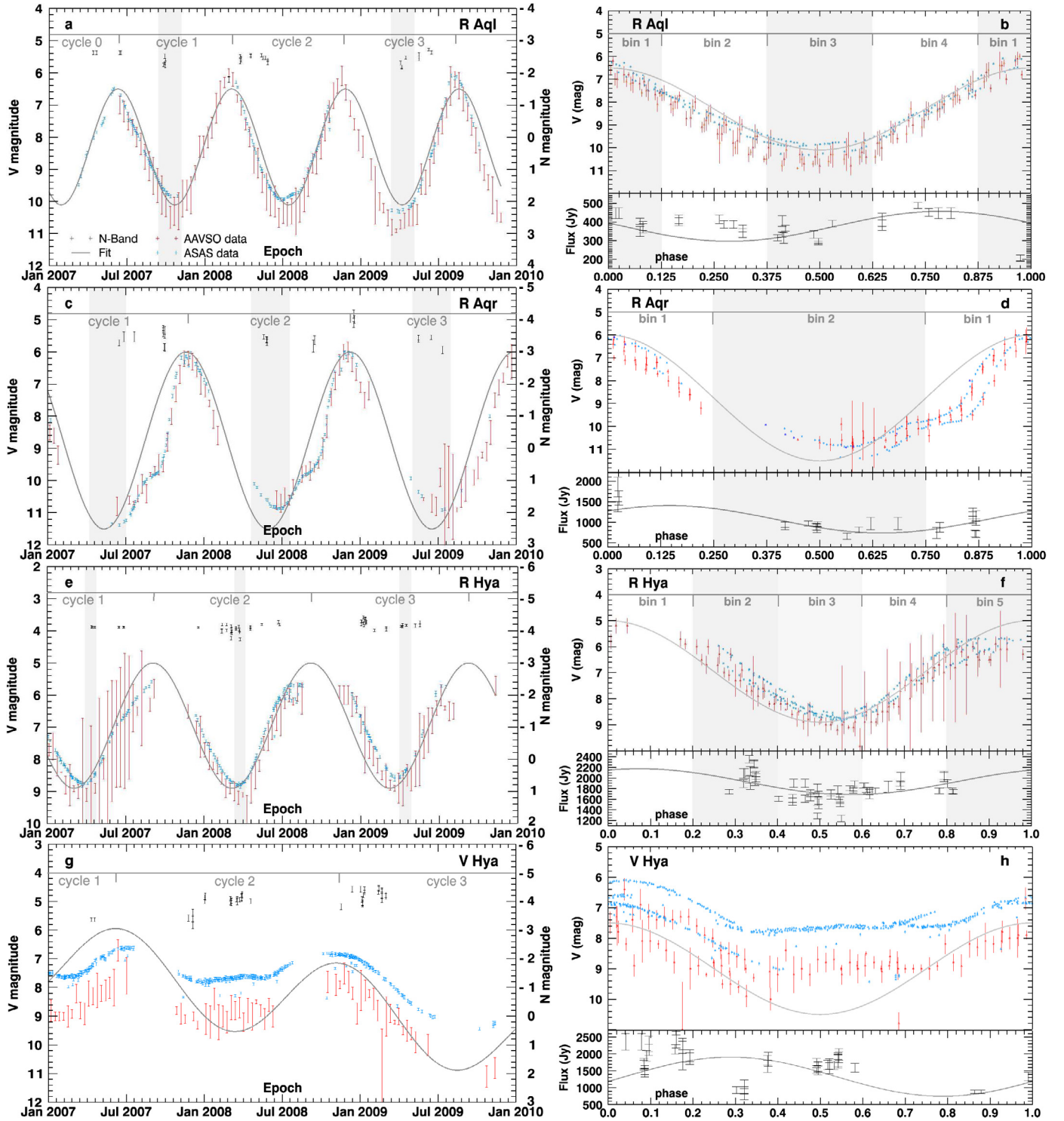


Fig. 1. *Left:* visual light curves covering the period of the MIDI observations. Simple sinusoidal fits are included to determine the pulsation phases used throughout this paper. The MIDI fluxes at around $12\ \mu\text{m}$ are shown as well with the magnitude scale given on the right. *Right:* same as left, but plotted versus visual phase. The MIDI fluxes at around $12\ \mu\text{m}$ are shown in the lower panels of each plot. The data within the shaded regions in both columns are used for size and flux variation studies in Sect. 5.3. The corresponding plots for W Hya can be found in Paper I (Figs. 3 and 4, respectively).

system might be related to this. However, V Hya’s evolutionary status as post AGB star, exhibiting the superwind phase with a fast and dense mass loss, might be the main reason for the varying mid-IR flux.

R Hya had a very smooth and regular visual light curve over the last decade. MIDI observations were only possible around

minimum visual light, since the period is close to one year. As a result, the mid-IR light curve could not be well constrained and the observed flux variation is relatively small, only on the order of 10%. The mid-IR and visual light curves of W Hya are very stable with only moderate amplitudes as well. For both stars, the low mid-IR flux variations might be related to the low mass-loss

rates. Since W Hya and R Hya are fairly nearby, both stars have high absolute mid-IR fluxes.

Even if the mid-IR flux variations of all five AGB stars are much smaller than the visual ones, they are still on the order of 10% to 30%. Similar flux amplitudes in the mid-IR have been reported for other AGB stars as well (cf. references given in Paper I). Except for R Aql, the mid-IR maximum occurs always after the visual maximum at an average visual phase of 0.15 ± 0.05 . This phase shift is consistent with previous studies of AGB stars (cf. e.g. Lattanzio & Wood 2004; Smith et al. 2006; Nowotny et al. 2010, and references therein). The reason for this phase-lag is most probably related to the dynamic processes of shock front and dust formation.

Since the mid-IR fits are relatively uncertain, all data are interpreted with respect to the visual light curve in the following. It should also be kept in mind that folding consecutive cycles into one cycle might not always be appropriate, since the pulsation is not strictly regular, in particular for V Hya (see Fig. 1).

4.2. Spectra

All calibrated MIDI spectra for each star are median averaged over all phases and cycles and are shown in the spectral energy distribution (SED) plots in the left hand panels of Fig. 2. The uncertainties are given by the standard deviation. The flux levels of ISO⁹ and IRAS¹⁰ have been adjusted to coincide with the 12 μm flux. Photometric data from 2MASS and IRAS are plotted as well. A blackbody curve is over-plotted as guidance, assuming a diameter and temperature which best represents the data points by eye. However, due to the infrared excess, strong metallic oxide lines, molecule absorption and dust extinction, it is not expected that a blackbody curve fits the spectral data in an appropriate way. Individual spectra of the MIDI observations are given in the right hand panels of Fig. 2, showing the same features as the averaged MIDI spectra in the left hand panels.

The ISO spectra of the O-rich stars are mainly dominated by absorption bands of H₂O between 2.5–3.0 μm (stretching mode) and 5.0–8.0 μm (bending mode), and an SiO absorption band between 8 and 9 μm ($\nu = 1-0$). Distinct absorption lines of CO at around 2.4 μm , OH at 2.9–4.0 μm , CO₂ at 4.25 μm and SO₂ at 7.4 μm can be seen in the spectra of some of the stars. From temperature investigations by e.g. Justtanont et al. (2004) for W Hya it could be derived that these absorptions originate from different molecular layers located in the close atmospheric environment of the star. OH and CO absorption bands arise mainly from a hot (about 3000 K), dense region very close to the stellar photosphere, where H₂O is still photodissociated by shocks. H₂O and CO₂ absorption bands originate from a layer with a temperature of 1000 K, i.e. a molecular layer (MOLsphere) farther out. The SiO molecule absorption arises in the same region where the H₂O molecular shell exists and where SiO is still not bound in dust grains.

All O-rich stars in the sample show dust emission in their ISO spectrum with different peculiarities. The features between 10 and 20 μm are a combination of emission from amorphous silicates at 9.7 μm , amorphous Al₂O₃ at around 11.5 μm , and MgFeO at around 19 μm . Regarding the 13 μm emission feature, seen in R Aql, R Hya and W Hya, it is still under debate whether it comes from spinel (MgAl₂O₄) (e.g. Posch et al. 1999; Fabian et al. 2001; Heras & Honny 2005) or corundum (crys-

talline Al₂O₃, α -Al₂O₃) (e.g. Onaka et al. 1989; DePew et al. 2006). W Hya is the only star which clearly shows the molecular SO₂ emission feature in the spectrum (Justtanont et al. 2004; Zhao-Geisler et al. 2011), while R Aqr is the only star which is completely dominated by amorphous silicate dust emission. In addition, R Aqr has an overabundance of SiO molecules as discussed in Angeloni et al. (2007). All stars also exhibit a remarkable infrared excess. In the dust emission scheme of Sloan & Price (1998b) R Hya is classified as SE2t (broad oxygen-rich dust emission), R Aql as SE5 (structured silicate emission), and R Aqr and W Hya as SE7 and SE8, respectively (classic narrow silicate emissions).

If the individual and averaged MIDI spectra are compared with the ISO spectra (cf. Fig. 2), it becomes obvious that the silicate emission at around 9.7 μm is not detected except for R Aqr. This behavior can be attributed to instrumental characteristics. ISO has a much larger field of view (FoV) compared to MIDI. With a small FoV of about 1 to 2 arcsec¹¹, the emission of the extended silicate dust shell could therefore not be observed with MIDI.

This applies to the nearby stars R Hya and W Hya. R Aql and R Aqr are located farther away and have nearly the same distance. Therefore, both stars should both either show or not show the silicate dust emission feature, but this apparent contradiction can be solved. In Sect. 5.1 it will be seen that the dust shell around R Aqr is much closer due to the fact that R Aqr is a symbiotic system probably containing a large amount of dust.

However, this non-detection allows to derive a lower limit for the inner boundary of the silicate dust shell. Assuming a conservative value of the FoV of 1 arcsec, most of the silicate dust emission originates from a shell with an inner diameter larger than about 100 θ_{phot} ¹² (>220 AU), 49 θ_{phot} (>130 AU), and 28 θ_{phot} (>90 AU) for R Aql, R Hya, and W Hya, respectively. However, this does not mean that silicate dust does not exist closer to the star. Its abundance is just below the detection limit of MIDI. For R Aqr it can be speculated that silicate dust must exist farther out, at a region with a diameter larger than 72 θ_{phot} (>250 AU), since with the larger FoV of ISO more silicate emission could be revealed than with the smaller FoV of MIDI (Fig. 2c).

The absolute flux levels for the MIDI spectra are lower than those of ISO/SWS and IRAS as it should be expected since the FoV of MIDI is smaller than those of ISO/SWS and IRAS. Also the 3.5 μm region of the ISO/SWS spectra, considered as a pseudo continuum, does nicely overlap with the blackbody continuum. However, this is not the case for R Hya. This might be due to a calibration problem at around 9 μm since the IRAS spectrum is flat around that point while it is not for the ISO/SWS one. At the same time, the flux level of the MIDI spectrum is slightly higher, but this is probably due to the large MIDI flux calibration uncertainties. A flux variation due to the pulsation can be ruled out since the ISO spectrum is taken at around visual maximum while the averaged MIDI spectrum of R Hya is mainly an averages of spectra taken around visual minimum.

V Hya is the only carbon star in the sample. The MIDI spectrum shows very clearly the dust emission of SiC at 11.3 μm . Amorphous carbon, which makes up most of the dust, is featureless. Both dust species typically condensate at around 2 photospheric radii at a temperature of around 1500 K (cf. e.g. Ohnaka et al. 2007). Molecular shells of C₂H₂ (bands at 8–9 μm

¹¹ The exact value depends on the baseline used, the slit/mask position and other instrumental specifications.

¹² Photospheric diameter of the star, cf. Sect. 4.4.

⁹ Sloan et al. (2003) and <http://iso.esac.esa.int/ida/>

¹⁰ <http://irsa.ipac.caltech.edu/Missions/iras.html>

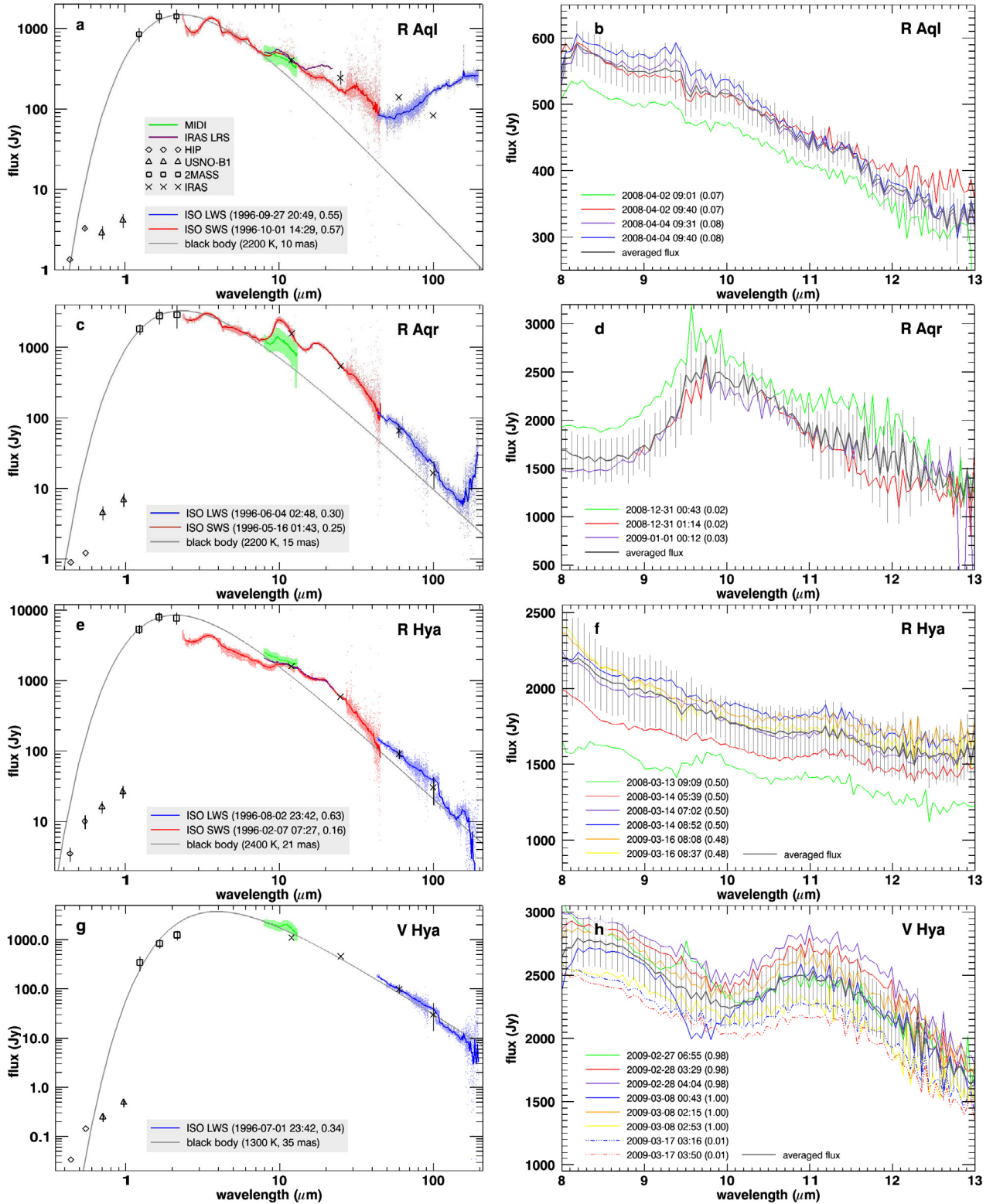


Fig. 2. *Left:* spectral energy distribution for all stars (see text). The black body curve is only included for guidance. *Right:* all available individual MIDI spectra around the visual maxima for all stars (including an average of these) except for R Hya where the spectra around the visual minima are given. The visual light phases are given in brackets. Note that due to the telluric ozone feature the uncertainties at around $9.6 \mu\text{m}$ are increased. The corresponding plots for W Hya can be found in Paper I (Fig. 5).

and 11–14 μm) and HCN (band at 11–13 μm) at different distances and temperatures from the star might be present as well, but are not resolved in the low resolution MIDI spectra. The absolute flux level of the MIDI spectrum is also reasonable and joins with the blackbody curve. In the scheme of Sloan et al.

(1998a), V Hya is categorized as Red, meaning that a strong continuum increase in intensity toward longer wavelengths is superposed on the dust features.

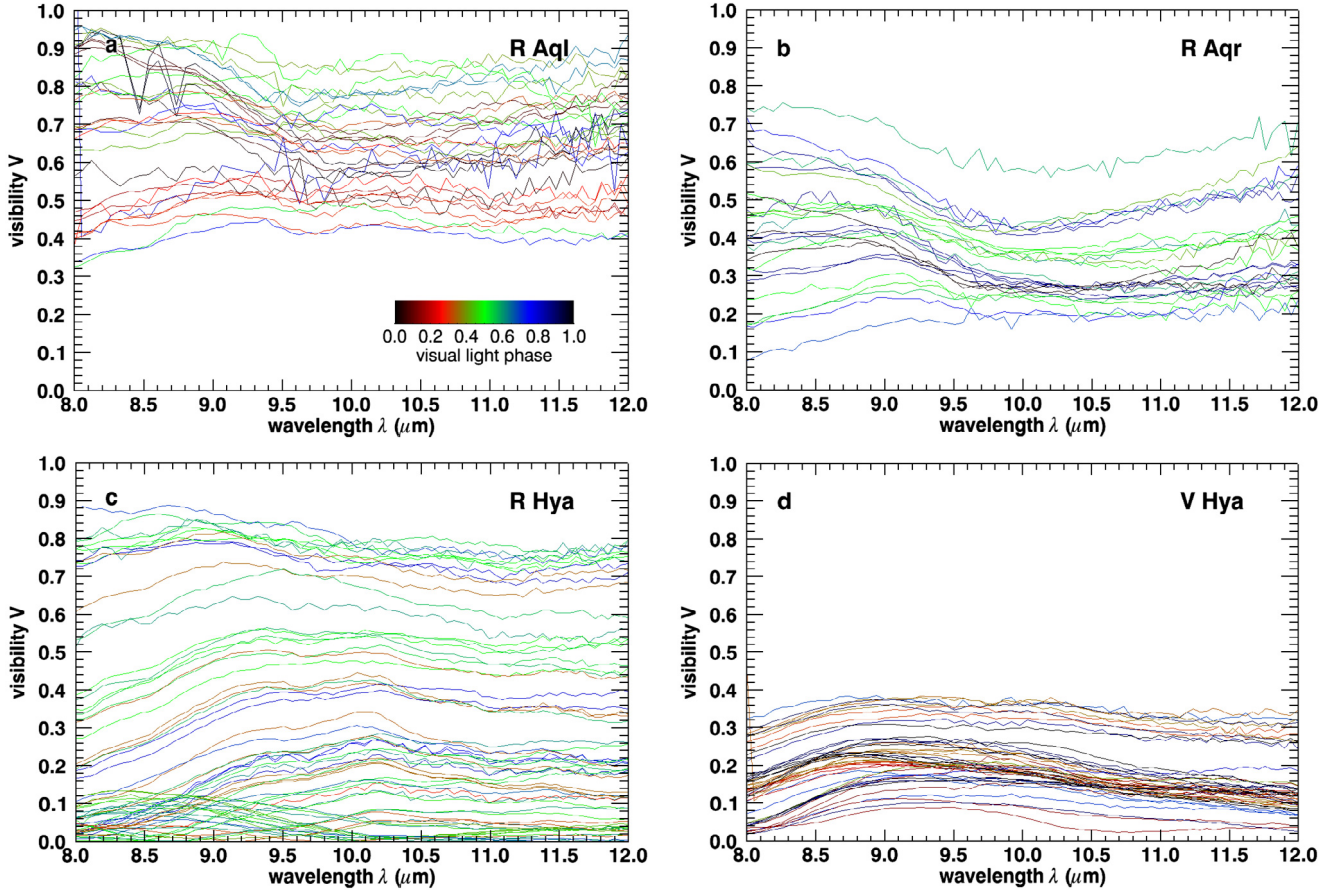


Fig. 3. Calibrated visibilities as function of wavelength, color-coded by visual light phase. Errors are omitted for clarity but are given in Tables A.1 to A.4. The corresponding plot for W Hya can be found in Paper I (Fig. 1).

4.3. Visibility modeling results

The most straight-forward way of interpreting sparsely sampled interferometric data (visibilities) is by fitting the Fourier transform of an assumed brightness distribution of the object. Simple size estimations can be obtained from elementary geometrical models with only a few free parameters. As mentioned in the introduction, the definition of a diameter is difficult because of its strong wavelength dependence as well as of phase-to-phase and long-term cycle-to-cycle variations. On the other hand, the size and its dependence on wavelength and pulsation phase can give some constraints on the chemical and physical mechanisms which are responsible for this appearance, but also which layer of the atmosphere is actually observed. This work focuses on interpreting the data using simple geometric models. In this section, all measurements over all pulsation phases, cycles and position angles are taken into account, knowing that this potentially biases the interpretation, but will give a first description of the size of the structures. In Sect. 5.3, measurements are interpreted through each available pulsation phase allowing to put constraints on the dynamical mechanisms involved. Self-consistent hydrodynamic models will be required for a more realistic analysis.

The low surface gravity results in an extended atmosphere and temperature structure and the formation of molecular layers around late-type stars. Therefore, no sharp transition between the star and the circumstellar environment exists. These stars can usually be modeled by using a uniform disk (UD) to account for the star and a uniform ring to represent a molecular layer (or simpler with two uniform disks). However, this would increase

the numbers of parameters to be fitted, and the later discussed pulsation dependence studies (Sect. 5.3) would not be possible. Therefore, a simple fully limb-darkened disk (FDD) will be used to represent the stellar photosphere and the close molecular environment. One can assume that the fitted FDD diameter will consequently be located in between the stellar photosphere and the outer boundary of the close molecular environment detectable with MIDI.

Uniform disk (UD) model fits are given for comparison where appropriate. For some of the stars, a Gaussian function is added to constrain the size of the extended dust shell. For the stars where this was not possible, i.e. where the dust shell was overresolved, only the flux contribution of a surrounding dust shell were determined by not forcing the visibility function to be 1 at zero spatial frequency (referred to as relative FDD/UD). The total visibility function, V , is written as

$$V = |\epsilon_{\text{FDD}} \mathcal{V}_{\text{FDD}} + (1 - \epsilon_{\text{FDD}}) \mathcal{V}_{\text{Gaussian}}|, \quad (1)$$

with ϵ_{FDD} the flux contribution of the FDD and \mathcal{V} the complex visibilities (Zhao-Geisler 2010). For an overresolved dust shell, $\mathcal{V}_{\text{Gaussian}}$ is equal to zero.

The final calibrated visibilities are shown in Fig. 3 as function of wavelength, whereas the assigned visibility errors are given in Tables A.1 to A.4. As described in Paper I, the visibility uncertainties are assumed to be the same within each wavelength bin to compensate for difficulties in determining them and to ensure a better fitting. The best model fits are displayed in the left hand panels of Fig. 4 for each star. The fit and the data, color-coded by visual light phase, are plotted as function of spatial

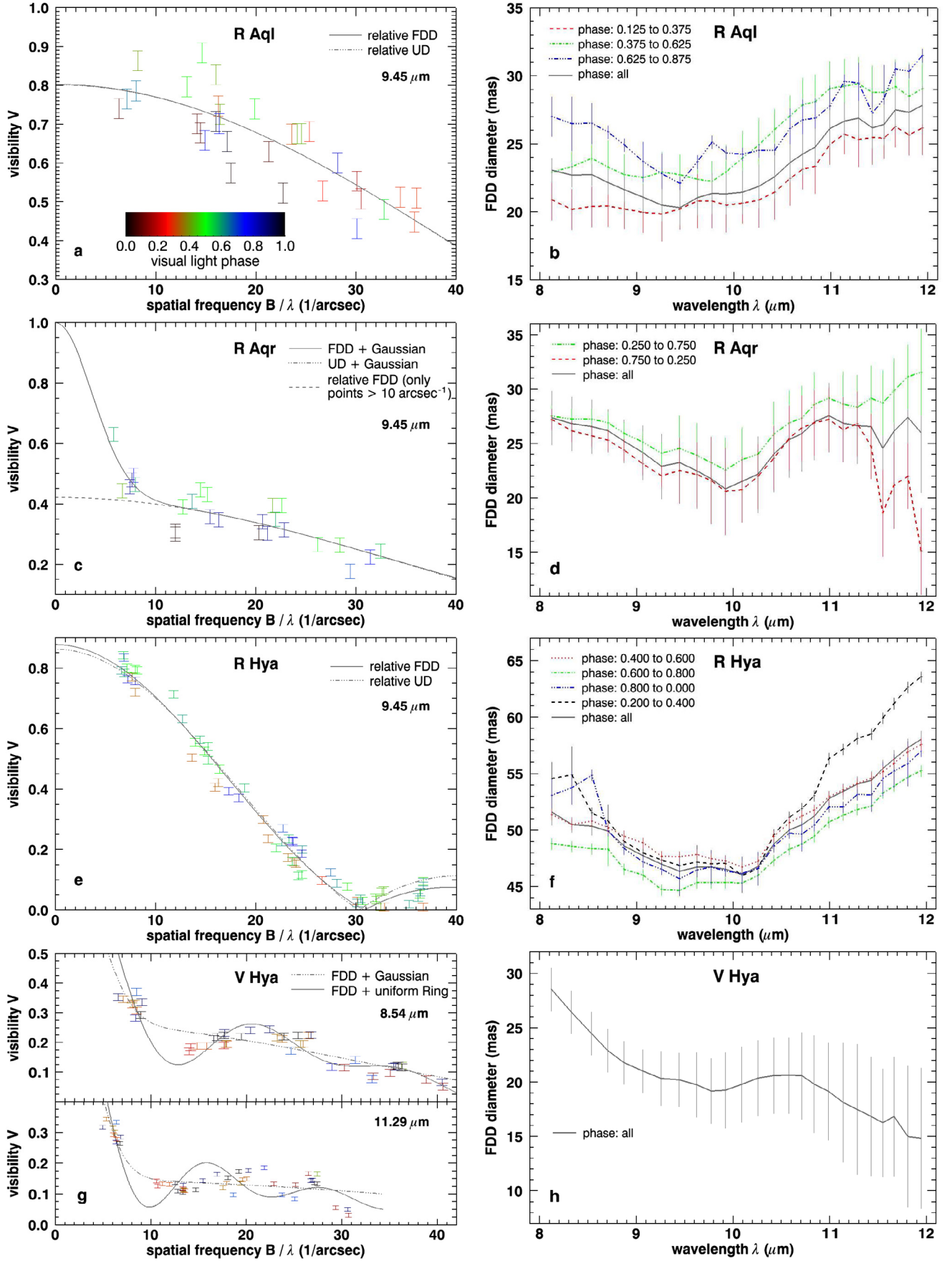


Fig. 4. *Left:* fits of different models to the visibility measurements at a representative wavelength. The visibility data are plotted versus spatial frequency and are color-coded by visual light phase. *Right:* the fitted circular fully limb-darkened disk diameter, θ_{FDD} , as function of wavelength for the full data set and selected pulsation phases. The corresponding plots for W Hya can be found in Paper I (Figs. 6 and 8, respectively).

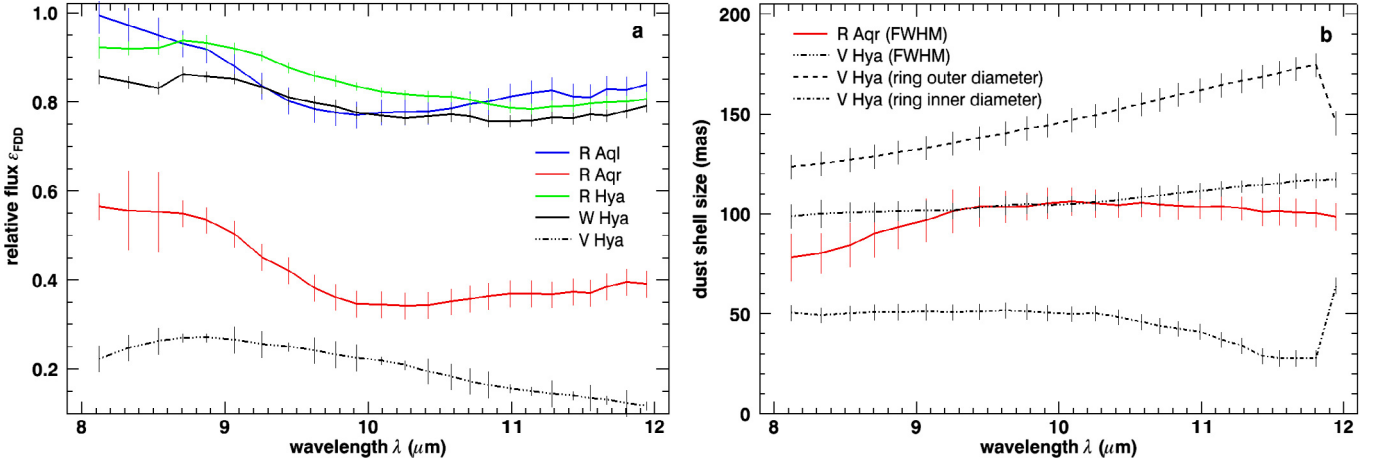


Fig. 5. *Left:* the relative flux contributions, ϵ_{FDD} , of the circular FDD obtained for the fits to the full data sets. *Right:* Gaussian FWHM, θ_{G} , and ring, $\theta_{\text{R,in}}$ and $\theta_{\text{R,out}}$, dust shell sizes obtained from the fit to the full data set for two of the five stars as function of wavelength.

Table 5. Summary of the results.

Target:	R Aql	R Aqr	R Hya	W Hya	V Hya
Best model:	relative FDD	FDD + Gaussian	relative FDD	relative FDD	FDD + Gaussian
ϵ_{FDD} layer ^a	0.77 ± 0.02	0.35 ± 0.03	0.84 ± 0.01	0.78 ± 0.01	0.23 ± 0.03
θ_{FDD} layer ^a (mas):	21.3 ± 2.0 (4.7 AU)	20.9 ± 3.5 (5.2 AU)	46.6 ± 0.6 (6.1 AU)	79.0 ± 1.2 (7.1 AU)	19.3 ± 3.5 (6.9 AU)
θ_{G} dust ^{a,b} (mas):	>1000 (>220 AU)	105 ± 8 (26.3 AU)	>1000 (>130 AU)	>1000 (>90 AU)	105 ± 4 (37.8 AU)
assumed θ_{phot} ^c (mas):	9.6 ± 1.2	13.8 ± 2.5	20.4 ± 1.0	35.7 ± 2.7	12.1 ± 0.3
assumed θ_{SiO} ^d (mas):	24.2 ± 2.7	31.7 ± 1.2	–	77.3 ± 10.5	–
$\theta_{\text{FDD},12\mu\text{m}} / \theta_{\text{FDD},10\mu\text{m}}$:	$(31 \pm 15)\%$	$(24 \pm 34)\%$	$(24 \pm 2)\%$	$(31 \pm 3)\%$	$(18 \pm 5)\%$ ^e
$\theta_{\text{SiO}} / \theta_{\text{phot}}$:	2.5 ± 0.4	2.3 ± 0.4	–	2.2 ± 0.3	–
$\theta_{\text{FDD},10\mu\text{m}} / \theta_{\text{phot}}$:	2.2 ± 0.3	1.5 ± 0.4	2.3 ± 0.1	2.2 ± 0.2	1.6 ± 0.3
$\theta_{\text{G},10\mu\text{m}} / \theta_{\text{phot}}$ ^b :	>100	7.6 ± 1.5	>49	>28	8.7 ± 0.4
Phase-to-phase variations:					
$\bar{\theta}_{\text{FDD,max}} / \bar{\theta}_{\text{FDD,min}}$:	$(18 \pm 12)\%$	$(14 \pm 19)\%$	$(8 \pm 3)\%$	$(13 \pm 4)\%$	–
$\bar{\epsilon}_{\text{FDD,max}} / \bar{\epsilon}_{\text{FDD,min}}$:	$(13 \pm 10)\%$	$(18 \pm 23)\%$	$(10 \pm 10)\%$	$(7 \pm 10)\%$	–
Cycle-to-cycle variations:					
Asymmetry:	no	yes	no	yes	yes

Notes. ^(a) At $10 \mu\text{m}$. ^(b) Lower limits of the dust shell diameter (not Gaussian) for R Aql, R Hya and W Hya are obtained from FoV restrictions (cf. Sect. 4.2). ^(c) Assumed photospheric diameter derived from the *K*-band diameter (Table 1) divided by 1.2 (cf. e.g. Millan-Gabet et al. 2005). ^(d) Assumed SiO ring diameter (average of the values given in Sect. 2, but see also Sect. 4.4). ^(e) For V Hya, $\theta_{\text{G},12 \mu\text{m}} / \theta_{\text{G},8 \mu\text{m}}$ is given.

frequency (projected baseline divided by wavelength) for a representative wavelength. It is important to note that different spatial frequencies probe different regions, i.e. high spatial frequencies are sensitive to small regions and low spatial frequencies to extended structures.

The best model parameters with errors are derived by performing the Levenberg-Marquardt least-squares minimization procedure programmed for the interactive data language IDL as MPFIT by C. B. Markwardt¹³ as described in Paper I. The FDD diameter as function of wavelength is shown in the right hand panels of Fig. 4 for the full data set and selected pulsation phase bins (details on the dynamic behavior are discussed in Sect. 5.3). The according numerical values are listed in Tables A.1 to A.4. The relative flux contribution of the FDDs and the dust shell sizes as function of wavelength are plotted in Fig. 5. The results for each star are described in the following in more detail and are summarized in Table 5.

¹³ <http://cow.physics.wisc.edu/~craigm/idl/idl.html>

4.3.1. R Aql and R Aqr

The individual visibility measurements of R Aql and R Aqr (Figs. 4a,c) have a relatively high scatter. This is caused mainly by the low *N*-band flux of the target and the calibrator and therefore a low signal-to-noise ratio of the fringe signal, but also due to the fact that the plot contains observations made at different pulsation phases and pulsation cycles. Intrinsic asymmetries of the objects might have an influence on the scatter as well.

The distribution of the visibilities suggests that two components contribute to the total visibility, since for both stars the values are significantly below one at low spatial frequencies. This can be attributed to the presence of a dust shell, which was already inferred from the MIDI spectra and its comparison with the ISO spectra. However, from Figs. 4a,c, it is clear that the size of the dust shell can only be estimated for R Aqr. Due to the lack of measurements at very low spatial frequencies this is not possible for R Aql (a lower limit is obtained from the limited FoV, cf. Sect. 4.2).

Even though the first zero is not present, the clear decline with increasing spatial frequency makes it possible to fit a circular FDD or circular UD as second component to the data. A UD is in general best suited for a first diameter estimation of a star and is therefore often used in the literature. However, the investigation of the O-rich stars R Hya and W Hya, presented below, suggests that an equally simple geometrical FDD describes the observed visibilities in O-rich stars much better in the second lobe. However, both models are not distinguishable in the case of R Aql and R Aqr (Figs. 4a,c).

The behavior of the FDD diameter, θ_{FDD} , as function of wavelength in the N -band is different for both stars (Figs. 4b,d and Tables A.1, A.2). While for R Aql, θ_{FDD} only slightly decreases from (23.1 ± 1.5) mas to (21.3 ± 2.0) mas, going from $8 \mu\text{m}$ to $10 \mu\text{m}$, the relative decrease for R Aqr, from (27.4 ± 2.5) mas to (20.9 ± 3.5) mas, is much higher. The following relative increase, $\theta_{12 \mu\text{m}}/\theta_{10 \mu\text{m}}$, beyond $10 \mu\text{m}$ is however similar, being $(31 \pm 15)\%$ for R Aql and $(24 \pm 34)\%$ for R Aqr. This apparent diameter increase from about 21 mas to (27.8 ± 2.0) mas and about 21 mas to (26.0 ± 5.5) mas is equivalent to an increase from 4.6 AU to 6.2 AU and 5.3 AU to 6.5 AU at the assumed distance of R Aql and R Aqr, respectively.

In comparison, the relative flux contribution of the FDD component, ϵ_{FDD} , decreases from (0.99 ± 0.02) to (0.80 ± 0.02) and from (0.57 ± 0.03) to (0.39 ± 0.03) for R Aql and R Aqr, respectively, going to longer wavelengths (Fig. 5a). This decrease reflects the increased flux contribution from the colder surrounding dust shell. In contrast to R Aql, the relative mid-IR flux contribution of the star/molecule layer of R Aqr is considerably lower because of the larger amount of circumstellar dust bound in the symbiotic system.

For R Aqr, measurements at spatial frequencies lower than 10 arcsec^{-1} have larger visibilities than expected for a pure FDD. This is illustrated in Fig. 4c by fitting a FDD to the measurements excluding the ones shortward of 10 arcsec^{-1} . This gives the possibility to constrain the inner extension of the silicate dust shell interferometrically. However, the Gaussian fit is dominated by one point at around 6 arcsec^{-1} , and therefore the result should be taken with caution. On the other hand, this single measurement was taken close in time to the points at around 7.5 arcsec^{-1} and has a position angle not too far off.

The fitted Gaussian FWHM diameter for R Aqr steadily increases from (78 ± 12) mas to (104 ± 7) mas between 8 and $10 \mu\text{m}$, and stays around this value between 10 and $12 \mu\text{m}$ (Fig. 5b). This is equivalent to an increase from 20 AU to 26 AU and sets the characteristic silicate dust shell radius at $10 \mu\text{m}$ at a distance of about 7.6 ± 1.5 times the photospheric radius. The constant or even slightly declining FWHM at wavelengths longward of $10 \mu\text{m}$ could be a hint that the dust shell is truncated due to the gravitational conditions set by the orbiting WD with a semi-major axis of around 15 AU (60 mas) (cf. Sect. 2.2). With the sudden decline of the dust density, cold dust in outer regions, probed by wavelengths longer than $10 \mu\text{m}$, is less abundant and can therefore not be detected. This would be also consistent with the low mass-loss rate reported for R Aqr.

4.3.2. R Hya and W Hya

The relatively high flux of the target and the calibrator entails a comparatively small scatter in the visibility measurements of R Hya and W Hya (Fig. 4e, and Fig. 6 in Paper I, respectively). However, there is still a considerable spread due to including observations obtained at different pulsations phases, pulsation cycles and position angles. From the investigation of W Hya in

Paper I (Fig. 6) and the plot for R Hya in Fig. 4e it can be seen that a circular FDD model can well reproduce the visibility amplitude in the second lobe.

The FDD diameter as function of wavelength in the N -band is similar for both stars (Fig. 4f, and Fig. 8 in Paper I). They are qualitatively also comparable to R Aql. While the FDD diameter of R Hya decreases only marginally from (51.6 ± 1.2) mas to (46.6 ± 0.6) mas between 8 and $10 \mu\text{m}$, θ_{FDD} stays almost constant at a value of about (80 ± 1.2) mas for W Hya. At wavelengths longer than $10 \mu\text{m}$ the apparent diameters gradually increase again and reach (58.0 ± 0.8) mas and (105 ± 1.2) mas at $12 \mu\text{m}$, corresponding to a relative increase, $\theta_{12 \mu\text{m}}/\theta_{10 \mu\text{m}}$, of $(24 \pm 2)\%$ and $(31 \pm 3)\%$ for R Hya and W Hya, respectively. The apparent diameter increase from 47 mas to 58 mas and 80 mas to 105 mas is equivalent to an increase from 6.1 AU to 7.5 AU and 7.1 AU to 9.5 AU at the distance of R Hya and W Hya, respectively.

In order to account for the flux contribution of an extended dust shell, the visibility function is not forced to be 1 at zero spatial frequency. Figure 5a shows that with longer wavelengths the relative flux contribution of the FDD, ϵ_{FDD} , decreases from (0.92 ± 0.03) to about (0.80 ± 0.02) and from (0.85 ± 0.02) to about (0.77 ± 0.02) for R Hya and W Hya, respectively, reflecting the increased flux contribution from the colder surrounding dust shell. This is very similar to R Aql.

4.3.3. V Hya

The scatter in the visibility measurements in the only C-rich AGB star in the sample is acceptable, since the target and the calibrator have a comparatively high flux (Fig. 4g). However, there is a considerable spread notably at higher spatial frequencies. This can probably be attributed to the presence of the temporally and spatially changing high velocity outflows (cf. Sect. 2.5).

A model consisting of two components is necessary to describe the visibility measurements. One component is needed to explain the moderate decrease of the visibilities from 10 to 40 arcsec^{-1} . As for the other stars, this could be either a UD or an FDD. Both geometrical models cannot be distinguished by these observations. As for the O-rich stars, the FDD will be preferred in the following.

The second component is essential to account for the points with high visibilities at spatial frequencies around 7 arcsec^{-1} . Similar to O-rich stars, a Gaussian, representing a carbon-rich (AMC + SiC) dust shell, could be an adequate function. However, the sinusoidal visibility variation between 10 and 20 arcsec^{-1} suggests a brightness distribution with steep edges. A uniform circular ring with a sharp inner and outer edge could be a proper function describing a dust shell and causing a sinusoidal modulation. Since the sinusoidal effect is only weak at longer wavelengths the dust shell is better represented by a Gaussian in that wavelength regime.

This is shown in Fig. 4g in more detail. At shorter wavelengths the FDD + ring model fits apparently better (upper panel, $8.5 \mu\text{m}$), while at longer wavelengths the FDD + Gaussian model is better (lower panel, $11.3 \mu\text{m}$). However, a comparison of the reduced chi square values, χ_r^2 , in Table A.4 reveals that the FDD + Gaussian model is actually the best representation across the whole N -band. Nevertheless, the χ_r^2 's are very similar between 8 and $9 \mu\text{m}$ for both models.

Due to the lack of measurements at very low spatial frequencies the boundaries of the ring and the FWHM of the Gaussian are less well constrained, respectively. Since the fit included all measurements, morphological and variability effects

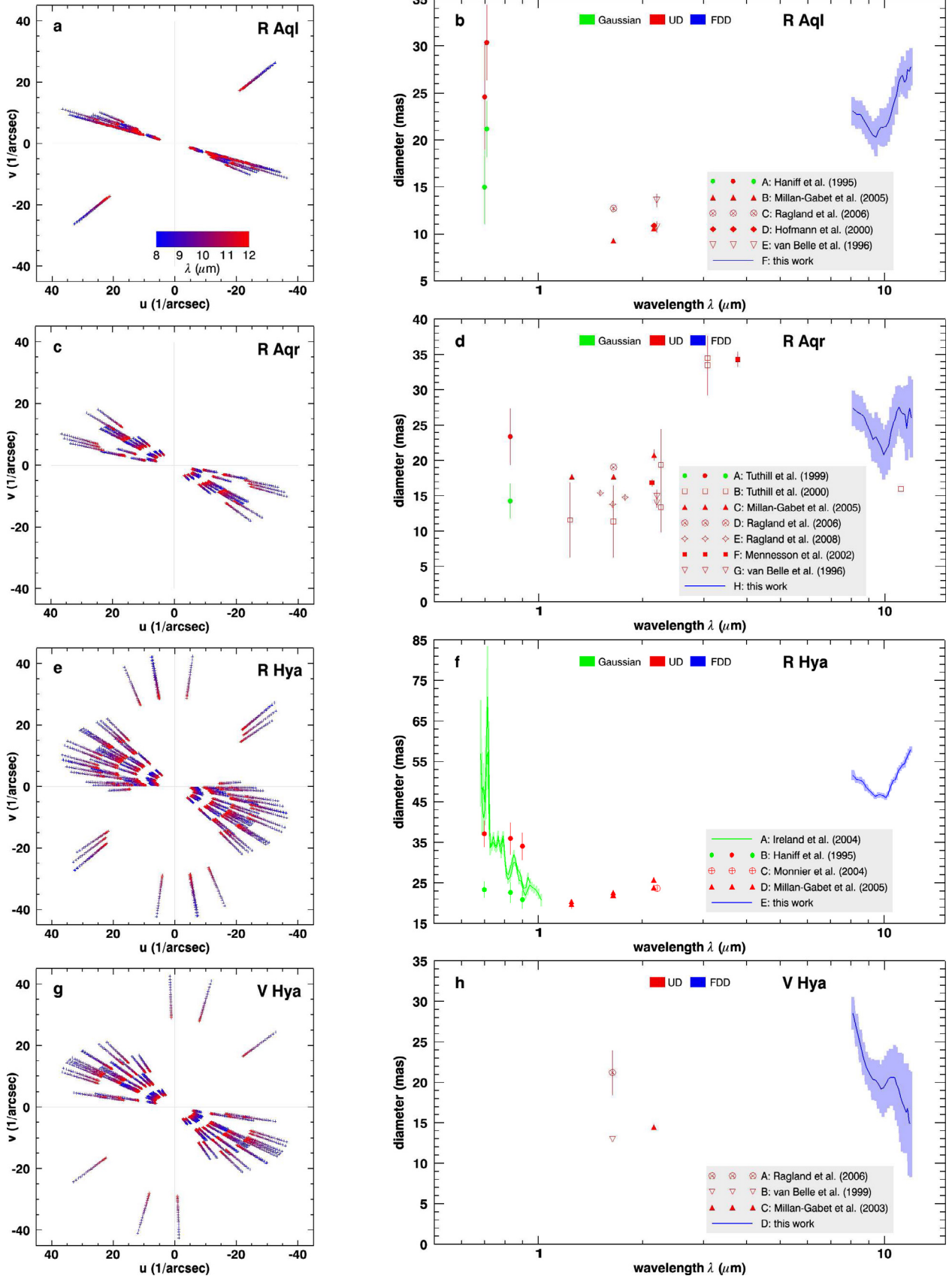


Fig. 6. *Left:* UV-coverage of all used interferometric observations. The visibility spectra are binned into 25 wavelength bins. *Right:* diameter measurements over a wide wavelength range with different models reported by various authors (FDD \approx 1.15 UD \approx 1.68 Gaussian). See Sect. 4.4 and Table B.1 (Appendix B) for more details. The corresponding UV-plot for W Hya can be found in Paper I (Fig. 1) and an updated diameter plot for W Hya is shown in Fig. 7.

are expected to have a non-negligible influence on the visibility measurements for this star. In particular, the ring dimensions should be taken with caution and the Gaussian FWHM should be used as a rough estimation of the inner dust shell boundary.

The trend of the FDD diameter as function of wavelength in the *N*-band is shown in Fig. 4h. It can be inferred from this plot (and Table A.4) that θ_{FDD} decreases from (28.5 ± 2.0) mas to (14.9 ± 6.5) mas between 8 and 12 μm with a local maximum at around 10.6 μm . This corresponds to a relative decrease $\theta_{12\ \mu\text{m}}/\theta_{8\ \mu\text{m}}$ of $(48 \pm 24)\%$. V Hya is the only star in the sample exhibiting a strong diameter decrease from short to long wavelengths. The diameter decrease from 28.5 mas to 14.9 mas is equivalent to a decrease from 10.3 AU to 5.4 AU at the distance of V Hya.

The relative flux contribution of the FDD, ϵ_{FDD} , decreases from a maximum of (0.27 ± 0.03) at 8.8 μm to (0.12 ± 0.02) at 12 μm , reflecting the increased flux contribution from the colder surrounding AMC and SiC dust shell detected at longer wavelengths (Fig. 5a and Sect. 5.2). This decrease is similar to the O-rich stars in the sample. As for R Aqr, the flux contribution of the star/molecule layer is considerably lower. This is probably again related to the large amount of dust bound in this system. In addition, the SiC dust shell with a spectral feature in the MIDI spectrum at around 11.3 μm could also explain part of the decrease of the relative flux contribution at longer wavelengths.

The Gaussian FWHM diameter, θ_{G} , on the other hand steadily increases from (99 ± 6) mas to (117 ± 4) mas between 8 and 12 μm (Fig. 5b). This is equivalent to an increase from 36 AU to 42 AU and sets the characteristic AMC dust shell radius at 10 μm at a distance of 8.7 ± 0.4 times the photospheric radius. This dust condensation radius is at a similar distance as for the symbiotic O-rich star R Aqr.

The increase of θ_{G} with longer wavelengths is consistent with the results for the FDD + ring model. Figure 5b shows that the outer ring diameter, $\theta_{\text{r,out}}$, increases with increasing wavelength as well. Notable is also that the inner ring diameter, $\theta_{\text{r,in}}$, approaches the FDD diameter at longer wavelengths.

4.4. Wavelength dependence of the diameter

In the following discussion, one has to keep in mind that the compared diameters and diameter ratios (summarized in Table 5) are averaged over the position angle, and are averages over the pulsation phase or may represent only a certain pulsation phase. It is also important to recognize that the FDD diameters obtained with MIDI describe a region whose exact location depends on the flux contribution of all constituents (continuum photosphere, atmospheric molecular layers and nearby dust shells; see next section) as function of wavelength and pulsation phase, and not only the photosphere of the star.

The right hand panels of Figs. 6 and 7 show the obtained FDD diameters in relation to interferometric angular diameter determinations reported by various authors from the visual to the mid-IR (0.6–12 μm). They are obtained by fitting a Gaussian, a uniform disk or a fully limb-darkened disk to the data. A conversion between the models is not performed, since the various diameter determinations depend on the number of visibility measurements and their spatial frequency distribution the authors used to fit their model¹⁴. Information on visual phases and position angles (if applicable) of these observations can be found in Table B.1 (Appendix B).

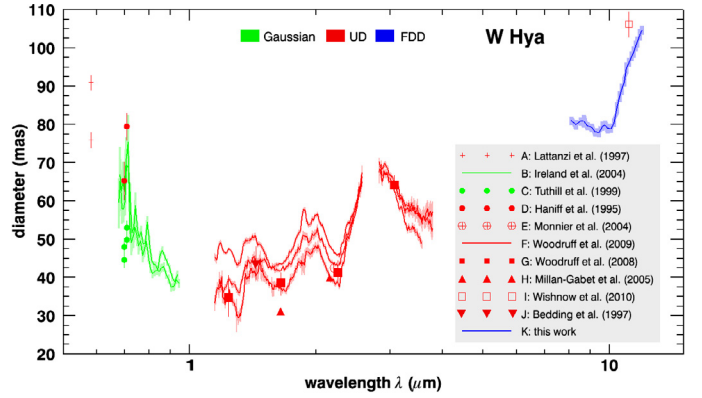


Fig. 7. Same as right hand panels of Fig. 6 but for W Hya (updated version from Paper I, Fig. 9).

The observed apparent diameter changes dramatically within the given wavelength range due to the strong wavelength dependent opacity of the atmospheric constituents (Baschek et al. 1991; Scholz 2001). For the O-rich stars, the measured diameters in the optical are sensitive to TiO bands. The largest variations are around the strongest bands at 712 nm and 670 nm with apparent diameter enlargements of up to a factor of two. Additionally, light scattered by dust (Norris et al. 2012) might also cause a large increase in apparent diameter towards the blue (Ireland et al. 2004a).

In the near-IR, predominantly H₂O and CO in different layers are responsible for the wavelength dependence of the diameter (Hofmann et al. 1998; Jacob et al. 2000). By comparing the observations conducted at *J*, *H*, *K* and *L* band (1.25, 1.65, 2.16 and 3.8 μm , respectively), one can again infer from the right hand panels of Figs. 6 and 7 that also in the near-IR diameters vary by up to a factor of two, and in particular for W Hya that there is a complex diameter dependence on pulsation cycle and pulsation phase (see Woodruff et al. 2009, for a more detailed discussion on this). This has been reported for a large number of AGB stars (e.g. Weiner et al. 2003). Unfortunately, for V Hya, only *H* and *K*-band observations have been published. Diameter determinations for C-stars in these bands are mainly influenced by the presence of molecular shells consisting of C₂H₂, HCN, CN and CO (Gautschy-Loidl et al. 2004; Paladini et al. 2009).

Emission from multiple layers and contamination by nearby continuum emission have a strong influence on determining the true photospheric extension of an AGB star through interferometric measurements. However, a reasonable estimate for the photospheric diameter, θ_{phot} , can be obtained from line free measurements at *K*-band. The UD diameter at *K*-band is approximately 1.2 times the true photospheric diameter (cf. e.g. Millan-Gabet et al. 2005)¹⁵. The estimated θ_{phot} used in this study are listed in Table 5. They were derived by averaging the *K*-band diameters shown in the right hand panels of Figs. 6 and 7 (cf. also Tables 1 and B.1) and dividing them by 1.2 ($\theta_{\text{UD, Kband}}/1.2$). The errors are obtained from the standard deviation.

Maser observations of different molecules give additional diameter constraints. For O-rich stars, SiO and H₂O masers probe inner regions where the molecular layers are present and the first dust formation takes place, while OH masers trace wind regions farther out. Ring diameters for SiO masers, θ_{SiO} , were measured at 43.1 and 42.8 GHz for R Aql, R Aqr and W Hya by

¹⁴ Empirical conversion factors are approximately: FDD \approx 1.15 UD \approx 1.68 FWHM.

¹⁵ However, for C-rich AGB stars, the *K*-band is probably not a good tracer for the true photosphere.

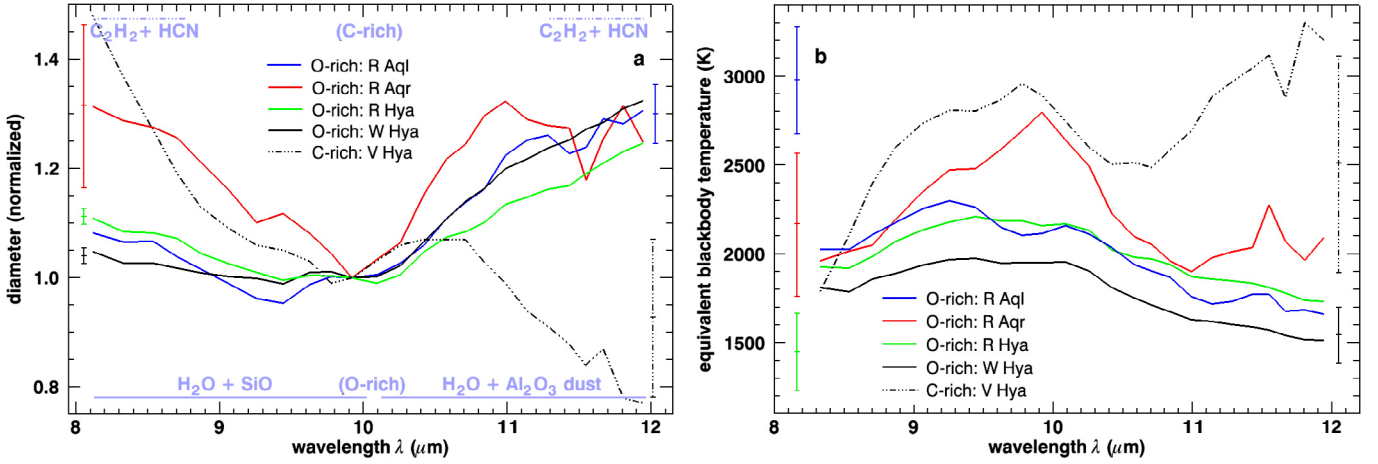


Fig. 8. *Left:* normalized FDD diameters of the AGB stars studied in this work (from the right hand panels of Fig. 4). The diameters are normalized to one at $10\ \mu\text{m}$. Errors are approximately the same for all wavelengths and are given on the side. *Right:* equivalent blackbody temperature of all five AGB stars as function of wavelength (cf. Eq. (2)).

the authors given in Sect. 2. The averages of these diameters are listed in Table 5. A comparison of the location of the SiO masers with the photospheric diameters shows that for all three stars the SiO masers occur at approximately the same distance from the star. The ratios, $\theta_{\text{SiO}}/\theta_{\text{phot}}$, are between 2.2 and 2.5 (Table 5).

Except for R Aqr and V Hya, a similar ratio of 2.2 can be found if the FDD diameters at $10\ \mu\text{m}$ are compared with the photospheric diameters ($\theta_{\text{FDD},10\ \mu\text{m}}/\theta_{\text{phot}}$). The SiO masers are therefore almost co-located with the region characterized by the FDD diameter (cf. next section).

For R Aqr and V Hya, the determined FDD diameters lie closer to the true photometric diameter. This might be again related to the fact that both stars are close binary systems with a large dust content and apparently a closer formation of constituents traced in the N -band.

In addition, it is notable from Fig. 6d that the apparent diameters of R Aqr at $3.1\ \mu\text{m}$ and within the L -band are higher compared to the K and N -band. This might be caused by an extended halo of OH as a result of the ionizing radiation of the compact close companion or the existence of hot circumstellar dust (Tuthill et al. 2000).

Millan-Gabet et al. (2003) obtained for the AMC dust shell in V Hya in the K -band a FWHM diameter, $\theta_{\text{G},2.2\ \mu\text{m}}$, of (35 ± 3) mas (with a flux contribution of 0.63 ± 0.02). This is 3.0 ± 0.3 times smaller compared to the FWHM diameter, $\theta_{\text{G},10\ \mu\text{m}}$, determined at $10\ \mu\text{m}$, and is therefore consistent with the fact that at the N -band colder circumstellar material farther out is probed.

In addition, the AMC dust shell with a FWHM of (113 ± 4) mas (and a flux contribution of 0.85 ± 0.01) determined with MIDI for V Hya is in good agreement with the inner Gaussian dust shell diameter of (98 ± 2) mas (and a flux contribution of the inner and outer shell of 0.78 ± 0.01) found by Townes et al. (2011) at $11.15\ \mu\text{m}$ (narrow bandwidth) with the Infrared Spatial Interferometer (ISI).

It should be also noted that the FDD diameter measured for W Hya of (96.3 ± 1.2) mas at around $11.15\ \mu\text{m}$, tracing the Al_2O_3 dust shell (see next section), is consistent with the average UD diameter of (106.2 ± 3.4) mas of the inner dust shell determined by Wishnow et al. (2010) with ISI. The inner shell flux contribution (including the stellar flux) is with 0.64 ± 0.02 similar to the value of 0.85 ± 0.01 (Table A.4) measured with MIDI as well.

5. Interpretation and discussion

Some of the important results from the last sections are summarized in Table 5 and show that the MIDI observations sample the region above the extended pulsating atmosphere where the molecular layers are present and probably first seed particles for dust formation originate. This study can therefore also help to understand the wind acceleration processes in AGB stars.

The obtained angular diameters as function of wavelength in the N -band are significantly different between the four O-rich stars and the one C-rich star in the sample. R Aql, R Aqr, R Hya and W Hya show a moderate to low diameter decrease from 8 to $10\ \mu\text{m}$ and a strong diameter increase from 10 to $12\ \mu\text{m}$, while the FDD diameter of V Hya essentially decreases from 8 to $12\ \mu\text{m}$. This is again shown in more detail in Fig. 8a. Since different constituents cause these differences in the shapes, both underlying chemistries are discussed separately in the following. General conclusions will be derived for oxygen and carbon-rich stars concerning their molecular shells and dust production. In addition, phase-to-phase variations and asymmetries are investigated.

Possible physical mechanism and chemical processes in the probed region are constrained by the temperature among other things. In particular, the temperature indicates if dust can already condensate at the determined FDD distance. A rough estimate of the equivalent blackbody temperature can be derived from the total flux S_ν (in Jy), the flux ratio ϵ_{FDD} and the diameter θ_{FDD} (in rad) measured with MIDI via

$$T_b = \frac{h\nu}{k_B} \frac{1}{\ln\left(\frac{2h\nu^3}{\epsilon_{\text{FDD}} I_\nu c^2} + 1\right)}, \quad (2)$$

with $I_\nu = 4S_\nu/(10^{26}\pi\theta_{\text{FDD}}^2)$ the spectral brightness, ν the frequency of the observation, h the Planck constant, k_B the Boltzmann constant and c the speed of light. The obtained temperatures are plotted in Fig. 8b for all stars. Due to the use of a simple FDD, giving a diameter which lies between the stellar photosphere and the outer boundary of the close molecular environment, the real extension of the molecular structure is underestimated. Therefore, this approximation may overestimate the temperature of the close molecular environment.

R Aql, R Hya and W Hya show very similar trends with temperatures between 1500 and 2000 K and an error on the order of 200 K. R Aqr and V Hya exhibit a temperature increase

longward of 11 μm , but have considerably higher errors on the order of 500 K. The largest error comes from the uncertainty of the total flux calibration. However, the temperatures between 10 and 12 μm , i.e. where a larger FDD diameter were measured, are sufficiently low for the O-rich stars so that dust particles are able to form (see the following sections).

5.1. Dust and molecular shells in O-rich AGB stars

5.1.1. Spectral features and detectability

The discussion on the spectra in Sect. 4.2 has shown that several molecules are present in the upper atmosphere. In the *N*-band, between 8 and 13 μm , strong pure-rotation lines of H_2O are expected. In addition, SiO exhibits fundamental bands between 8 and 10 μm (e.g. Decin 2000). Such quasi-static, warm and dense molecular layers close to the star, at typically 2–3 photospheric radii (R_{phot}), have been detected in O-rich AGB stars (e.g. Mennesson et al. 2002; Perrin et al. 2004; Ireland et al. 2004d; Woodruff et al. 2004; Fedele et al. 2005) and red supergiant stars (e.g. Perrin et al. 2007). These layers were introduced earlier to explain spectroscopic observations (e.g. Hinkle & Barnes 1979; Tsuji et al. 1997; Yamamura et al. 1999).

Besides the classical amorphous silicate feature at 9.7 μm , spectral dust features in the *N*-band probably originate from amorphous aluminum oxide (Al_2O_3) at around 11.5 μm (Begemann et al. 1997) and spinel (MgAl_2O_4) at around 13 μm (e.g. Posch et al. 1999; Fabian et al. 2001). In particular, amorphous Al_2O_3 provides significant opacity for wavelengths longwards of 10 μm (Koike et al. 1995; Begemann et al. 1997; Posch et al. 1999; Woitke 2006a; Ireland & Scholz 2006; Robinson & Maldoni 2010). In addition, features of crystalline aluminum oxide (corundum, $\alpha\text{-Al}_2\text{O}_3$) at 12.7 μm and several modifications of titanium oxide (e.g. rutile, TiO_2) might be present as well (e.g. Posch et al. 1999, 2002).

It is expected that in O-rich atmospheres oxides condensate first since silicon in silicates have a comparable low electron affinity for oxygen (cf. Stencel et al. 1990) and have therefore in general a lower condensation temperature due to the lower binding energy. The condensation sequence probably starts with TiO_2 before Al_2O_3 , MgAl_2O_4 and $\text{Mg}_{0.1}\text{Fe}_{0.9}\text{O}$ forms (Tielens 1990; Gail & Sedlmayr 1998; Jeong et al. 1999; Blommaert et al. 2006; Lebzelter et al. 2006; Verhoelst et al. 2009). If most of the available high electron affinity metals (primarily Al, Mg, Fe, Ca) have been oxidized, silicates, like forsterite (Mg_2SiO_4) or olivine ($\text{Mg}_{0.8}\text{Fe}_{1.2}\text{SiO}_4$), may condense and will be absorbed onto the seed particles. However, iron-free silicates, nearly transparent at the stellar flux maximum at around 1 μm , can survive at higher temperatures, thus also condensing at small radii (Norris et al. 2012), and are eventually able to trigger the mass-loss through photon scattering (Höfner 2008). Iron-rich silicates, which are not transparent to the stellar radiation, thus absorbing the radiation and heat up, can only exist at larger radii from the star.

Concerning the detectability of the spectral features, two characteristics have to be considered. First, if the mass loss is relatively low the abundance of silicates will remain low (since most of the oxygen is bound in oxides) and the *N*-band will not be dominated by the classical silicate feature (Sogawa & Kozasa 1997). This is also related to the geometrical thickness of the dust shell as described in Egan & Sloan (2001) (referred to as silicate dust sequence): spectra showing the classical narrow 10 μm feature arise from optically thin shells dominated by amorphous silicates while spectra with broad low-contrast emission peaking around 11–12 μm arise from optically and geometrically thin shells composed primarily of alumina dust. This might be also

evidence for different evolutionary stages of O-rich AGB stars (Stencel et al. 1990; Posch et al. 2002; Lebzelter et al. 2006). In earlier evolutionary stages the dust mass-loss rates are low and aluminum oxide dust dominates while at later stages, when effective mass loss has set in, iron-rich silicates will form in large amounts farther away from the star and will dominate the dust spectra (e.g. Woitke 2006a).

The second point concerns the fact that an interferometer always acts as a spatial filter. The measured visibility at a given baseline, and therefore the determined diameter, is a function of the flux contribution (or opacity) of all emitting components at that spatial frequency. In addition, only flux contribution of components within the field of view (FoV) are measurable.

5.1.2. The molecular water shell and close Al_2O_3 dust shell

The observations made in this work, in particular the trend of the apparent FDD diameter as function of wavelength, summarized in Fig. 8a, can be understood qualitatively. If they are additionally compared with the results of Ohnaka et al. (2005) and Wittkowski et al. (2007) for RR Sco and S Ori, respectively, as described in detail for W Hya in Paper I, the following conclusions can be drawn: the overall larger diameter in the mid-IR originates from a warm molecular layer of H_2O , and the apparent gradual increase longward of 10 μm arises most likely from the presence of very close Al_2O_3 dust emitting in this wavelength range (labeled in Fig. 8a).

However, also any other kind of dust compound thermally stable in the very close environment of the star and emitting in the mid-IR could be responsible for this. The iron-rich silicate dust emission does not have any influence since its emitting region is over-resolved at the relevant baselines. The comparison with the models for RR Sco (Ohnaka et al. 2005) and S Ori (Wittkowski et al. 2007) suggests that the partially resolved molecular layers are optically thick and that the nearby Al_2O_3 dust shell is optically and geometrically thin (cf. also Egan & Sloan 2001).

The formation of Al_2O_3 dust at these short distances from the stellar surface would be consistent with the empirical results by e.g. Lorenz-Martins & Pompeia (2000). The interpretation of the apparent diameter increase beyond 10 μm as a result of the presence of an Al_2O_3 dust shell above the molecular water vapor shell is supported by the fact that in R Aql and R Hya the spectra are characterized by broad oxygen-rich dust emission, meaning that oxides are the dominant dust species. In addition, the determined equivalent blackbody temperature (Fig. 8b) indicates as well that the temperatures are low enough that dust composed of titanium and aluminum oxides is stable in the probed region but iron-rich silicate dust not.

For R Aqr, Al_2O_3 grains are probably present as well, but their emission is smeared out by the large amount of amorphous silicate dust in the MIDI FoV mainly emitting in the *N*-band. Extinction effects are probably the reason why the diameter increase longward of 10 μm is first strong but reaches a constant value beyond 11 μm . In addition, the ionizing radiation of the compact companion prevents the formation of large amounts of water vapor, meaning that H_2O cannot sufficiently form from OH and H in the reaction equilibrium. Therefore, the FDD diameter at around 10 μm is only marginally larger than the photospheric diameter.

5.1.3. The contribution of SiO

The only O-rich star in the sample which does not fit very well into the previous interpretation is R Aqr. An overabundance

of SiO (Angeloni et al. 2007) and a strong silicate dust emission could already be inferred from the spectrum and can be attributed to the gravitational attraction of the WD in this symbiotic system. The high abundance of SiO molecules and the gravitational attraction leads to an effective formation of silicate dust close to the star and results in a detectable silicate emission feature in the MIDI spectrum and a high flux contribution of this dust shell.

At shorter wavelengths, the FDD diameter increases due to the presence and increased flux contribution of a SiO molecular shell emitting in the 8 to 9 μm range. This is similar to the apparent enlargement for the RSG star α Orionis in this wavelength regime (Perrin et al. 2007). Even the other O-rich stars show a small diameter enlargement shortwards of 10 μm due to a close SiO molecular shell. A possible relevance of SiO at shorter wavelengths is supported by the occurrence of SiO masers in the region of the water vapor layer and inner boundary of the putative Al_2O_3 dust shell. Since specific physical conditions are necessary in order to exhibit maser emission and these conditions are solely present at a certain distance from the star, the SiO maser shell in R Aqr is also located at a similar distance from the star as for the other O-rich stars in the sample.

5.1.4. The outer silicate dust shell

Since, except for R Aqr, the silicate emission feature is not visible in the MIDI spectra, but seen in the ISO spectra, it can be assumed that there is a surrounding dust shell consistent of mainly the more abundant classical silicates, and that even outside the FoV of MIDI dust formation is still ongoing. From visibility modeling and the FoV some limits on the size of the silicate dust shells were obtained. These lower limits are summarized in Table 5 and show that the amorphous iron-rich silicate dust is located fairly far away from the star.

However, this could be related for R Aql and R Hya to their recent thermal pulse with a short period of enhanced mass loss. Such an outer detached shell may contribute significantly to the total silicate dust emission. In addition, W Hya is known to have a very extended dust shell (Hawkins 1990). Since the mass-loss rates for these three stars are comparably low, the dust shells are not very prominent and contribute only weakly to the total flux in the mid-IR. In contrast, the emission of the silicate dust in the symbiotic system R Aqr contributes substantially to the total flux and the characteristic dust condensation radius could be determined to approximately $7.6 R_{\text{phot}}$.

5.1.5. On the wind formation and mass-loss mechanism

The details of the pulsation-enhanced dust-driven wind mass-loss mechanism in O-rich AGB stars are still under investigation (Höfner et al. 2003; Woitke 2006a; Höfner 2008; Norris et al. 2012). It is believed that the wind is initialized by absorbing the momentum of the outward-directed stellar radiation by dust and re-emitting it in all directions. The required increase of the scale height of the atmosphere is naturally done by the pulsation and the formation of shock fronts, accelerating the gas to reach the location where it is able to condense into dust grains. Since amorphous Al_2O_3 has only a moderate abundance, it can probably not be responsible to initiate the mass-loss (cf. e.g. Woitke 2006a). Al_2O_3 can exist close to the star without inducing mass loss. Unfortunately, the observations presented here cannot give a conclusive answer which dust species are responsible for triggering a high mass loss.

As described in Paper I, the scattering off large iron-free silicate grains, as proposed by Höfner (2008), cannot be verified either, since they were not detected. However, this might be related to their low abundance making their emission smeared out by H_2O , SiO, and Al_2O_3 . The low abundance of iron-free silicates is not critical for driving the wind since a small fraction of Si condensed into Mg_2SiO_4 would be already sufficient (Höfner 2008). Recent observations in scattered light in the near-IR by Norris et al. (2012) support the existence of large iron-free silicates at around 2 stellar radii. Since for this first study no radiative transfer modeling associated to self-consistent dynamic modeling was done, no strong conclusions about the grain mixture and wind formation in the close environment can be drawn.

Not many other wind acceleration mechanisms come in mind. There might be the possibility that small amounts of carbon grains play a role as speculated by Höfner & Andersen (2007), but with the side effect that this would lead to a too high infrared excess. Despite its very low abundance, TiO_2 might have some relevance as well (Posch et al. 2002), but is not detectable with these observations. In this context, it might be interesting to know if scattering on Al_2O_3 grains is important. Also the role of large amounts of water vapor in molecular shells and the radiation pressure on water molecules may need more detailed calculations. In addition, metallic Fe might have some effects as well (McDonald et al. 2010).

It is clear that quantitative modeling is necessary to support the above findings, in particular, if the derived constituents of the close molecular and dust layers (H_2O , SiO, Al_2O_3) can really provide sufficient opacities to explain the observed diameter dependence on wavelength, in particular if Al_2O_3 could cause the apparent diameter increase beyond 10 μm . In order to quantify the results, it will be necessary to apply dynamic atmospheric models of e.g. Ireland & Scholz (Ireland & Scholz 2006; Ireland et al. 2011) or Höfner et al. (see Lebzelter et al. 2010; Sacuto et al. 2011). Even if Al_2O_3 dust is not consistently included in these models so far, and has often to be added ad hoc, this will give more detailed insight into the physical processes at work there.

5.2. Dust and molecular shells in C-rich AGB stars

5.2.1. Spectral features

The study of the oxygen-rich stars in the sample has shown that dense molecular layers, extending to up to 2 photospheric radii, are present in these stars in agreement with findings in other O-rich AGB stars. In contrast, the physical properties of the outer atmosphere of carbon stars and their temporal variations have not yet been probed well. Hydrostatic and dynamic model atmospheres of carbon-rich Miras as well as non-Mira carbon stars fail to explain observed spectra longward of about 5 μm (Jørgensen et al. 2000; Gautschy-Loidl et al. 2004). These models predict very strong absorption due to C_2H_2 and HCN at 7 and 14 μm , but the observed ISO spectra of carbon stars show only weak absorption due to these molecular species. However, Aoki et al. (1998) and Aoki et al. (1999) proposed that emission from extended warm molecular layers, containing C_2H_2 and HCN, may be responsible for the discrepancy between the ISO spectra and the models. Both species are among the most abundant in C-rich atmospheres.

While in the *K* and *H* band the spectrum is contaminated with CO bands, absorption features of C_2H_2 and HCN, as well as emission from SiC at 11.3 μm (Kozasa et al. 1996) and featureless amorphous carbon (AMC) dust, play an important role

in the N -band. In addition, molecules such as silane ($11 \mu\text{m}$) and ammonia ($10.7 \mu\text{m}$) may also provide significant opacities in C-rich stars (Monnier et al. 2000, and references therein).

The only observations with MIDI of classical C-rich stars were conducted by Ohnaka et al. (2007) for V Oph and Sacuto et al. (2011) for R Scl. Ohnaka et al. (2007) modeled V Oph with a dust shell, consisting of AMC (85%) and SiC (15%), with a multi-dimensional Monte Carlo code (Ohnaka et al. 2006), and added a polyatomic molecular layer, consisting of C_2H_2 and HCN, where the opacities of these molecules were calculated with an appropriate band model assuming LTE. Sacuto et al. (2011) applied a self-consistent dynamic model atmosphere to their data (Höfner et al. 2003; Mattsson et al. 2008, 2010). With this model, molecular shells of C_2H_2 and HCN above the stellar photosphere could be probed. However, the dusty environment could not be adequately sampled and a complementary model was applied (a hydrostatic stellar model plus a dust radiative transfer code).

5.2.2. The dust and molecular shells

The FWHM of the Gaussian distribution in V Hya (Fig. 5b) slightly increases by about 20% longwards of $10 \mu\text{m}$ probably due to the presence of SiC dust surrounding the star and emitting in the N -band. The FDD diameter as function of wavelength (Fig. 4h) shows a strong increase of 30% shortward of $9 \mu\text{m}$ which could be related to the presence of molecular layers of C_2H_2 and HCN (see Ohnaka et al. 2007; Sacuto et al. 2011). These molecular layers would then lie at about 2 photospheric radii. Noteworthy, the equivalent blackbody temperature shortward of $9 \mu\text{m}$ gets low enough ($\approx 2000 \text{ K}$, Fig. 8b), supporting the fact that molecules are able to form.

There is, however, a discrepancy of the FDD diameter at wavelengths longward of $11 \mu\text{m}$. With the presence of the mentioned molecular shells one would also expect some increase of the FDD diameter in this wavelength part. There are possibly several reasons for this discrepancy. First of all, the uncertainties in fitting a FDD (determined by the visibilities with spatial frequencies larger than 10 arcsec^{-1}) are much higher in this wavelength regime due to a much higher scatter of the visibilities (cf. Fig. 4h and Table A.4).

This scatter comes from combining observations done at different epochs and position angles. For example, asymmetries are very pronounced in V Hya (cf. Sect. 5.4). The position angles where the observations were made are similar to the position angles of the high velocity wind (cf. Fig. 6g and e.g. Hirano et al. 2004) and temporal fluctuations of the density and emissivity of the massive outflows can be expected.

Therefore, it can only be concluded that SiC and certainly AMC dust is present at the very close circumstellar environment. The dust-driven wind formation scenario in C-rich stars is to a certain amount satisfactorily solved (e.g. Gail & Sedlmayr 1987; Höfner et al. 2003; Gautschy-Loidl et al. 2004; Nowotny et al. 2005; Woitke 2006b; Wachter et al. 2008). Radiation pressure on carbon grains is efficient enough to initiate the wind.

The presence of C_2H_2 and HCN in V Hya cannot be confirmed with certainty due to measurement uncertainties and applying only a simple geometric model. However, also the visibility as function of wavelength (Fig. 3d) is very similar to the ones of V Oph and R Scl (Fig. 1 in Ohnaka et al. 2007; and Fig. 3 in Sacuto et al. 2011, respectively), suggesting the same atmospheric conditions and the presence of those layers.

V Hya shows some similarities to R Aqr except for the underlying chemistry. As for R Aqr, the average N -band

FDD diameter is only about 1.6 times larger than the photospheric diameter, and the dust condensation radius is at about 8 times the photospheric radius. However, it is not expected that the K -band diameter is a good tracer for the true photospheric radius in C-rich stars, and the condensation of AMC dust could occur at smaller radii, i.e. at higher temperatures.

As for the oxygen-rich stars, it is necessary to use dynamic model atmospheres (e.g. Sacuto et al. 2011), computed with stellar parameters corresponding to V Hya, for a better understanding of the physical processes responsible for the molecule and dust formation close to the star.

5.3. Dynamic behavior of the close environment

As a result of the intrinsic pulsation, mid-IR flux variations on the order of 20%, with a phase offset of about 0.15, were detected in this study except for R Aql (Sect. 4.1). This section investigates how this relates to changes of the apparent angular sizes and flux contributions of the close stellar atmosphere, and how this influences or triggers the dust formation and mass loss.

5.3.1. Size and flux variations

Cycle-to-cycle variations were studied for all oxygen-rich stars for the phase ranges given in the left hand panels of Fig. 1. For this, the best geometrical model was fitted to the visibilities with the relative fluxes fixed to the value obtained for the full data set (cf. Fig. 5a). No cycle-to-cycle investigation could be done for V Hya due to the fact that observations are not repeated at the same phase in consecutive cycles.

However, reliable cycle-to-cycle variations could be obtained for R Hya and W Hya (for W Hya see Paper I). Both stars show a maximum variation of the N -band averaged and normalized FDD diameter, $\bar{\theta}_{\text{FDD}}$ (normalized in respect to the full data set), on the order of $(5 \pm 4)\%$, thus much lower than phase-to-phase variations as shown below. This verifies that the folding of consecutive pulsation cycles into one cycle is an acceptable assumption for the following phase-to-phase analysis. For R Aql and R Aqr, the uncertainties are higher and no reliable trend could be found.

For studying the phase-to-phase behavior of the diameter and the relative flux contribution of the FDD, the pulsation phase of each star is divided into several phase bins as shown in the right hand panels of Fig. 1 and listed in Table 6. As for the cycle-to-cycle investigation, the best geometrical model is then fitted to the data within each bin. For the fit to R Aqr, the Gaussian FWHM is fixed to the value obtained for the full data set (cf. Fig. 5b). No reliable fits could be obtained for V Hya because of a very unfavorable spatial frequency coverage. In several phase bins the FDD diameter could not be fitted or the uncertainties were too high due to potential asymmetries and unknown cycle-to-cycle variations (cf. Sect. 5.4) even after reducing the number of phase bins. Therefore, V Hya is not considered in the following discussion.

For a simple comparison between phase bins, the obtained FDD diameters, θ_{FDD} (cf. right hand panels of Fig. 4), and relative flux contributions, ϵ_{FDD} , are averaged over the N -band wavelength regime ($8\text{--}12 \mu\text{m}$). Since the chromatic trend of θ_{FDD} and ϵ_{FDD} does not change considerably between phases, and in general other error sources are more prominent (see below), this approach can be appropriate for a first investigation. The similar chromatic trend found for each subsequent phase bin indicates also that the probed different layers behave similarly as function of pulsation phase.

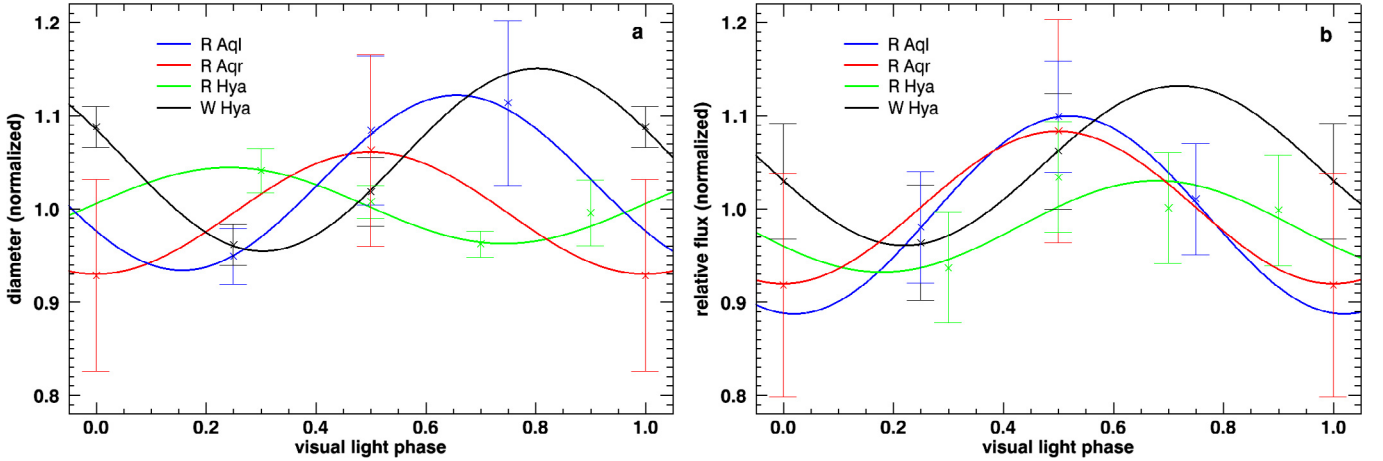


Fig. 9. Phase-to-phase variations of all oxygen-rich stars in the sample. The *left panel* shows the normalized FDD diameter as function of visual light phase and the *right panel* the normalized relative flux contribution of the FDD as function of visual light phase (normalized in respect to the full data set). It was not possible to obtain reliable results for the C-rich star V Hya.

Table 6. Phase-to-phase variations.

Phase bin ^a	Phase range	No. of obs.	Norm. ^b FDD diameter	Norm. ^b flux contribution
R Aql:				
1	0.875–0.125	8	– ^c	– ^c
2	0.125–0.375	9	0.95 ± 0.03	0.98 ± 0.06
3	0.375–0.625	9	1.08 ± 0.08	1.10 ± 0.06
4	0.625–0.875	6	1.11 ± 0.09	1.01 ± 0.06
R Aqr:				
1	0.750–0.250	12	0.93 ± 0.10	0.92 ± 0.12
2	0.250–0.750	14	1.06 ± 0.10	1.08 ± 0.12
R Hya:				
1	0.000–0.200	0	–	–
2	0.200–0.400	14	1.04 ± 0.02	0.94 ± 0.06
3	0.400–0.600	27	1.01 ± 0.02	1.04 ± 0.06
4	0.600–0.800	20	0.96 ± 0.01	1.00 ± 0.06
5	0.800–0.000	3	1.00 ± 0.04	1.00 ± 0.06
W Hya:				
1	0.875–0.125	23	1.09 ± 0.02	1.03 ± 0.06
2	0.125–0.375	42	0.96 ± 0.02	0.96 ± 0.06
3	0.375–0.625	10	1.02 ± 0.04	1.06 ± 0.06
4	0.625–0.875	0	–	–

Notes. ^(a) Cf. right hand panels of Fig. 1. ^(b) Normalized in respect to the full data set. ^(c) No reliable fit could be obtained.

The *N*-band averaged diameters, $\bar{\theta}$, and relative flux contributions, $\bar{\epsilon}$, are plotted as function of visual phase in Fig. 9, and are listed in Table 6 in comparison to the full data set values. The errors are in general relatively high because of the low number of visibility points used for these fits. In addition, the large phase binning reduces the true amplitude of the variation somewhat. It should be also noted that for R Aqr only two phase bins are used and that there are no fit results and observations available for R Aql and R Hya at visual maximum, respectively.

Except for R Hya, the FDD diameter is largest at or after the visual minimum (Fig. 9a and Table 5). The increase, $\bar{\theta}_{\text{FDD,max}}/\bar{\theta}_{\text{FDD,min}}$, between minimum and maximum is on the order of 15%. While the layer representing the photosphere in a Mira variable is in the mid-infrared largest near the stellar luminosity maximum (Weiner et al. 2003), the more outer pulsating layers reach their maximum extension with an increasing phase delay. This is in agreement with the movement of a mass-shell at

around 2 stellar radii as modeled by Nowotny et al. (2010, their Figs. 1 and 2) for a carbon star. However, for R Hya a different trend was found making this interpretation uncertain. The large error bars also reflecting this uncertainty.

In contrast, the variation of the relative flux contribution as function of visual light phase shows a more consistent behavior. The flux contribution is lower at around visual maximum than at around visual minimum (Fig. 9b and Table 5). The increase, $\bar{\epsilon}_{\text{FDD,max}}/\bar{\epsilon}_{\text{FDD,min}}$, between minimum and maximum is on the order of 10 to 15%, but also with large uncertainties and therefore not strongly significant.

The location of the outer silicate dust shell as function of visual phase was studied for the symbiotic system R Aqr. For this the Gaussian FWHM was not fixed to the full data set value. At visual minimum, the averaged Gaussian FWHM, $\bar{\theta}_{\text{G}}$, was larger than at visual maximum by about $(24 \pm 19)\%$.

5.3.2. Dust and wind formation

Taking the above findings at face value, one infers that new dust forms around or after the visual minimum when the pulsating layer at around 2 photospheric radii reaches its maximum extension. Since a higher relative flux contribution of the FDD around the visual minimum is approximately canceled out by the lower absolute flux, the temperature in this region will be lower too.

Calculating the equivalent blackbody temperature according to Eq. (2), the temperatures around the visual minimum are on average (150 ± 100) K lower and at around the visual maximum on average (150 ± 100) K higher than the temperatures averaged over the cycles shown in the right panel of Fig. 8. This means that in particular in the 11–12 μm range, where the putative Al_2O_3 dust shell is traced, the temperatures around the visual minimum are getting as low as the condensation temperature of Al_2O_3 of approximately 1400 K, showing that new Al_2O_3 dust could form.

The phase behavior would also be consistent with the theoretical predictions of Ireland & Scholz (2006). In their model, the largest rate of grain growth occurs between phases 0.3 and 0.7, similar to what is predicted for carbon-rich stars (cf. Fig. 2 in Nowotny et al. 2010).

While the observations made in this work show that Al_2O_3 dust might newly form around the visual minimum, it cannot be determined conclusively how this relates to the acceleration of the wind and the mass-loss rate. As mentioned before and in

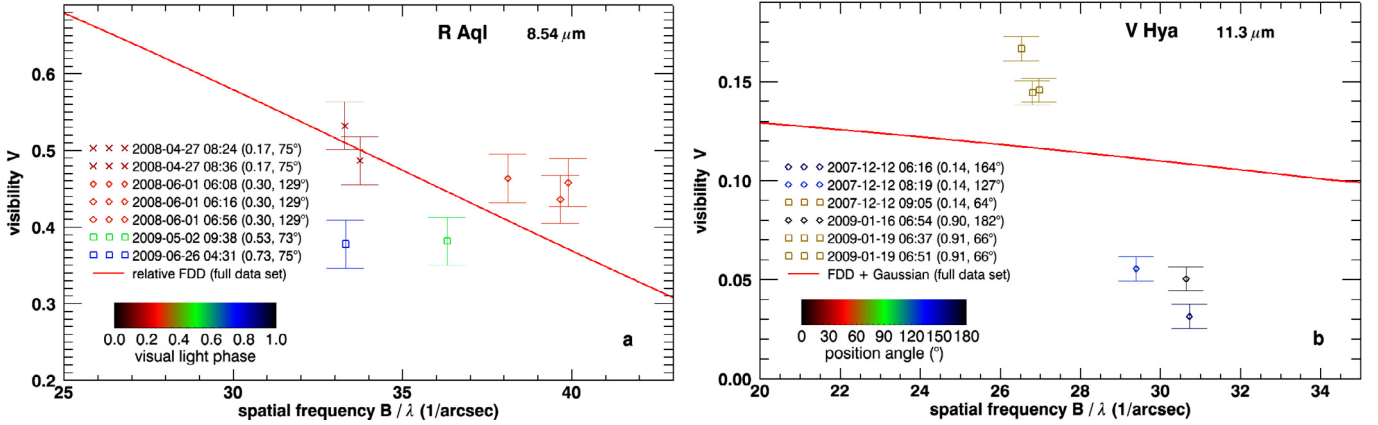


Fig. 10. Selected visibility measurements to investigate the asymmetries in R Aql (*left*) and V Hya (*right*). The visual light phase and position angle are given in parenthesis for each data point. See text for more details.

Paper I, Al_2O_3 can exist in the upper atmosphere without being a wind-driver. No conclusion can be given concerning the relevance of micrometer-sized iron-free silicates for the wind formation since this needs the use of radiative transfer modeling associated to self-consistent dynamic modeling taking opacities of different realistic chemical compounds into account. However, it can be speculated that the relevant constituents that are responsible for the wind acceleration are formed along with Al_2O_3 .

5.4. Asymmetries

The good uv-coverage for R Hya and W Hya, shown in the left hand panels of Fig. 6 and Fig. 1 in Paper I, makes it possible to directly fit a elliptical FDD to the data. For R Aql, R Aqr and V Hya, the uv-planes are not filled well. Departure from spherical symmetry was here studied by simply comparing visibility measurements at different position angles taken closely in time and with similar projected baselines. Differential phases were not used but will be investigated in more detail in future studies.

As described in detail in Paper I, W Hya shows a small elongation in the mid-IR. The position angle (PA) and axis ratio of an elliptical FDD were determined to $(11 \pm 20)^\circ$ and 0.87 ± 0.07 , respectively. The asymmetry was explained by a possible enhanced dust concentration along an N-S axis. As for W Hya, an elliptical FDD was fitted to the full data set of R Hya, but also to subsets of the full data set to test for time dependencies. However, no departure from spherical symmetry could be revealed within the measurement uncertainties. Any intrinsic deviation from sphericity is less than 10%.

While for W Hya contradictory position angles were found in the literature, the non-detection of an asymmetry in R Hya is consistent with the results of Ireland et al. (2004a) and Monnier et al. (2004). Both authors did not find any departures from symmetry within the measurement errors in the optical and near-IR (680–940 nm and 2.26 μm , respectively).

Because both stars have similar intrinsic properties but a different asymmetric appearance, they are excellent targets for studying the origin and formation of asymmetries in more detail, e.g. if they are related to different evolutionary phases. By comparing both stars, it could be investigated why W Hya shows an asymmetry and R Hya not, and in particular why in W Hya asymmetries appear different at different scales and how they are connected.

Figure 10 shows selected visibility measurements for R Aql and V Hya to investigate their asymmetry. In order to do so,

groups of points with similar spatial frequencies are compared with the best model fit to the full data set serving as reference¹⁶. In R Aql, it can be seen that the visibilities measured at visual light phase 0.17 with a PA of 75° (crosses) lie on the full data set fit as well as basically also the measurements taken at an almost perpendicular PA of 129° (diamonds). Therefore, it can be concluded that there is no departure from symmetry in the close vicinity of the star at around 2.2 photospheric radii within the measurement uncertainties. In contrast, it can be inferred that at a distinct different visual light phase the visibilities (squares) are smaller and therefore probing a region appearing larger (cf. Sect. 5.3.1).

In V Hya an opposite effect can be seen. Points with a PA around 65° (squares) have a higher visibility than expected for a circular FDD and points with PAs from 130 to 180° a lower visibility. This seems not be related to the pulsation since at different light phases but similar PAs the visibilities are similar. This means that a strong asymmetry already sets in in the very close stellar environment at less than 2 photospheric radii with an elongation along a north-south direction, therefore, a similar orientation as found by e.g. Tsuji et al. (1988); Kahane et al. (1988, 1996); Sahai et al. (2003) and particular also by Lagadec et al. (2005) in the mid-infrared (cf. Sect. 2.5). In contrast to R Aql, where the symmetry is seen over the whole N-band wavelength regime, the asymmetry in V Hya appears stronger at longer wavelengths (10 to 12 μm).

For R Aqr, only one set of visibilities could be compared. In the shorter wavelength regime (8 to 10 μm), the visibilities taken at 2007-10-07 05:54 at a PA of 79° (phase 0.87, $B_{\text{proj}} = 40.3$ m) are larger than the ones taken at 2007-10-07 01:16 (phase 0.87, $B_{\text{proj}} = 41.3$ m) at a PA of 59° (cf. Table C.2). This is a hint that the distribution of SiO strongly deviates from spherical symmetry. From this investigation it follows that three out of the five stars observed show asymmetries.

6. Summary

Five AGB stars, namely R Aql, R Aqr, R Hya, W Hya, and V Hya, were observed over a period of nearly three years

¹⁶ Note that a comparably large phase and spatial frequency range is used. This allows a more reliable analysis due to comparing groups of points instead of only single measurements with large errors. However, it can not be excluded that this is biased by the fact that different spatial frequencies probe different parts of the envelope. Therefore, only a qualitative analysis is given here.

covering several pulsation cycles. All stars were for the first time monitored in the mid-IR (8–13 μm) with the interferometric instrument MIDI. These high-resolution observations are sensitive to the structure of the stellar atmosphere, consisting of the continuum photosphere and overlying molecular layers, as well as to the properties of the dust shell.

The results and conclusions can be summarized as follows:

- Except for R Aql, a periodic flux variation is found in the *N*-band. The typical semi-amplitudes are on the order of 20% to 30% for the Miras and 10% for the SR/Mira variable W Hya. The amplitude is probably also related to the dust content in the system. The mid-IR maximum occurs always after the visual maximum at visual phase 0.15 ± 0.05 .
- In the MIDI spectrum of R Aqr, the silicate dust emission feature could be clearly identified, while it was not present in the spectra of the other O-rich stars. This has been attributed to the field-of-view of MIDI smaller than the one of ISO. The expected SiC dust emission feature is detected in the MIDI spectrum of the carbon star V Hya.
- The obtained visibility data were best fitted by a fully limb-darkened disk (FDD), representing the central star and the close atmospheric layers, and a spherical Gaussian distribution, representing the extended dusty environment.
- The trend of the FDD diameter as function of wavelength is similar for all O-rich stars in the sample. The apparent size is almost constant between 8 and 10 μm (21.3 ± 2.0 mas, 20.9 ± 3.5 mas, 46.6 ± 0.6 mas, and 79.0 ± 1.2 mas, for R Aql, R Aqr, R Hya, and W Hya, respectively) and gradually increases at wavelengths longer than 10 μm . The enlargement is for all stars between 25% and 30%. In contrast, the relative flux contribution of the FDD decreases, reflecting the increased flux contribution from the surrounding dust shell.
- The measured FDD diameters at 10 μm are about 2.2 times larger than the photospheric diameters (except for R Aqr and V Hya). This ratio is consistent with observations of other AGB stars. The smaller ratio of about 1.6 for R Aqr and V Hya can be understood from the gravitational interaction with a compact companion.
- The obtained diameter trends for the O-rich stars are compared with the findings of [Ohnaka et al. \(2005\)](#) and [Wittkowski et al. \(2007\)](#) for RR Sco and S Ori, respectively. It can be concluded that the overall larger diameter in the mid-IR originates from a warm molecular layer of H_2O , and the gradual increase longward of 10 μm can be most likely attributed to the contribution of a spatially resolved close Al_2O_3 dust shell. A contribution of SiO shortward of 10 μm can be seen as well, maybe except for W Hya.
- These observations of a larger sample of stars than available before confirm previous results, and emphasize the need for dynamic models able to treat the formation of dust in a self-consistent way. In particular, the close dust shell composed of Al_2O_3 well below the distance at which the iron-rich silicate dust shell is traced, could now be revealed for a significant number of stars.
- A comparison with available SiO maser ring diameters shows that the SiO maser emission is co-located with the region probed with MIDI.
- For the carbon rich star V Hya it can be concluded that SiC and AMC dust is present in the very close circumstellar environment. The chromatic shape of the Gaussian FWHM shows an increase around the SiC feature (11.3 μm). The apparent FDD diameter as function of wavelength shows a

strong increase of more than 30% shortward of 9 μm , which could be a hint that close molecular layers consisting of C_2H_2 and HCN at about 2 photospheric radii are probed. However, a simultaneous increase at wavelengths longward of 11 μm could not be detected, but this might be related to large fitting uncertainties.

- It is found that the iron-rich silicate dust shells are located fairly far away from the star, at radii larger than 30 times the photospheric radius. Only the silicate dust shell of R Aqr is located closer to the star at around 8 photospheric radii, which is most probably related to the interaction with a close companion.
- Phase-to-phase variations of the FDD diameter and the relative flux contribution of the O-rich stars are on the order of 15% and 10–15%, respectively. It was found that the relative flux contribution was highest at around visual minimum, while there was no clear behavior detectable for the FDD diameter as function of visual light phase. Due to the large uncertainties this is not strongly significant and no firm conclusions can be drawn concerning the mass-loss mechanism. Nevertheless, one can speculate that new dust forms around visual minimum.
- Maximal diameter changes due to cycle-to-cycle variations are on the order of 6%, and are therefore lower than phase-to-phase variations. This could only be determined for R Hya and W Hya.
- The close environment geometry could be investigated for all stars. R Aql and R Hya do not show any deviation from sphericity, while R Aqr, W Hya and V Hya do.

Most of the proposed goals could be accomplished. However, a few items remain open. First, no clear connection could be established between the dust condensation and wind formation. Second, the size of the iron-rich silicate dust shell could not be satisfactorily constrained for 3 of the 4 oxygen-rich stars due to the lack of observations at short baselines. Third, the pulsation phase coverage allowed only for some of the stars an analysis of the apparent diameter with time.

The majority of the above conclusions rely on fits of a relatively simple FDD to the observational data. However, this can only be an approximation, even if this model represents the data quite well. In order to obtain a more meaningful diameter and the exact composition, it is therefore necessary to compare with hydrodynamic model atmospheres of e.g. Ireland & Scholz ([Ireland & Scholz 2006](#); [Ireland et al. 2011](#)) and Höfner et al. (see [Lebzelter et al. 2010](#); [Sacuto et al. 2011](#)).

Another big reward can be gained if these results can be combined with kinematic information. Complementary high-resolution radio and mm observations, tracing the relevant constituents and sampling the dust formation zone probed with MIDI, are therefore necessary.

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Appendix A: Visibility model fit results for R Aql, R Aqr, R Hya and V Hya**Table A.1.** R Aql: circular fully limb-darkened disk (FDD) and circular uniform disk (UD).

λ (μm)	ΔV^a	Circular FDD			Circular UD			
		θ_{FDD} (mas)	Flux ϵ_{FDD}	$\chi_r^{2,b}$	θ_{UD} (mas)	Flux ϵ_{UD}	$\chi_r^{2,b}$	
8.12	0.034	23.1 \pm 0.9	0.99 \pm 0.04	4.7	20.4 \pm 0.8	0.99 \pm 0.04	4.7	
8.33	0.033	22.7 \pm 0.9	0.97 \pm 0.04	5.0	20.1 \pm 0.9	0.97 \pm 0.03	5.1	
8.54	0.031	22.7 \pm 0.8	0.95 \pm 0.04	3.8	20.1 \pm 0.7	0.95 \pm 0.03	3.8	
8.71	0.031	22.2 \pm 0.9	0.93 \pm 0.03	3.5	19.6 \pm 0.7	0.93 \pm 0.03	3.5	
8.87	0.031	21.6 \pm 0.9	0.92 \pm 0.03	3.5	19.2 \pm 0.8	0.92 \pm 0.03	3.5	
9.07	0.029	21.1 \pm 1.0	0.88 \pm 0.03	4.2	18.7 \pm 0.9	0.88 \pm 0.03	4.2	
9.26	0.029	20.5 \pm 1.2	0.84 \pm 0.03	5.0	18.2 \pm 1.1	0.84 \pm 0.03	5.0	
9.45	0.026	20.3 \pm 1.3	0.80 \pm 0.03	6.7	18.1 \pm 1.2	0.80 \pm 0.03	6.7	
9.63	0.028	21.1 \pm 1.3	0.78 \pm 0.03	5.3	18.7 \pm 1.1	0.78 \pm 0.03	5.3	
9.78	0.027	21.4 \pm 1.5	0.78 \pm 0.03	6.9	19.0 \pm 1.4	0.78 \pm 0.03	6.9	
9.92	0.027	21.3 \pm 1.5	0.77 \pm 0.03	6.5	18.9 \pm 1.3	0.77 \pm 0.03	6.5	
10.09	0.027	21.4 \pm 1.6	0.78 \pm 0.03	7.5	19.0 \pm 1.4	0.78 \pm 0.03	7.5	
10.26	0.026	21.9 \pm 1.6	0.78 \pm 0.03	7.7	19.4 \pm 1.4	0.78 \pm 0.03	7.7	
10.42	0.029	22.6 \pm 1.6	0.78 \pm 0.03	6.0	20.1 \pm 1.5	0.78 \pm 0.03	6.0	
10.58	0.031	23.6 \pm 1.4	0.79 \pm 0.03	4.8	21.0 \pm 1.3	0.79 \pm 0.03	5.8	
10.71	0.030	24.2 \pm 1.5	0.80 \pm 0.03	5.3	21.5 \pm 1.3	0.79 \pm 0.03	5.3	
10.84	0.030	24.8 \pm 1.4	0.80 \pm 0.03	4.6	22.0 \pm 1.3	0.80 \pm 0.03	4.6	
10.99	0.030	26.1 \pm 1.4	0.81 \pm 0.03	4.6	23.2 \pm 1.3	0.81 \pm 0.03	4.6	
11.14	0.027	26.7 \pm 1.4	0.82 \pm 0.03	5.2	23.7 \pm 1.2	0.82 \pm 0.03	5.2	
11.29	0.031	26.9 \pm 1.3	0.83 \pm 0.03	3.8	23.8 \pm 1.1	0.82 \pm 0.03	3.8	
11.43	0.030	26.2 \pm 1.5	0.81 \pm 0.03	4.3	23.2 \pm 1.2	0.81 \pm 0.03	4.4	
11.55	0.029	26.4 \pm 1.5	0.81 \pm 0.03	4.9	23.5 \pm 1.3	0.81 \pm 0.03	5.0	
11.67	0.026	27.5 \pm 1.4	0.83 \pm 0.03	5.6	24.4 \pm 1.2	0.83 \pm 0.03	5.6	
11.81	0.029	27.3 \pm 1.4	0.83 \pm 0.03	4.3	24.2 \pm 1.2	0.83 \pm 0.03	4.4	
11.95	0.029	27.9 \pm 1.4	0.84 \pm 0.03	4.2	24.7 \pm 1.2	0.84 \pm 0.03	4.2	

Table A.2. R Aqr: circular fully limb-darkened disk (FDD) + circular Gaussian (G) and circular uniform disk (UD) + circular Gaussian (G).

λ (μm)	ΔV^a	Circular FDD + circular Gaussian				Circular UD + circular Gaussian			
		θ_{FDD} (mas)	Flux ϵ_{FDD}	θ_{G} (mas)	$\chi_r^{2,b}$	θ_{UD} (mas)	Flux ϵ_{UD}	θ_{G} (mas)	$\chi_r^{2,b}$
8.12	0.025	27.4 \pm 2.5	0.57 \pm 0.03	78 \pm 12	4.9	24.2 \pm 2.0	0.56 \pm 0.03	78 \pm 11	4.9
8.33	0.026	26.8 \pm 2.5	0.56 \pm 0.09	81 \pm 10	4.9	23.7 \pm 2.0	0.55 \pm 0.09	80 \pm 11	4.8
8.54	0.025	26.6 \pm 2.5	0.55 \pm 0.09	85 \pm 11	5.4	23.5 \pm 2.0	0.55 \pm 0.03	84 \pm 12	5.4
8.71	0.024	26.2 \pm 2.0	0.55 \pm 0.03	90 \pm 12	4.7	23.2 \pm 2.0	0.55 \pm 0.03	90 \pm 13	4.7
8.87	0.022	25.2 \pm 2.0	0.54 \pm 0.03	94 \pm 11	5.1	22.4 \pm 2.0	0.53 \pm 0.03	94 \pm 12	5.1
9.07	0.023	24.2 \pm 2.5	0.50 \pm 0.03	97 \pm 11	4.4	21.5 \pm 2.0	0.50 \pm 0.03	97 \pm 11	4.4
9.26	0.021	22.9 \pm 3.0	0.45 \pm 0.03	102 \pm 11	5.4	20.4 \pm 2.5	0.45 \pm 0.03	101 \pm 10	5.3
9.45	0.023	23.3 \pm 3.5	0.42 \pm 0.03	104 \pm 10	4.4	20.7 \pm 2.5	0.42 \pm 0.03	104 \pm 10	4.4
9.63	0.025	22.5 \pm 3.5	0.38 \pm 0.03	104 \pm 8	3.6	20.0 \pm 3.0	0.38 \pm 0.03	104 \pm 9	3.6
9.78	0.020	21.8 \pm 3.5	0.36 \pm 0.03	104 \pm 7	4.6	19.4 \pm 3.5	0.36 \pm 0.03	104 \pm 7	4.6
9.92	0.019	20.9 \pm 3.5	0.35 \pm 0.03	105 \pm 8	4.8	18.6 \pm 3.0	0.35 \pm 0.03	105 \pm 8	4.8
10.09	0.017	21.5 \pm 3.5	0.35 \pm 0.03	106 \pm 7	5.3	19.2 \pm 3.0	0.35 \pm 0.03	106 \pm 7	5.3
10.26	0.017	22.2 \pm 3.5	0.34 \pm 0.03	105 \pm 7	5.8	19.7 \pm 3.0	0.34 \pm 0.03	105 \pm 7	5.8
10.42	0.018	24.0 \pm 3.5	0.34 \pm 0.03	105 \pm 6	4.9	21.4 \pm 3.5	0.34 \pm 0.03	105 \pm 7	4.9
10.58	0.021	25.4 \pm 3.5	0.35 \pm 0.03	106 \pm 7	3.1	22.5 \pm 3.0	0.35 \pm 0.03	106 \pm 6	3.1
10.71	0.019	25.9 \pm 3.5	0.36 \pm 0.03	105 \pm 6	4.3	23.0 \pm 3.0	0.36 \pm 0.03	105 \pm 6	4.3
10.84	0.020	27.0 \pm 3.5	0.36 \pm 0.03	104 \pm 7	3.8	24.0 \pm 3.0	0.36 \pm 0.03	104 \pm 6	3.9
10.99	0.019	27.6 \pm 3.0	0.37 \pm 0.03	104 \pm 6	4.1	24.5 \pm 3.0	0.37 \pm 0.03	104 \pm 6	4.1
11.14	0.022	26.9 \pm 3.5	0.37 \pm 0.03	104 \pm 7	2.8	23.9 \pm 3.0	0.37 \pm 0.03	104 \pm 6	2.8
11.29	0.018	26.6 \pm 3.5	0.37 \pm 0.03	103 \pm 6	5.0	23.6 \pm 3.5	0.37 \pm 0.03	103 \pm 7	5.0
11.43	0.022	26.6 \pm 4.0	0.37 \pm 0.03	101 \pm 7	3.7	23.6 \pm 3.5	0.37 \pm 0.03	101 \pm 6	3.7
11.55	0.022	24.6 \pm 4.5	0.37 \pm 0.03	102 \pm 7	4.0	21.8 \pm 4.5	0.37 \pm 0.03	101 \pm 7	4.0
11.67	0.022	26.1 \pm 4.5	0.39 \pm 0.03	101 \pm 7	4.2	23.2 \pm 4.0	0.38 \pm 0.03	101 \pm 7	4.2
11.81	0.029	27.4 \pm 4.5	0.40 \pm 0.03	101 \pm 7	2.7	24.3 \pm 4.0	0.40 \pm 0.03	100 \pm 8	2.7
11.95	0.032	26.0 \pm 5.5	0.39 \pm 0.03	99 \pm 7	2.8	23.1 \pm 5.0	0.39 \pm 0.03	99 \pm 7	2.8

Notes. ^(a) Mean visibility error used for the corresponding wavelength bin (cf. Sect. 4.3); ^(b) reduced chi square.

Table A.3. R Hya: circular fully limb-darkened disk (FDD) and circular uniform disk (UD).

λ (μm)	ΔV^a	Circular FDD			Circular UD		
		θ_{FDD} (mas)	Flux ϵ_{FDD}	$\chi_r^{2,b}$	θ_{UD} (mas)	Flux ϵ_{UD}	$\chi_r^{2,b}$
8.12	0.012	51.6 \pm 1.2	0.92 \pm 0.03	13	45.6 \pm 1.2	0.91 \pm 0.02	19
8.33	0.012	50.5 \pm 0.7	0.92 \pm 0.02	13	43.4 \pm 1.2	0.89 \pm 0.03	18
8.54	0.012	50.4 \pm 0.8	0.92 \pm 0.02	14	43.2 \pm 0.8	0.89 \pm 0.02	19
8.71	0.011	49.9 \pm 0.7	0.94 \pm 0.01	13	42.9 \pm 0.6	0.91 \pm 0.02	18
8.87	0.011	48.6 \pm 0.8	0.93 \pm 0.02	12	42.1 \pm 0.6	0.91 \pm 0.02	17
9.07	0.012	47.7 \pm 0.5	0.92 \pm 0.01	10	41.1 \pm 0.6	0.90 \pm 0.01	13
9.26	0.011	47.0 \pm 0.5	0.90 \pm 0.01	9	40.5 \pm 0.6	0.88 \pm 0.01	11
9.45	0.013	46.4 \pm 0.6	0.88 \pm 0.01	7	40.3 \pm 0.6	0.86 \pm 0.02	9
9.63	0.011	46.8 \pm 0.6	0.86 \pm 0.01	9	40.3 \pm 0.6	0.84 \pm 0.01	11
9.78	0.011	46.7 \pm 0.5	0.85 \pm 0.01	9	40.3 \pm 0.6	0.83 \pm 0.01	11
9.92	0.011	46.6 \pm 0.6	0.84 \pm 0.01	8	40.3 \pm 0.6	0.82 \pm 0.01	10
10.09	0.011	46.1 \pm 0.5	0.82 \pm 0.01	8	40.3 \pm 0.6	0.81 \pm 0.01	10
10.26	0.011	46.8 \pm 0.5	0.82 \pm 0.01	9	40.9 \pm 0.8	0.81 \pm 0.01	11
10.42	0.009	48.8 \pm 0.8	0.81 \pm 0.01	14	42.2 \pm 0.6	0.80 \pm 0.01	18
10.58	0.009	50.0 \pm 0.6	0.81 \pm 0.01	16	43.2 \pm 0.6	0.79 \pm 0.01	21
10.71	0.010	50.5 \pm 0.7	0.80 \pm 0.01	16	43.7 \pm 0.6	0.79 \pm 0.01	20
10.84	0.009	51.3 \pm 0.8	0.80 \pm 0.01	19	44.3 \pm 0.6	0.78 \pm 0.01	24
10.99	0.008	52.8 \pm 0.7	0.79 \pm 0.01	21	45.5 \pm 0.6	0.77 \pm 0.01	28
11.14	0.008	53.4 \pm 0.7	0.78 \pm 0.01	21	46.0 \pm 0.8	0.77 \pm 0.02	27
11.29	0.010	54.1 \pm 0.7	0.79 \pm 0.01	16	46.6 \pm 0.8	0.77 \pm 0.01	21
11.43	0.011	54.4 \pm 0.8	0.79 \pm 0.01	13	46.9 \pm 0.8	0.77 \pm 0.01	16
11.55	0.011	55.5 \pm 0.8	0.80 \pm 0.01	14	47.8 \pm 0.8	0.78 \pm 0.01	17
11.67	0.011	56.3 \pm 0.8	0.80 \pm 0.02	15	48.5 \pm 1.0	0.78 \pm 0.02	19
11.81	0.008	57.3 \pm 0.8	0.80 \pm 0.01	29	49.3 \pm 1.2	0.78 \pm 0.02	37
11.95	0.007	58.0 \pm 0.8	0.81 \pm 0.02	40	49.9 \pm 1.0	0.79 \pm 0.02	51

Table A.4. V Hya: circular fully limb-darkened disk (FDD) + circular Gaussian (G) and circular fully limb-darkened disk (FDD) + circular uniform ring (R).

λ (μm)	ΔV^a	Circular FDD + circular Gaussian				Circular FDD + circular ring				
		θ_{FDD} (mas)	Flux ϵ_{FDD}	θ_{G} (mas)	$\chi_r^{2,b}$	θ_{FDD} (mas)	Flux ϵ_{FDD}	$\theta_{\text{R,in}}$ (mas)	$\theta_{\text{R,out}}$ (mas)	$\chi_r^{2,b}$
8.12	0.011	28.5 \pm 2.0	0.22 \pm 0.03	99 \pm 6	8	35.3 \pm 2.0	0.32 \pm 0.04	51 \pm 4	124 \pm 6	14
8.33	0.011	26.5 \pm 2.0	0.25 \pm 0.03	100 \pm 7	8	31.9 \pm 2.0	0.33 \pm 0.04	49 \pm 4	125 \pm 6	12
8.54	0.012	24.5 \pm 2.0	0.26 \pm 0.03	101 \pm 5	8	30.0 \pm 2.0	0.34 \pm 0.04	50 \pm 4	127 \pm 6	12
8.71	0.011	22.9 \pm 2.0	0.27 \pm 0.01	101 \pm 5	9	28.7 \pm 2.0	0.35 \pm 0.04	51 \pm 4	129 \pm 6	12
8.87	0.011	21.8 \pm 2.0	0.27 \pm 0.01	102 \pm 5	10	27.9 \pm 2.0	0.35 \pm 0.04	51 \pm 4	131 \pm 6	12
9.07	0.011	21.0 \pm 2.0	0.27 \pm 0.03	102 \pm 5	11	27.7 \pm 2.0	0.35 \pm 0.04	51 \pm 4	133 \pm 6	15
9.26	0.010	20.4 \pm 2.5	0.26 \pm 0.03	102 \pm 4	13	27.7 \pm 2.0	0.34 \pm 0.04	51 \pm 4	135 \pm 6	17
9.45	0.010	20.2 \pm 2.5	0.25 \pm 0.01	103 \pm 5	14	27.9 \pm 2.0	0.34 \pm 0.04	51 \pm 4	138 \pm 6	20
9.63	0.009	19.8 \pm 3.0	0.24 \pm 0.03	105 \pm 5	18	28.1 \pm 2.0	0.33 \pm 0.04	52 \pm 4	140 \pm 6	26
9.78	0.009	19.2 \pm 3.0	0.23 \pm 0.03	105 \pm 5	19	28.1 \pm 2.0	0.32 \pm 0.04	51 \pm 4	143 \pm 6	29
9.92	0.008	19.3 \pm 3.5	0.23 \pm 0.03	105 \pm 4	20	28.6 \pm 2.0	0.32 \pm 0.04	51 \pm 4	145 \pm 6	30
10.09	0.008	19.8 \pm 3.5	0.22 \pm 0.01	105 \pm 4	25	29.3 \pm 2.0	0.31 \pm 0.04	50 \pm 4	147 \pm 6	39
10.26	0.007	20.4 \pm 3.5	0.21 \pm 0.01	106 \pm 4	26	30.4 \pm 2.0	0.30 \pm 0.04	50 \pm 4	149 \pm 6	41
10.42	0.006	20.6 \pm 3.5	0.20 \pm 0.03	107 \pm 4	33	31.0 \pm 2.0	0.29 \pm 0.04	49 \pm 4	152 \pm 6	56
10.58	0.006	20.6 \pm 3.5	0.18 \pm 0.03	108 \pm 5	35	31.0 \pm 2.0	0.27 \pm 0.04	46 \pm 4	155 \pm 6	65
10.71	0.007	20.6 \pm 4.0	0.17 \pm 0.03	109 \pm 5	29	31.1 \pm 2.0	0.26 \pm 0.04	44 \pm 4	157 \pm 6	57
10.84	0.006	19.8 \pm 4.5	0.17 \pm 0.03	111 \pm 4	36	30.7 \pm 2.0	0.25 \pm 0.04	43 \pm 4	160 \pm 6	73
10.99	0.005	19.2 \pm 4.5	0.16 \pm 0.01	112 \pm 4	41	30.4 \pm 2.0	0.24 \pm 0.04	41 \pm 4	162 \pm 6	85
11.14	0.006	18.1 \pm 5.5	0.15 \pm 0.01	113 \pm 4	37	29.2 \pm 2.0	0.22 \pm 0.04	37 \pm 4	165 \pm 6	77
11.29	0.006	17.5 \pm 6.0	0.15 \pm 0.03	114 \pm 3	33	28.6 \pm 2.0	0.21 \pm 0.04	34 \pm 4	167 \pm 6	70
11.43	0.006	16.9 \pm 5.5	0.14 \pm 0.01	115 \pm 4	33	27.7 \pm 2.0	0.20 \pm 0.04	29 \pm 4	169 \pm 6	71
11.55	0.006	16.3 \pm 5.0	0.14 \pm 0.03	115 \pm 5	33	27.8 \pm 2.0	0.19 \pm 0.04	28 \pm 4	171 \pm 6	73
11.67	0.006	16.8 \pm 5.5	0.13 \pm 0.01	117 \pm 4	30	28.8 \pm 2.0	0.19 \pm 0.04	28 \pm 4	173 \pm 6	69
11.81	0.006	15.0 \pm 6.5	0.12 \pm 0.03	117 \pm 4	34	28.9 \pm 2.0	0.18 \pm 0.04	28 \pm 4	175 \pm 6	79
11.95	0.007	14.9 \pm 6.5	0.12 \pm 0.01	117 \pm 4	30	25.5 \pm 2.0	0.13 \pm 0.04	64 \pm 4	146 \pm 6	70

Notes. ^(a) Mean visibility error used for the corresponding wavelength bin (cf. Sect. 4.3); ^(b) reduced chi square.

Appendix B: Diameter details

Table B.1. Details of the diameter measurements presented in the right hand panels of Figs. 6 and 7.

R Aql: Author	Model	Visual phase	Comments
A: Haniff et al. (1995)	UD+G	0.06	UD and Gaussian at 700 and 710 nm
B: Millan-Gabet et al. (2005)	UD	0.90	UD diameter at <i>H</i> and <i>K</i> band
C: Ragland et al. (2006)	UD	0.70	UD diameter at <i>H</i> band
D: Hofmann et al. (2000)	UD	0.17	UD diameter at <i>K</i> band
E: van Belle et al. (1996)	UD	0.90 and 0.31	upper for phase 0.31 and lower for phase 0.90 (<i>K</i> band)
F: this work	FDD	0.0–1.0	full data set with error bars
R Aqr: Author	Model	Visual phase	Comments
A: Tuthill et al. (1999)	UD+G	–	UD and Gaussian at 830 nm
B: Tuthill et al. (2000)	UD	0.12 and 0.68	phase 0.68 for upper/lower point at 2.2/3.1 μm
C: Millan-Gabet et al. (2005)	UD	0.40	UD diameter at <i>J</i> , <i>H</i> and <i>K</i> band
D: Ragland et al. (2006)	UD	0.30	UD diameter at <i>H</i> band
E: Ragland et al. (2008)	UD	0.60–1.11	UD diameters around the <i>H</i> band at different phases
F: Mennesson et al. (2002)	UD	0.41 and 0.51	UD diameter at <i>K</i> and <i>L</i> band
G: van Belle et al. (1996)	UD	0.34 and 0.57	upper for phase 0.34 & lower for phase 0.57 (<i>K</i> band)
H: this work	FDD	0.0–1.0	full data set with error bars
R Hya: Author	Model	Visual phase	Comments
A: Ireland et al. (2004a)	G	0.62	upper for PA 123° & lower for PA 72°
B: Haniff et al. (1995)	UD+G	0.28	UD and Gaussian at 700, 833 and 902 nm
C: Monnier et al. (2004)	UD	0.50	UD diameter at <i>K</i> band
D: Millan-Gabet et al. (2005)	UD	0.80	UD diameters at <i>J</i> , <i>H</i> and <i>K</i> band
E: this work	FDD	0.0–1.0	full data set with error bars
W Hya: Author	Model	Visual phase	Comments
A: Lattanzi et al. (1997)	UD	0.64	two perpendicular axes ($\eta \approx 0.86$, PA $\approx 143^\circ$, 583 nm)
B: Ireland et al. (2004a)	G	0.44	upper curve for PA 120° and lower curve for PA 252°
C: Haniff et al. (1995)	UD	0.04	UD diameter at 700 and 710 nm
D: Tuthill et al. (1999)	G	0.04	elliptical Gaussian at 700 and 710 nm ($\eta \approx 0.94$, PA $\approx 93^\circ$)
E: Monnier et al. (2004)	UD	0.50	UD reported as a bad fit to the data (<i>K</i> band)
F: Woodruff et al. (2009)	UD	0.58–1.53	curves for phase 0.58 (middle), 0.79 (lower) and 1.53 (upper)
G: Woodruff et al. (2008)	UD	0.50–1.00	mean of multiple measurements in given phase range (<i>J</i> , <i>H</i> , <i>K</i> , <i>L</i>)
H: Millan-Gabet et al. (2005)	UD	0.60	UD diameter at <i>H</i> and <i>K</i> band
I: Wishnow et al. (2010)	UD	0.1–1.1	inner UD dust shell diameter at 11.15 μm
J: Bedding et al. (1997)	UD	0.43	UD diameter at 1.45 μm
K: this work	FDD	0.0–1.0	full data set with error bars
V Hya: Author	Model	Visual phase	Comments
A: Ragland et al. (2006)	UD	0.10	UD diameter at <i>H</i> band
B: van Belle et al. (1999)	UD	0.00	UD diameter at <i>H</i> band
C: Millan-Gabet et al. (2003)	UD	–	UD diameter at <i>K</i> band
D: this work	FDD	0.0–1.0	full data set with error bars

Appendix C: Observation log

Table C.1. AT stations used in this study (cf. <http://www.eso.org/sci/facilities/paranal/telescopes/vlti/configuration/index.html>).

Name	AT stations	Ground length	Ground PA	Resolution (at 10 μm)
A	E0-G0	16.006 m	71.020°	128 mas
B	G0-H0	31.998 m	70.998°	64 mas
B*	A0-D0	32.011 m	71.014°	64 mas
C	E0-H0	48.004 m	71.005°	42 mas
D	D0-H0	64.005 m	71.012°	32 mas
E	D0-G1	71.557 m	134.443°	28 mas
F	H0-G1	71.555 m	7.576°	28 mas

Table C.2. Detailed observation logs of R Aql, R Aqr, R Hya, and V Hya.

Observation log of R Aql:										
Date	UT time	P ^a	AT ^b	Disp ^c	Cal ^d	B ^e (m)	PA ^f (°)	Phase ^g	H ^h (°)	QF ⁱ
2007-04-17	09:06:23.779	P79	B	GRISM	2 of 3	29.05	74.77	0.78	53.87	used
2007-04-25	08:09:12.338	P79	D	GRISM	2 of 2	54.90	74.83	0.81	50.84	used
2007-05-09	09:51:15.000	P79	D	GRISM	0 of 1	63.39	71.22	0.85	52.97	not used
2007-06-19	08:25:08.000	P79	B	GRISM	0 of 2	28.98	66.54	0.02	41.70	not used
2007-06-20	03:28:40.000	P79	C	GRISM	4 of 6	34.14	73.90	0.02	41.23	used
2007-06-20	04:42:25.000	P79	B	GRISM	0 of 1	28.64	74.81	0.02	52.51	not used
2007-06-21	08:30:51.000	P79	A	GRISM	0 of 2	14.04	65.19	0.02	39.22	not used
2007-06-22	08:05:24.000	P79	C	GRISM	1 of 1	44.27	67.37	0.02	43.09	used
2007-10-02	23:37:29.000	P80	A	PRISM	1 of 1	16.01	72.65	0.40	56.10	used
2007-10-05	00:24:43.000	P79	B	GRISM	1 of 2	31.24	70.22	0.41	50.57	used
2007-10-05	23:33:31.000	P80	B	PRISM	1 of 1	32.00	72.56	0.41	55.85	used
2007-10-06	23:43:58.000	P80	C	PRISM	2 of 2	47.87	71.90	0.42	54.73	used
2007-10-07	00:11:23.000	P80	C	PRISM	2 of 2	47.08	70.51	0.42	51.29	used
2008-03-06	09:16:57.330	P80	D	PRISM	1 of 1	31.21	69.28	0.98	28.48	used
2008-03-06	09:26:46.124	P80	D	PRISM	1 of 1	33.42	70.36	0.98	30.49	used
2008-03-25	09:31:47.779	P79	A	GRISM	0 of 1	12.33	74.45	0.05	45.38	not used
2008-04-02	09:00:39.945	P81	A	PRISM	3 of 3	12.34	74.46	0.07	45.44	used
2008-04-02	09:39:51.946	P81	C	PRISM	3 of 4	41.50	74.83	0.07	51.25	used
2008-04-04	09:30:40.946	P81	B	PRISM	1 of 1	27.57	74.82	0.08	51.08	used
2008-04-04	09:39:46.960	P81	B	PRISM	1 of 1	28.17	74.82	0.08	52.22	used
2008-04-27	08:24:58.000	P81	D	PRISM	1 of 1	58.66	74.76	0.17	53.96	used
2008-04-27	08:36:46.960	P81	D	PRISM	1 of 1	59.45	74.69	0.17	55.04	used
2008-05-23	05:54:09.000	P79	D	GRISM	1 of 1	52.03	74.69	0.26	47.67	used
2008-05-26	05:17:58.000	P81	D	PRISM	1 of 1	49.44	74.46	0.27	43.68	used
2008-06-01	06:08:05.138	P81	A	PRISM	4 of 4	70.28	128.8	0.30	54.02	used
2008-06-01	06:16:17.960	P81	A	PRISM	4 of 4	69.88	128.8	0.30	54.79	used
2008-06-01	06:56:41.946	P81	A	PRISM	4 of 4	67.14	129.2	0.30	57.02	used
2008-06-01	07:04:33.959	P81	A	PRISM	0 of 4	66.46	129.4	0.30	57.13	not used
2008-06-06	07:46:19.000	P81	A	PRISM	0 of 2	15.96	71.90	0.32	54.21	not used
2008-06-06	09:40:04.000	P81	C	PRISM	0 of 1	41.28	64.31	0.32	36.72	not used
2008-06-07	06:16:17.945	P81	C	PRISM	1 of 1	45.96	74.42	0.32	56.43	used
2008-06-07	06:39:05.000	P81	B	PRISM	3 of 3	31.67	73.66	0.32	57.11	used
2009-04-20	08:01:43.946	P83	B	PRISM	3 of 3	25.57	74.61	0.49	47.18	used
2009-04-23	06:40:13.946	P83	C	PRISM	2 of 6	28.53	72.10	0.50	34.71	used
2009-04-23	07:53:25.946	P83	C	PRISM	6 of 6	38.78	74.66	0.50	47.72	used
2009-05-02	09:38:45.000	P83	D	PRISM	3 of 3	63.97	72.88	0.53	56.23	used
2009-06-03	05:35:12.000	P83	A	PRISM	1 of 3	13.88	74.85	0.65	51.00	used
2009-06-03	06:52:23.000	P83	A	PRISM	1 of 3	15.69	74.01	0.65	57.07	used
2009-06-26	04:31:29.000	P83	D	PRISM	1 of 2	58.70	74.75	0.73	54.09	used
2009-07-03	05:21:54.000	P83	B	PRISM	1 of 2	31.88	73.27	0.76	56.82	used
Observation log of R Aqr:										
Date	UT time	P ^a	AT ^b	Disp ^c	Cal ^d	B ^e (m)	PA ^f (°)	Phase ^g	H ^h (°)	QF ⁱ
2007-05-16	10:06:28.000	P79	D	GRISM	1 of 1	51.09	53.81	0.50	50.38	used
2007-06-18	09:46:44.000	P79	A	GRISM	2 of 4	15.53	67.42	0.59	74.20	used
2007-06-19	09:34:00.000	P79	B	GRISM	0 of 2	30.79	66.67	0.59	72.48	not used
2007-06-20	08:25:38.000	P79	C	GRISM	4 of 6	42.81	61.15	0.59	58.66	used
2007-06-21	06:59:42.000	P79	A	GRISM	2 of 2	11.32	45.06	0.59	40.09	used
2007-07-02	07:18:59.000	P79	B	GRISM	2 of 3	26.64	56.61	0.62	54.29	used
2007-07-27	10:07:03.000	P79	D	GRISM	1 of 1	57.40	78.05	0.68	60.39	used
2007-10-04	06:26:11.000	P79	A	GRISM	0 of 1	12.59	79.91	0.86	49.04	not used
2007-10-04	02:12:15.000	P80	B	PRISM	2 of 2	30.08	64.81	0.86	68.14	used
2007-10-04	04:10:49.000	P80	B	PRISM	2 of 2	31.80	73.85	0.86	77.57	used
2007-10-04	05:28:51.000	P80	A	PRISM	1 of 1	14.50	77.84	0.86	61.91	used
2007-10-05	05:16:14.000	P79	B	GRISM	0 of 2	29.57	77.35	0.86	63.83	not used
2007-10-06	01:57:28.000	P80	C	PRISM	2 of 2	44.52	63.84	0.87	66.67	used
2007-10-07	05:54:46.000	P79	C	GRISM	1 of 1	40.31	79.13	0.87	53.48	used
2007-10-07	01:16:29.000	P80	C	PRISM	2 of 2	41.29	58.76	0.87	58.52	used
2007-10-07	02:00:53.165	P80	A	PRISM	1 of 1	14.88	64.02	0.87	68.23	used
2007-11-30	00:31:14.000	P80	D	PRISM	0 of 1	47.51	74.32	0.01	76.85	not used
2007-12-02	00:23:50.000	P80	D	PRISM	0 of 3	63.42	74.20	0.01	76.78	not used
2008-05-22	09:16:47.000	P81	D	PRISM	0 of 3	48.10	49.62	0.43	45.12	not used

Notes. ^(a) Semester of proposal. ^(b) AT station: A = E0–G0, B = G0–H0, B* = A0–D0, C = E0–H0, D = D0–H0, E = D0–G1 or F = H0–G1 (cf. Table C). ^(c) Dispersive element. ^(d) Calibrators used out of those available. ^(e) Projected baseline length. ^(f) Position angle of the projected baseline on the sky. ^(g) Visual light phase. ^(h) Elevation. ⁽ⁱ⁾ Quality flag showing if that observation is used for the model fitting or not.

Table C.2. continued.

Date	UT time	P ^a	AT ^b	Disp ^c	Cal ^d	B ^e (m)	PA ^f (°)	Phase ^g	H ^h (°)	QF ⁱ
2008-05-30	07:15:31.945	P80	D	PRISM	0 of 5	36.48	21.26	0.47	24.69	not used
2008-05-30	09:49:08.137	P80	D	PRISM	2 of 5	55.36	59.13	0.47	59.52	used
2008-06-06	08:15:59.945	P81	A	PRISM	0 of 2	11.72	47.73	0.49	44.70	not used
2008-06-06	09:53:36.946	P81	C	PRISM	1 of 1	44.07	63.13	0.49	66.54	used
2008-06-07	09:21:11.000	P81	B	PRISM	3 of 3	28.21	60.38	0.49	60.30	used
2008-06-07	09:54:00.945	P81	B	PRISM	3 of 3	29.58	63.60	0.49	67.47	used
2008-09-25	05:26:02.000	P81	D	PRISM	1 of 1	61.26	76.25	0.78	69.53	used
2008-09-28	05:26:37.330	P81	A	PRISM	1 of 1	15.23	76.49	0.78	66.90	used
2008-12-28	01:14:16.000	P82	A	PRISM	0 of 1	12.25	80.18	0.01	43.58	not used
2008-12-31	00:43:23.000	P82	B	PRISM	1 of 2	26.09	79.50	0.02	47.72	used
2008-12-31	01:14:25.000	P82	B	PRISM	1 of 2	23.39	80.52	0.02	40.95	used
2009-01-01	00:12:38.000	P82	C	PRISM	1 of 1	39.63	79.35	0.03	53.72	used
2009-05-25	09:28:26.000	P83	D	PRISM	0 of 1	50.56	53.10	0.39	50.22	not used
2009-06-03	09:04:03.000	P83	A	PRISM	2 of 3	13.01	55.02	0.42	52.70	used
2009-06-03	09:40:43.000	P83	C	PRISM	1 of 1	42.32	60.38	0.42	60.93	used
2009-07-03	06:48:28.000	P83	B	PRISM	1 of 2	24.83	51.87	0.50	48.71	used
2009-07-30	08:40:36.000	P83	D	PRISM	1 of 1	63.29	74.41	0.57	75.51	used
2009-08-14	08:16:39.000	P83	C	PRISM	0 of 1	45.81	76.36	0.62	68.58	not used
2009-08-14	08:38:16.000	P83	A	PRISM	0 of 1	14.85	77.26	0.62	63.93	not used
2009-08-14	09:30:22.000	P83	B	PRISM	0 of 1	26.11	79.49	0.62	52.30	not used
Observation log of R Hya:										
Date	UT time	P ^a	AT ^b	Disp ^c	Cal ^d	B ^e (m)	PA ^f (°)	Phase ^g	H ^h (°)	QF ⁱ
2007-04-12	02:08:09.000	P79	A	GRISM	2 of 3	13.48	48.88	0.60	52.64	used
2007-04-17	07:28:33.338	P79	B	GRISM	2 of 3	24.73	86.35	0.61	49.77	used
2007-04-18	07:10:38.780	P79	A	GRISM	3 of 3	12.92	85.18	0.61	52.93	used
2007-04-22	01:35:49.071	P79	D	GRISM	8 of 8	54.75	50.43	0.62	55.11	used
2007-04-22	07:13:32.070	P79	D	GRISM	8 of 8	48.03	87.13	0.62	47.83	used
2007-04-25	01:23:03.779	P79	E	GRISM	0 of 2	63.50	123.9	0.63	54.00	not used
2007-04-25	04:23:39.780	P79	F	GRISM	2 of 2	71.55	9.98	0.63	84.59	used
2007-05-16	23:52:59.000	P79	B	GRISM	0 of 1	27.96	52.53	0.69	52.30	not used
2007-06-20	01:20:22.000	P79	C	GRISM	6 of 6	46.25	77.60	0.78	76.25	used
2007-06-21	22:54:49.000	P79	C	GRISM	1 of 1	46.13	62.66	0.78	71.24	used
2007-07-02	23:17:47.000	P79	C	GRISM	5 of 5	47.95	69.99	0.81	86.20	used
2007-07-02	01:42:07.000	P79	C	GRISM	0 of 5	41.92	82.60	0.81	60.55	not used
2007-07-03	22:54:48.000	P79	A	GRISM	0 of 2	15.91	68.30	0.82	81.96	not used
2007-07-03	00:28:49.000	P79	A	GRISM	2 of 2	15.57	76.81	0.82	76.34	used
2007-07-04	23:58:37.000	P79	B	GRISM	0 of 4	31.72	74.45	0.82	82.30	not used
2007-07-04	02:19:46.000	P79	B	GRISM	0 of 4	24.68	86.41	0.82	50.24	not used
2007-12-26	08:39:14.000	P79	D	GRISM	1 of 1	51.86	44.87	0.29	45.73	used
2008-02-20	07:53:42.000	P80	D	PRISM	4 of 4	63.89	69.61	0.44	85.31	used
2008-02-20	08:42:11.000	P80	D	PRISM	6 of 4	63.50	74.33	0.44	83.27	used
2008-02-21	09:02:26.000	P79	D	GRISM	0 of 2	62.50	76.42	0.44	77.80	used
2008-02-22	07:02:15.000	P80	B*	PRISM	0 of 6	31.22	64.71	0.45	75.47	not used
2008-02-22	07:54:30.156	P80	B*	PRISM	0 of 6	32.00	70.49	0.45	87.16	not used
2008-03-02	06:36:33.000	P80	E	PRISM	2 of 2	70.92	129.9	0.47	77.67	used
2008-03-02	07:52:58.000	P80	F	PRISM	1 of 2	71.55	10.27	0.47	84.61	used
2008-03-02	08:28:33.000	P80	D	PRISM	2 of 2	62.29	76.75	0.47	76.56	used
2008-03-13	04:43:47.000	P80	B	PRISM	7 of 8	29.03	56.32	0.50	61.84	used
2008-03-13	07:00:13.945	P80	B	PRISM	7 of 8	31.97	72.36	0.50	86.68	used
2008-03-13	09:09:41.945	P80	B	PRISM	7 of 8	27.22	83.52	0.50	57.36	used
2008-03-14	05:39:07.000	P80	A	PRISM	4 of 6	15.57	64.36	0.50	75.34	used
2008-03-14	07:02:11.000	P80	A	PRISM	4 of 6	15.96	73.21	0.50	85.40	used
2008-03-14	08:51:47.000	P80	A	PRISM	4 of 6	13.98	82.60	0.50	60.53	used
2008-03-25	06:08:58.000	P80	C	PRISM	6 of 6	47.97	72.15	0.53	87.51	used
2008-03-25	07:59:34.945	P80	C	PRISM	6 of 6	42.97	81.63	0.53	62.57	used
2008-03-31	04:48:31.000	P80	C	PRISM	1 of 1	47.29	66.29	0.54	79.04	used
2008-04-01	03:50:22.946	P81	B	PRISM	2 of 2	29.75	58.88	0.55	66.69	used
2008-04-02	06:42:37.945	P81	C	PRISM	4 of 4	46.11	77.84	0.55	72.93	used
2008-04-02	08:01:14.946	P81	A	PRISM	3 of 3	13.26	84.39	0.55	55.05	used
2008-04-03	07:04:02.946	P81	B	PRISM	2 of 2	29.69	79.96	0.55	67.16	used
2008-04-28	01:55:35.946	P81	D	PRISM	6 of 6	58.79	57.60	0.62	64.72	used
2008-04-28	02:57:39.946	P81	E	PRISM	2 of 2	70.99	130.1	0.62	78.85	used
2008-04-28	04:06:01.945	P81	F	PRISM	1 of 2	71.55	9.69	0.62	85.24	used
2008-04-28	07:13:08.945	P81	D	PRISM	6 of 6	44.07	89.17	0.62	42.84	used
2008-05-25	00:16:55.000	P81	D	PRISM	2 of 2	59.74	59.31	0.69	66.43	used
2008-07-03	01:31:24.000	P81	A	PRISM	1 of 2	14.10	82.30	0.79	61.43	used

Table C.2. continued.

Date	UT time	P ^a	AT ^b	Disp ^c	Cal ^d	B ^e (m)	PA ^f (°)	Phase ^g	H ^h (°)	QF ⁱ
2008-07-03	02:43:24.000	P81	C	PRISM	2 of 2	33.75	88.69	0.79	45.14	used
2008-07-06	03:20:45.000	P81	D	PRISM	2 of 2	35.68	93.62	0.80	34.14	used
2009-01-16	08:03:46.946	P82	F	PRISM	4 of 5	71.54	-7.84	0.32	57.04	used
2009-01-16	08:34:11.000	P82	D	PRISM	1 of 2	58.75	57.54	0.32	63.95	used
2009-01-17	07:50:45.946	P82	E	PRISM	2 of 2	63.99	124.0	0.32	54.99	used
2009-01-21	07:17:41.000	P81	B	PRISM	5 of 5	26.59	47.49	0.33	51.06	used
2009-01-21	09:02:59.000	P82	B	PRISM	5 of 5	31.10	64.15	0.33	74.98	used
2009-01-22	07:23:42.945	P81	C	PRISM	4 of 5	40.45	48.91	0.34	53.31	used
2009-01-22	07:36:00.946	P81	C	PRISM	4 of 5	41.40	51.25	0.34	56.10	used
2009-01-25	08:13:46.945	P82	A	PRISM	8 of 8	14.94	59.33	0.34	67.36	used
2009-01-25	08:50:11.945	P82	A	PRISM	8 of 8	15.56	64.18	0.34	75.65	used
2009-01-26	09:11:32.000	P82	B	PRISM	1 of 1	31.71	67.44	0.35	81.40	used
2009-01-27	08:13:44.945	P82	C	PRISM	4 of 4	45.26	60.42	0.35	69.14	used
2009-01-27	08:39:07.946	P82	C	PRISM	4 of 4	46.52	63.77	0.35	74.92	used
2009-01-27	08:46:50.123	P82	C	PRISM	4 of 4	46.83	64.72	0.35	76.68	used
2009-02-16	07:39:19.000	P82	D	PRISM	2 of 2	63.27	66.95	0.40	79.20	used
2009-03-16	08:08:24.000	P82	D	PRISM	2 of 3	59.80	79.60	0.48	68.84	used
2009-03-16	08:36:32.000	P81	D	PRISM	2 of 3	56.78	82.00	0.48	62.43	used
2009-04-20	07:34:42.945	P83	B	PRISM	2 of 3	23.02	88.14	0.57	45.29	used
2009-04-23	05:28:10.000	P83	C	PRISM	6 of 6	45.43	78.85	0.58	71.30	used
2009-04-23	07:05:14.946	P83	C	PRISM	6 of 6	36.81	86.57	0.58	49.27	used
2009-04-24	06:05:35.000	P83	B	PRISM	2 of 2	28.16	82.31	0.58	61.90	used
2009-05-02	01:44:52.000	P83	D	PRISM	3 of 3	59.37	58.63	0.60	65.64	used
2009-05-03	01:50:41.946	P83	E	PRISM	2 of 2	68.81	126.7	0.61	67.85	used
2009-05-03	06:19:20.000	P83	F	PRISM	1 of 3	70.55	22.78	0.61	50.75	used
2009-05-24	23:13:50.000	P83	D	PRISM	1 of 1	53.58	48.26	0.66	51.89	used
2009-06-04	23:30:42.000	P83	C	PRISM	3 of 3	44.27	58.02	0.69	64.64	used
2009-06-04	03:46:00.000	P83	A	PRISM	1 of 2	13.39	84.09	0.69	56.99	used
Observation log of V Hya:										
Date	UT time	P ^a	AT ^b	Disp ^c	Cal ^d	B ^e (m)	PA ^f (°)	Phase ^g	H ^h (°)	QF ⁱ
2007-04-12	03:45:42.000	P79	A	GRISM	3 of 3	15.01	78.79	0.68	68.63	used
2007-04-14	04:01:23.388	P79	C	GRISM	1 of 1	43.49	80.29	0.68	63.90	used
2007-04-14	04:56:33.000	P79	B	GRISM	0 of 1	24.46	84.98	0.68	50.71	not used
2007-04-22	23:36:20.000	P79	D	GRISM	1 of 8	58.41	58.54	0.70	63.41	used
2007-04-22	03:48:12.779	P79	D	GRISM	2 of 8	55.34	81.89	0.70	58.22	used
2007-12-02	07:58:13.000	P80	D	PRISM	0 of 3	52.05	48.04	0.12	50.30	not used
2007-12-02	08:58:00.000	P80	D	PRISM	1 of 3	58.65	58.93	0.12	63.90	used
2007-12-12	06:16:34.000	P80	F	PRISM	1 of 1	71.54	-16.21	0.14	36.30	used
2007-12-12	07:28:52.000	P80	D	PRISM	2 of 3	53.33	50.29	0.14	52.60	used
2007-12-12	08:19:04.000	P80	E	PRISM	1 of 1	68.45	126.5	0.14	64.00	used
2007-12-12	09:05:20.166	P80	D	PRISM	2 of 3	61.77	64.26	0.14	74.50	used
2008-01-10	07:13:33.000	P80	B	PRISM	2 of 2	31.14	65.29	0.20	76.50	used
2008-01-10	05:03:32.000	P79	B	GRISM	1 of 1	25.01	44.22	0.20	45.49	used
2008-01-11	04:54:29.000	P80	B	PRISM	1 of 1	24.73	43.11	0.20	45.60	used
2008-01-12	05:27:07.000	P80	A	PRISM	0 of 2	13.39	50.69	0.20	52.60	not used
2008-01-12	06:18:56.000	P80	A	PRISM	0 of 2	14.65	58.83	0.20	64.40	not used
2008-01-12	04:37:00.000	P79	A	GRISM	0 of 1	11.96	39.65	0.20	41.26	not used
2008-02-20	04:42:41.000	P80	D	PRISM	0 of 4	62.75	66.32	0.28	78.50	not used
2008-02-21	03:27:22.000	P80	D	PRISM	0 of 3	57.55	57.17	0.28	61.20	not used
2008-02-22	03:37:17.000	P80	B*	PRISM	0 of 6	29.39	59.09	0.28	64.30	not used
2008-02-22	04:25:40.000	P80	B*	PRISM	0 of 6	31.15	65.28	0.28	75.30	not used
2008-03-11	02:14:28.945	P80	A	PRISM	3 of 3	14.29	56.53	0.31	61.60	used
2008-03-11	02:48:44.946	P80	A	PRISM	3 of 3	15.05	61.44	0.31	69.40	used
2008-03-13	01:21:28.946	P80	B	PRISM	7 of 8	26.17	48.54	0.32	51.30	used
2008-03-13	01:53:55.946	P80	B	PRISM	7 of 8	27.93	54.46	0.32	58.70	used
2008-03-13	03:34:35.946	P80	B	PRISM	7 of 8	31.64	67.68	0.32	81.40	used
2008-03-25	02:22:58.000	P80	C	PRISM	6 of 6	46.74	65.36	0.34	76.70	used
2008-03-25	02:02:04.000	P79	C	GRISM	1 of 1	45.74	62.80	0.34	71.28	used
2008-03-27	00:03:49.946	P80	A	PRISM	1 of 1	12.56	44.63	0.34	47.10	used
2008-03-27	00:54:34.945	P80	C	PRISM	1 of 2	41.87	54.41	0.34	58.60	used
2008-04-02	05:13:23.946	P81	C	PRISM	2 of 4	40.95	82.29	0.35	56.96	used
2008-04-07	00:24:01.946	P81	A	PRISM	1 of 1	14.18	55.86	0.36	60.61	used
2008-04-07	01:01:29.000	P81	C	PRISM	1 of 1	45.24	61.65	0.36	69.13	used
2008-04-07	01:47:45.945	P81	B	PRISM	2 of 2	31.47	66.78	0.36	79.52	used
2008-04-08	00:39:00.946	P81	A	PRISM	1 of 1	14.64	58.73	0.36	64.91	used
2008-04-08	01:37:05.946	P81	B	PRISM	2 of 2	31.32	66.04	0.36	78.03	used

Table C.2. continued.

Date	UT time	P ^a	AT ^b	Disp ^c	Cal ^d	B ^e (m)	PA ^f (°)	Phase ^g	H ^h (°)	QF ⁱ
2008-04-28	01:24:40.000	P81	D	PRISM	6 of 6	63.91	72.77	0.40	84.97	used
2008-11-30	07:49:13.000	P81	D	PRISM	1 of 1	51.02	46.15	0.81	47.18	used
2008-12-27	07:24:08.000	P82	A	PRISM	1 of 1	14.84	60.02	0.86	65.61	used
2008-12-27	08:14:23.000	P80	C	PRISM	0 of 1	47.04	66.21	0.86	76.98	not used
2009-01-16	05:01:58.946	P82	E	PRISM	0 of 1	62.98	124.5	0.90	57.84	not used
2009-01-16	06:54:20.000	P82	F	PRISM	4 of 5	71.35	1.97	0.90	76.67	used
2009-01-19	06:37:49.000	P82	D	PRISM	2 of 2	62.41	65.54	0.91	75.61	used
2009-01-19	06:51:54.959	P82	D	PRISM	2 of 2	62.80	66.42	0.91	78.75	used
2009-01-20	04:05:35.000	P80	C	PRISM	2 of 4	36.00	39.97	0.91	41.95	used
2009-01-20	04:50:06.946	P82	C	PRISM	1 of 4	39.53	49.19	0.91	52.04	used
2009-01-20	06:41:18.946	P82	B	PRISM	1 of 1	31.23	65.66	0.91	77.27	used
2009-01-22	05:59:08.945	P82	B	PRISM	0 of 1	30.12	61.51	0.91	69.54	not used
2009-01-22	06:07:04.959	P82	B	PRISM	0 of 1	30.41	62.53	0.91	71.34	not used
2009-01-22	06:42:31.946	P82	C	PRISM	3 of 5	47.18	66.67	0.91	79.28	used
2009-01-25	03:35:25.945	P82	A	PRISM	2 of 8	11.64	36.53	0.92	39.57	used
2009-01-25	07:17:58.945	P82	A	PRISM	8 of 8	16.01	71.37	0.92	86.60	used
2009-02-19	01:53:34.000	P82	D	PRISM	0 of 1	46.81	37.21	0.97	38.77	not used
2009-02-27	06:54:56.945	P82	B	PRISM	1 of 1	29.27	79.89	0.98	64.50	used
2009-02-28	03:28:46.946	P82	B	PRISM	2 of 2	29.92	60.86	0.98	68.43	used
2009-02-28	04:04:29.946	P82	B	PRISM	2 of 2	31.14	65.27	0.98	76.49	used
2009-03-08	00:42:31.015	P82	C	PRISM	3 of 3	34.29	34.38	1.00	37.82	used
2009-03-08	02:14:47.000	P80	C	PRISM	3 of 3	42.15	55.01	1.00	58.75	used
2009-03-08	02:52:36.000	P80	C	PRISM	3 of 3	44.78	60.63	1.00	67.36	used
2009-03-08	03:50:00.000	P82	A	PRISM	1 of 1	15.81	67.46	1.00	80.24	used
2009-03-17	03:16:00.000	P82	D	PRISM	2 of 2	63.26	67.61	0.01	80.54	used
2009-03-17	03:48:12.000	P82	D	PRISM	2 of 2	63.98	70.78	0.01	86.38	used
2009-05-03	23:43:46.000	P83	D	PRISM	0 of 2	62.16	65.02	0.09	75.35	not used